

# **A Life-Cycle Model of Trans-Atlantic Employment Experiences**

Sagiri Kitao

Keio University

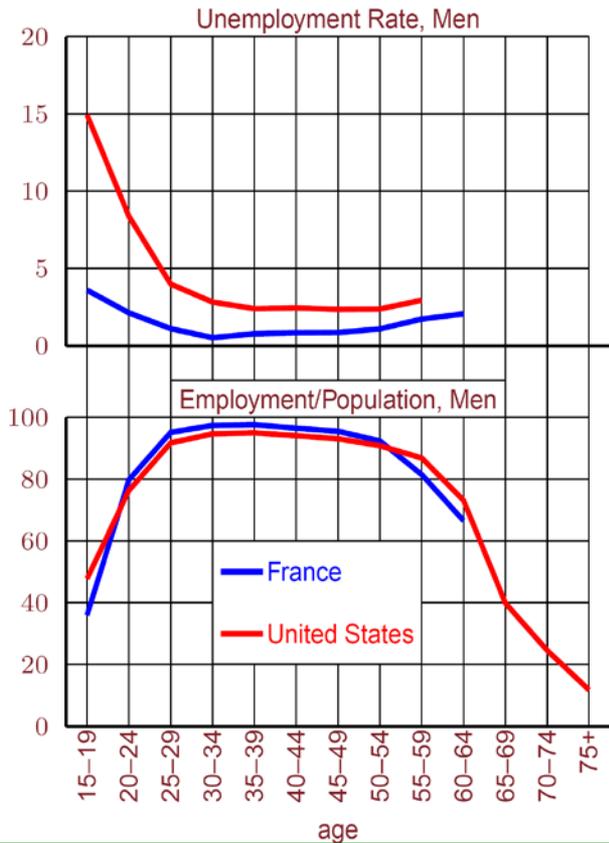
Lars Ljungqvist

Stockholm School of Economics and New York University

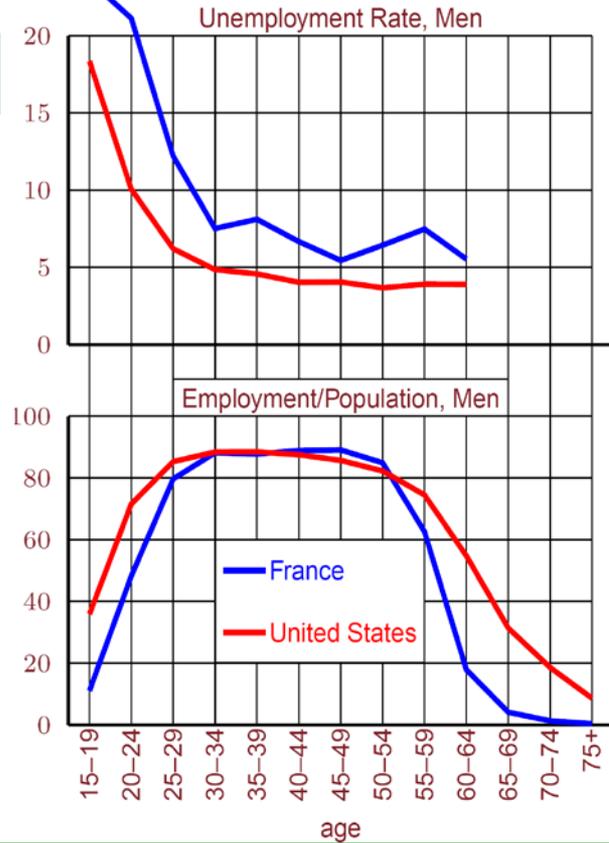
Thomas J. Sargent

New York University and Hoover Institution

1970



2004



Source:  
OECD  
via Shimer

Extension of turbulence theory by

Ljungqvist and Sargent (1998)

– “ – (2008)

Empirical motivation from  
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N(0.7, 0.02) truncated to interval [0,1],

and become experienced with prob. 0.33

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shock with variance 0.04

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layoff costs

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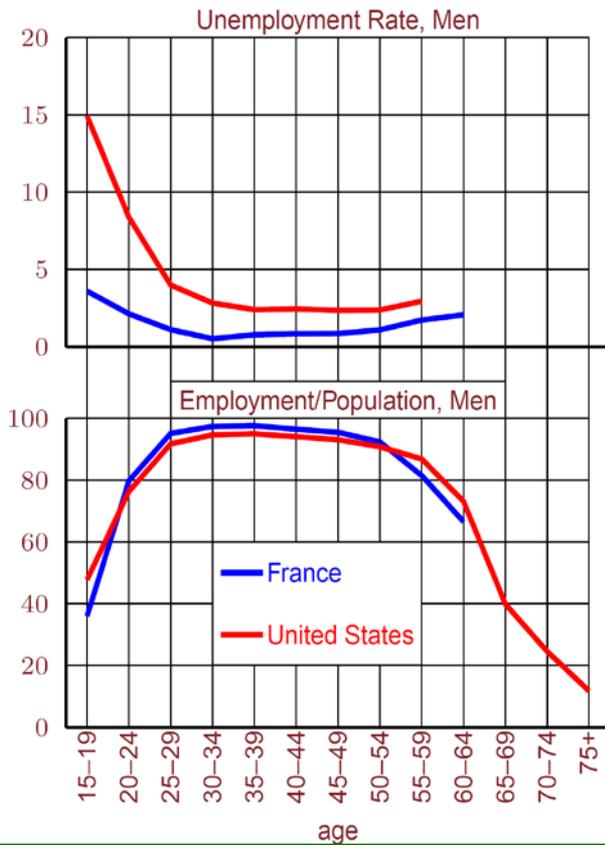
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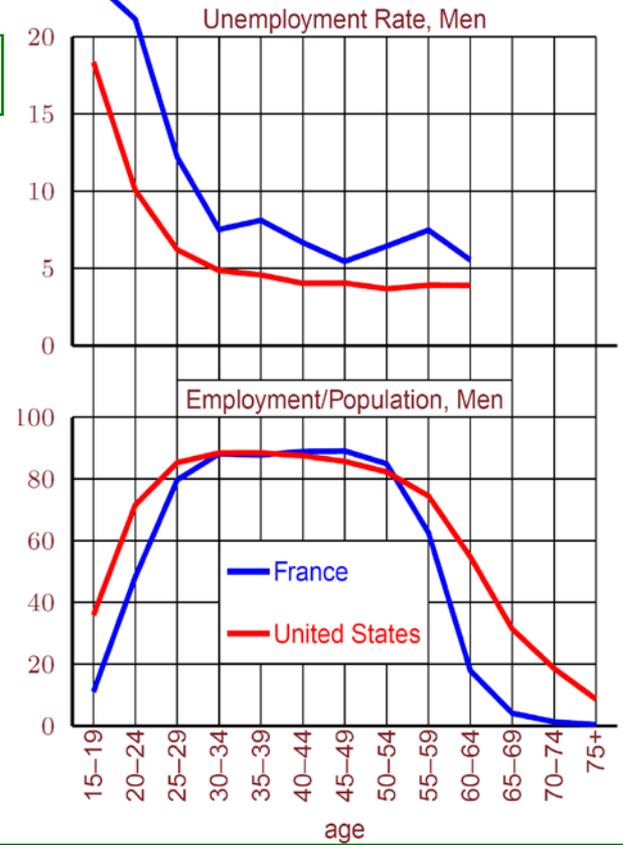
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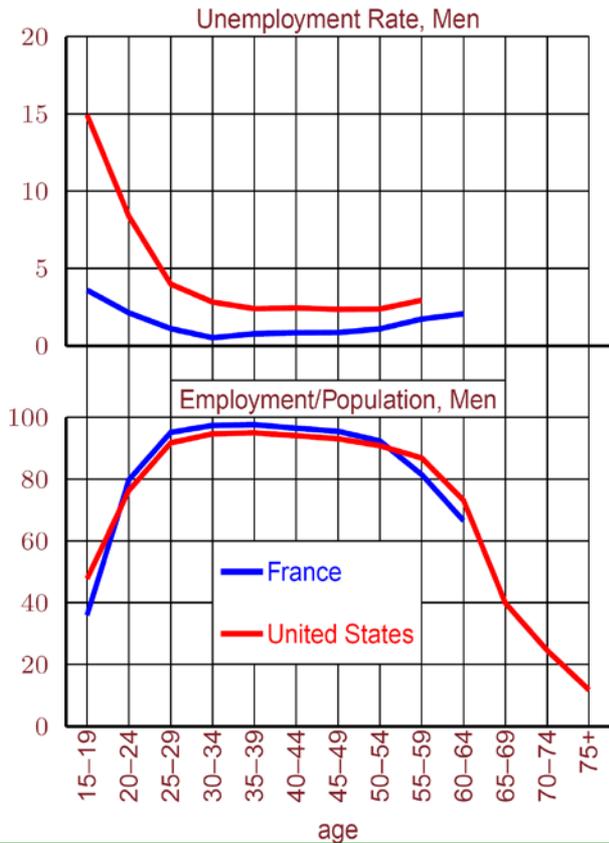
Source:  
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Benefit dependency rates<sup>c</sup>

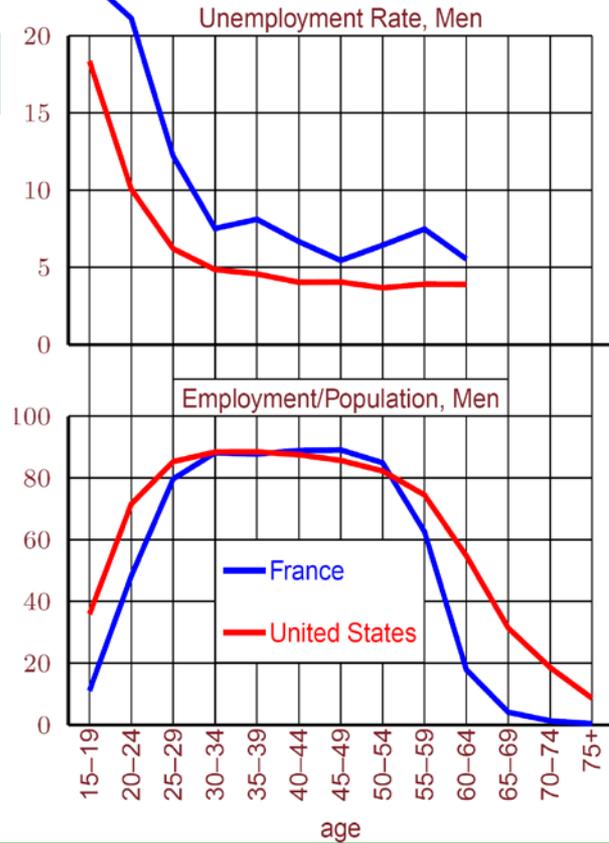
	1980	1990	1999
France	13.9	20.2	24.2
Germany	15.2	18.1	22.4
United States	16.8	15.6	13.7

Source: OECD Employment Outlook 2003

1970

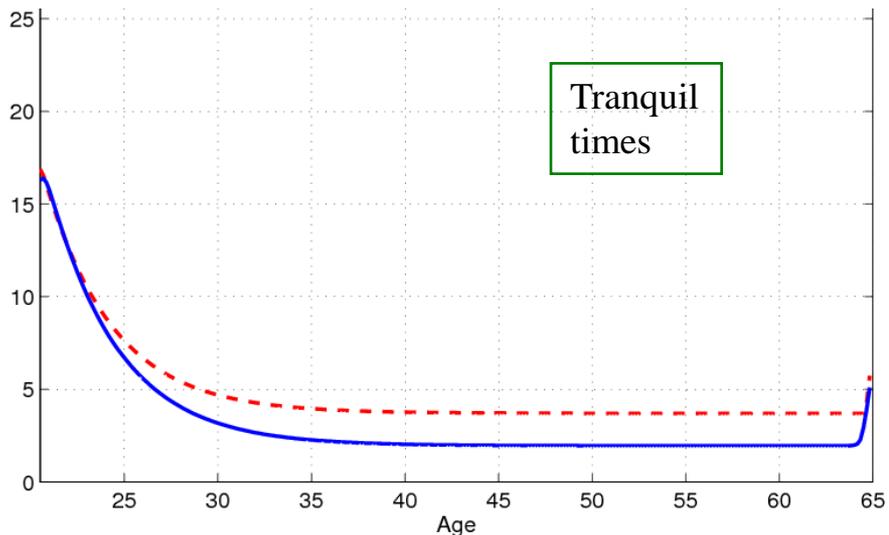


2004

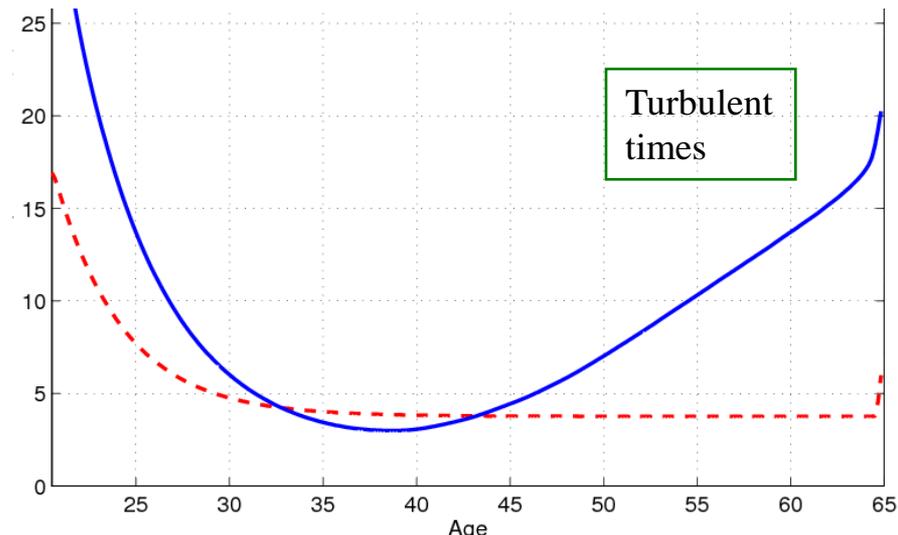


Source: OECD via Shimer

Tranquil times



Turbulent times



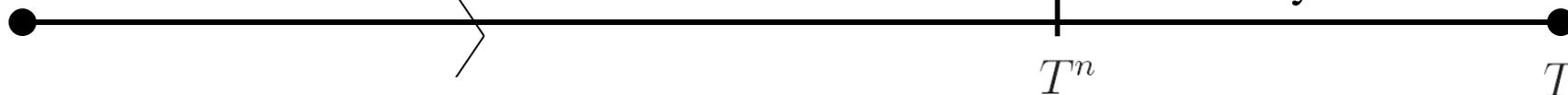
# OLG search-island model with indivisible labor

**Ex ante heterogeneity:** 2 types (L and H)  
distinguished by parameters of

**McCall productivity distribution** in a phase of 'inexperience' (high job destruction probability)

**Ben-Porath human capital technology** in a phase of 'experience' (lower job destruction probability)

**Ex post heterogeneity:**

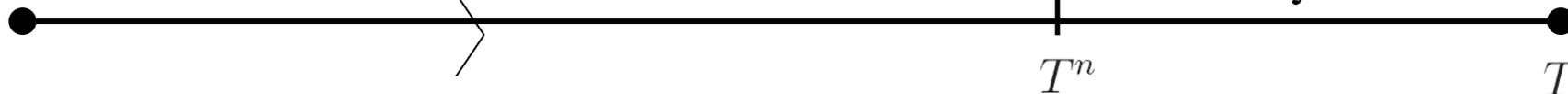


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## **Ex post heterogeneity:**

- time to become experienced
- job search luck
- job destruction luck
- i.i.d. earnings shocks
- human capital investments
- ... and depreciation at job destructions ('turbulence')
- financial savings

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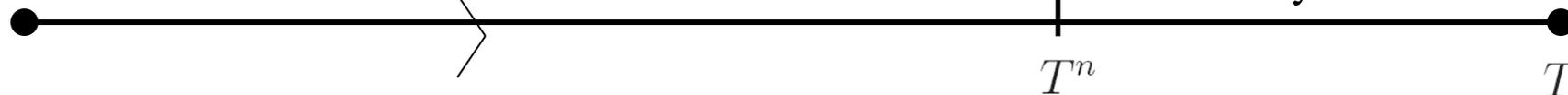
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## **Government**

- labor and capital taxes
- layoff tax
- UI benefits
- social security
- (minimum wage)

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## **Ways to smooth consumption:**

- trade a risk-free asset
- invest in human capital
- career planning
- social safety net (UI)
- social security

**Agents** 2 types;  $i = L, H$  [ low type (high school) , high type (college) ]

Preferences  $E_0 \sum_{t=0}^T \beta^t [\log c_t - B_t]$

$B_t = B$  employed (indivisible labor)

$B_t = B^u(s_t)$  unemployed (search intensity  $s_t$ )

$B_t = 0$  inactive (incl. retirement)

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**Career path** working age 20-65, mandatory retirement 66-90 { survival prob.  $m_t$  }

(1) 'Inexperienced':



transition probability  $\pi$

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(2) 'Experienced': efficiency units  $h_t(1 - l_t)$ , { human capital  $h_t$  , investment  $l_t \in [0, 1]$  }

Ben-Porath technology  $h_{t+1} = h_t + A_i(h_t l_t)^\nu$  (no depreciation)

convert into bimonthly transition probabilities  $H_i^n(h, h'; l)$

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**Turbulence** transition probability at an exogenous job termination  $H_i^\lambda(h', h'')$

**Firms** each firm creates a single job

Production function  $F(z, k, n) = z k^\alpha n^{1-\alpha}$

$z$  job-specific productivity level Markov transition kernel  $Z(z, z')$

$k$  physical capital (depreciation rate  $\delta$ )

$\mu$  cost of creating a new job (with productivity level  $z_{\text{initial}}$ )

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**Search-island model** (Alvarez and Veracierto, 2001)

$B^u(s_t)$  disutility of search

$S(s_t)$  prob. of finding labor market next period

- workers and firms are randomly matched each period
- after observing worker, firm hires profit-maximizing capital
- anonymous labor market with a market-clearing wage rate per efficiency unit of labor

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**Endogenous and**

**exogenous separations:**

$q$  prob. firm destroys job endogenously

$\lambda$  exogenous destruction

$\bar{\lambda} - \lambda$  additional exog. breakups for inexperienced

# Value functions

Value function	phase of life	decisions
$\tilde{V}_i^u(a, \gamma, d, t)$	inexperienced, unemployed	$c, a', s$
$\tilde{V}_i^n(a, n, t)$	inexperienced, employed	$c, a'$
$V_i^u(a, h, \gamma, d, t)$	experienced, unemployed	$c, a', s$
$V_i^n(a, h, t)$	experienced, employed	$c, a', l$
$\hat{V}(a, t)$	old, retired	$c, a'$
$V^f(z)$	firm	{stay, exit}, $k$

$a$	assets	$h$	human capital
$\gamma$	UI benefits	$i$	skill type
$d$	elapsed duration	$c$	consumption
$t$	age	$s$	search intensity
$n$	inexperienced efficiency units	$l$	investment in skills

## Parameters set outside the model

- |                                     |  |   |
|-------------------------------------|--|---|
| (a) government policies             |  | (public expenditures clear the government b.c.) |
| (b) aggregate production technology |  |   |
| (c) real interest rate, 4%          |  | (do not model top 5% of the population)         |

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## Parameters estimated/calibrated within the model to U.S. data

- |                                     |  |
|-------------------------------------|--|
| (1) Subjective discount factor      | Fraction of wealth held by 95% of population   |
| (2) Ben-Porath technology           | Earnings profiles (college and non-college)  |
| (3) Search technology               | Average unemployment duration  |
| (4) Idiosyncratic firm productivity | Average number of jobs held over a lifetime and 'equilibrium response' to layoff taxes |
| (5) Disutility of work              | Cross-time and cross-continent unemployment and permanent earnings volatility          |

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## Check auxiliary implications

- (i) life-cycle profiles of asset holdings and consumption
- (ii) unemployment duration and long-term unemployment by age group
- (iii) autocorrelations of individual earnings at different lag orders and by age group

# Government

$\Gamma(e)$	UI, last labor earnings $e$
$d_{\max}$	UI duration
$\Omega$	job destruction tax
$e_{\min}$	minimum wage
$\tau_n$	labor tax rate
$\tau_p$	social security tax rate
$\tau_k$	capital tax rate
$\hat{e}$	retirement benefit
$X$	public consumption

# Government

U.S.

Europe

$\Gamma(e)$	UI, last labor earnings $e$	60 % replacement rate	
$d_{\max}$	UI duration	6 months	unlimited duration
$\Omega$	job destruction tax		
$e_{\min}$	minimum wage		
$\tau_n$	labor tax rate		
$\tau_p$	social security tax rate		
$\tau_k$	capital tax rate		
$\hat{e}$	retirement benefit		
$X$	public consumption		

OECD Economic Studies (1996):

Net unemployment benefit replacement rates  
in 1994 for single-earner households, in percent

	U.S.	France	Germany
first year	34 (38)	79 (80)	66 (74)
second and third year	9 (14)	63 (62)	63 (72)
fourth and fifth year	9 (14)	61 (60)	63 (72)
without (with) dependent spouse			

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Hunt (J. of Labor Economics, 1995):

German unemployment benefits in 1983

First 12 months      ‘Arbeitslosengeld’      68% replacement rate

Thereafter,          ‘Arbeitslosenhilfe’      58% replacement rate  
unlimited duration, means tested

# Government

U.S.

Europe

		U.S.	Europe
$\Gamma(e)$	UI, last labor earnings $e$	60 % replacement rate	
$d_{\max}$	UI duration	6 months	unlimited duration
$\Omega$	job destruction tax	0	3 months of low-type earnings
$e_{\min}$	minimum wage	no	yes, in turbulent times
$\tau_n$	labor tax rate		
$\tau_p$	social security tax rate		
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Europe

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$\tau_n$	labor tax rate	15%	30%
$\tau_p$	social security tax rate	10%	10%
$\tau_k$	capital tax rate	15%	15%
$\hat{e}$	retirement benefit		
$X$	public consumption		

Mendoza et al. (JME, 1994) and

<http://www.econ.umd.edu/~mendoza/pp/newtaxdata.pdf>

Tax on labor income

U.S. 28%

France 46%

Germany 41%

# Government

U.S.

Europe

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$\tau_p$	social security tax rate	10%	10%
$\tau_k$	capital tax rate	15%	15%
$\hat{e}$	retirement benefit	Based on replacement rate of average earnings	
		40%	50%
$X$	public consumption		

OECD study (2006): Gross replacement rate of average earnings	U.S.	France	Germany
	38.6%	52.9%	45.8%

# Government

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Europe

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$X$	public consumption		

Residual

# Ben-Porath technology

## Target:

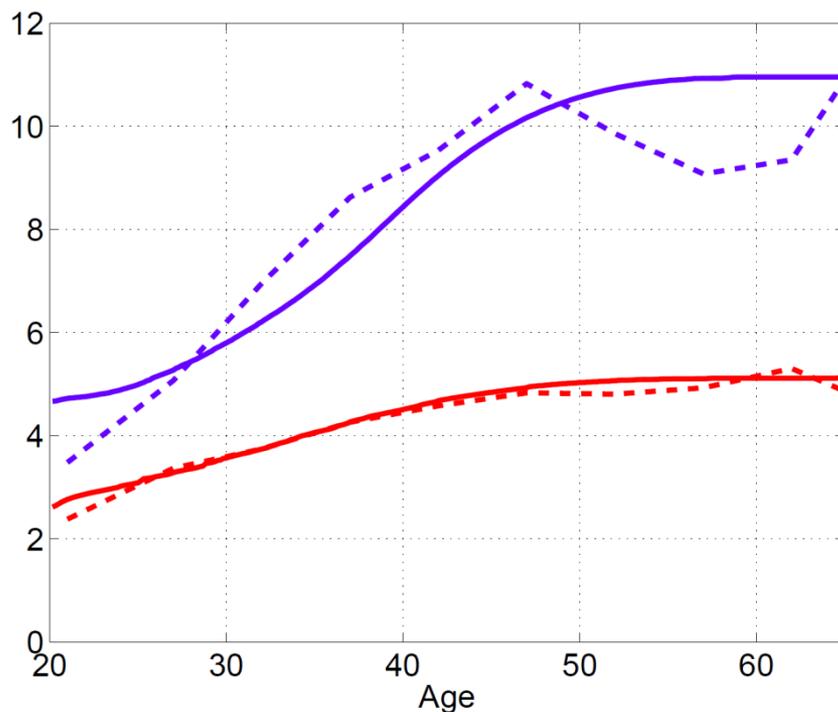
U.S. Census 2006  
non-college and college graduates

## Model:

Experienced workers  $h' = h + A_i(hl)^\nu$   
with type-specific  $A_i, h_{o,i}$

Inexperienced workers  $G_i(n)$   
normal dist. on  $[0, \rho h_{o,i}]$

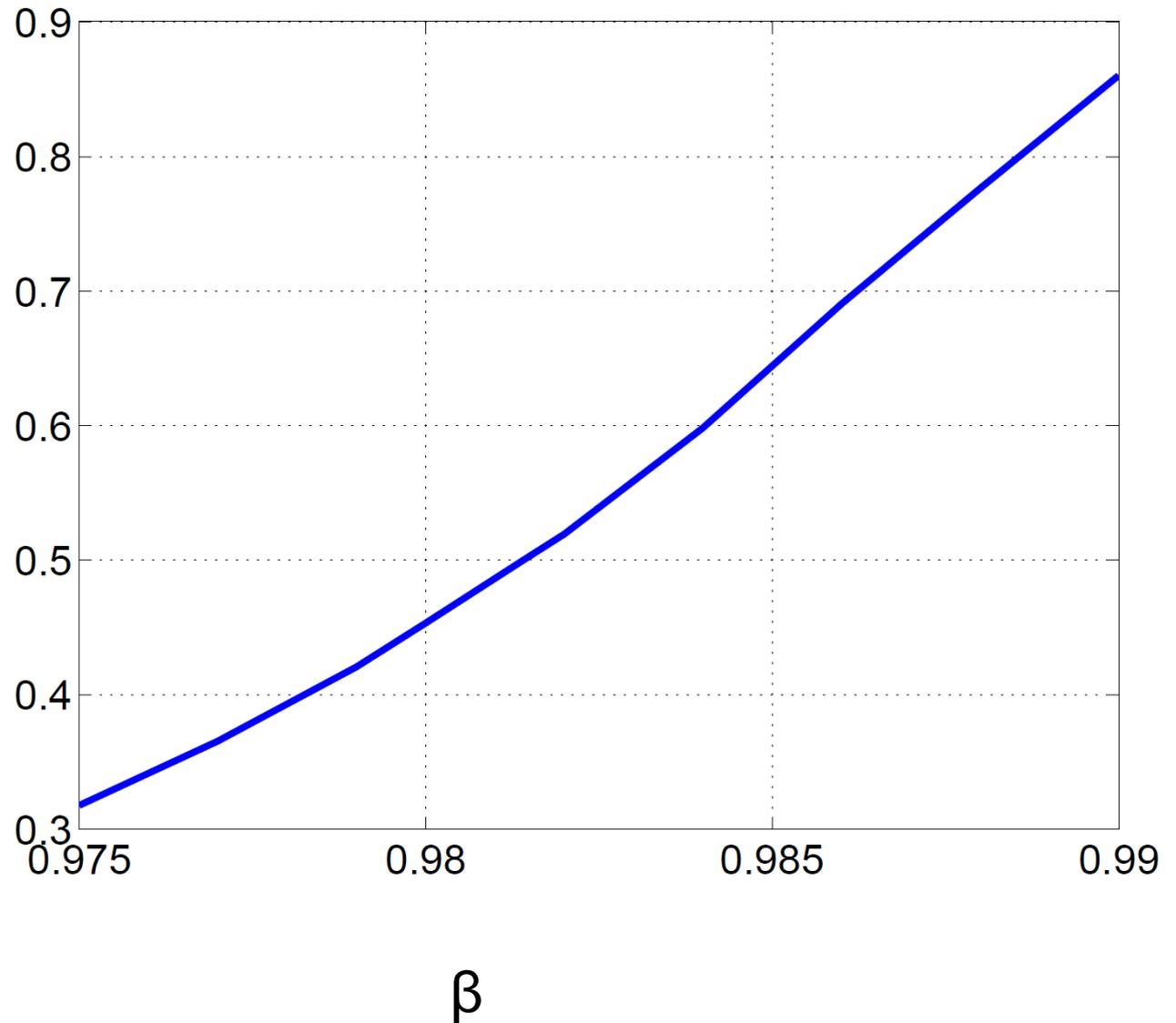
## Earnings profile (in \$10,000 dollars)



Solid line – model  
Dashed line – data

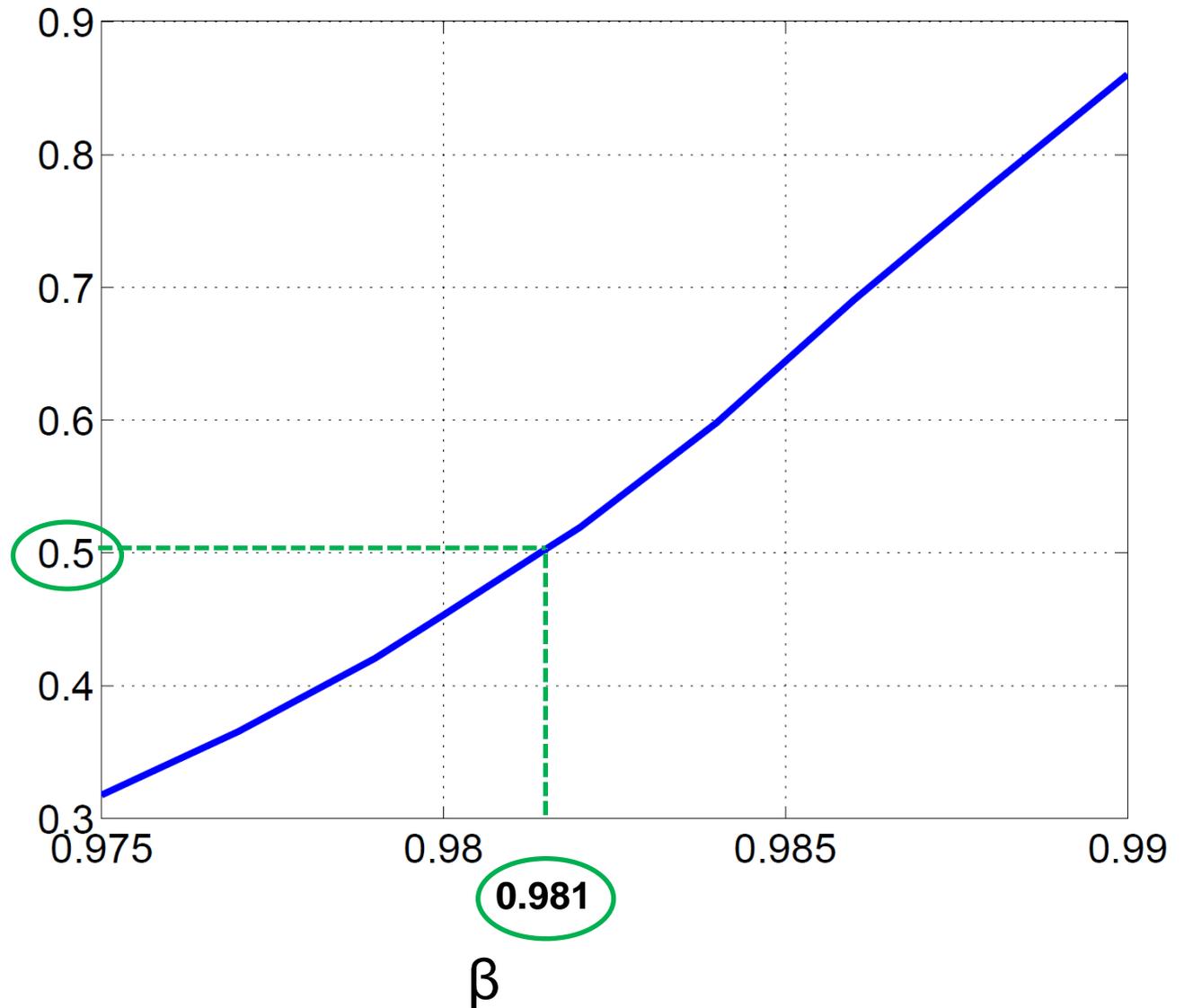
## Subjective discount factor

Fraction of wealth held  
by 95% of population



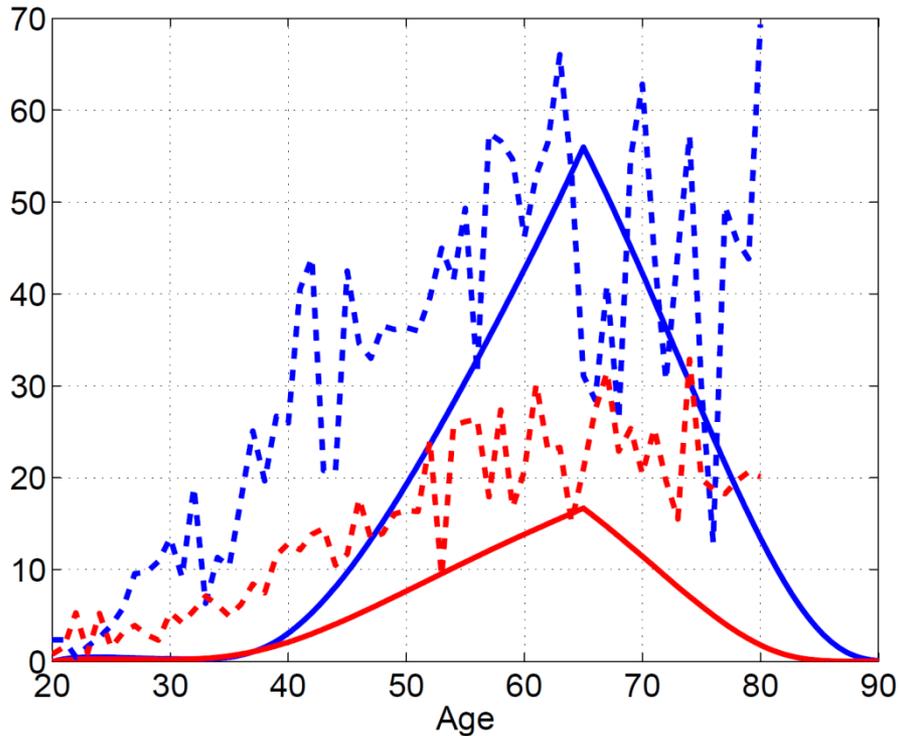
# Subjective discount factor

Fraction of wealth held  
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**Asset profile**  
(in \$10,000 dollars)

Solid line – model  
Dashed line – data



Predictions versus data:

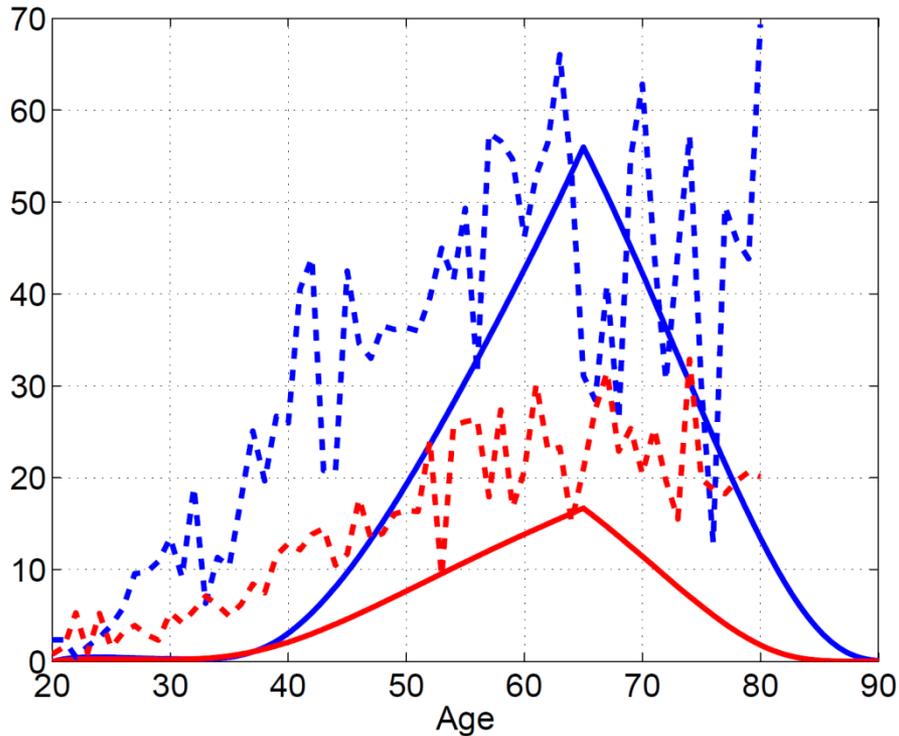
SCF (Survey of Consumer Finance) in 2004,  
excluding the 5% wealthiest

Gourinchas and Parker (2002):

“Young consumers behave as buffer-stock agents  
Around age 40, the typical household starts  
accumulating liquid assets for retirement...”

## Asset profile (in \$10,000 dollars)

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Dashed line – data



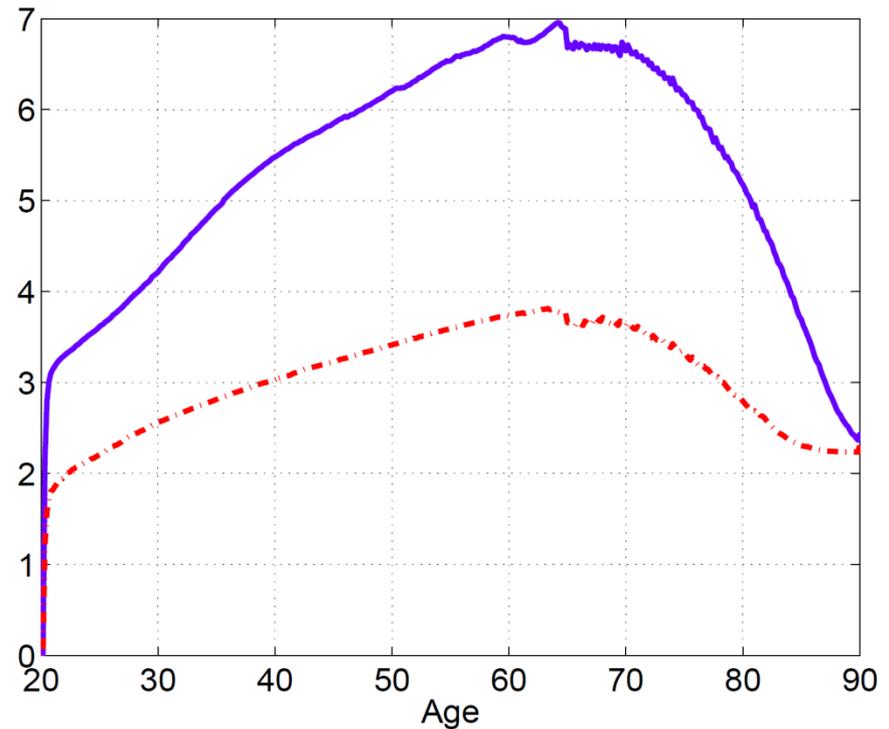
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Gourinchas and Parker (2002):

“Young consumers behave as buffer-stock agents  
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## Consumption profile (in \$10,000 dollars)



Key parameters:  $\beta = 0.981$

and survival probabilities  $\{m_t\}$   
[source: Social Security Adm.]

Gourinchas and Parker (2002):

“...the profiles are very sensitive to small  
variations in the discount factor”

# Job tenures of inexperienced and experienced workers

## Observations

Hall (AER, 1982):

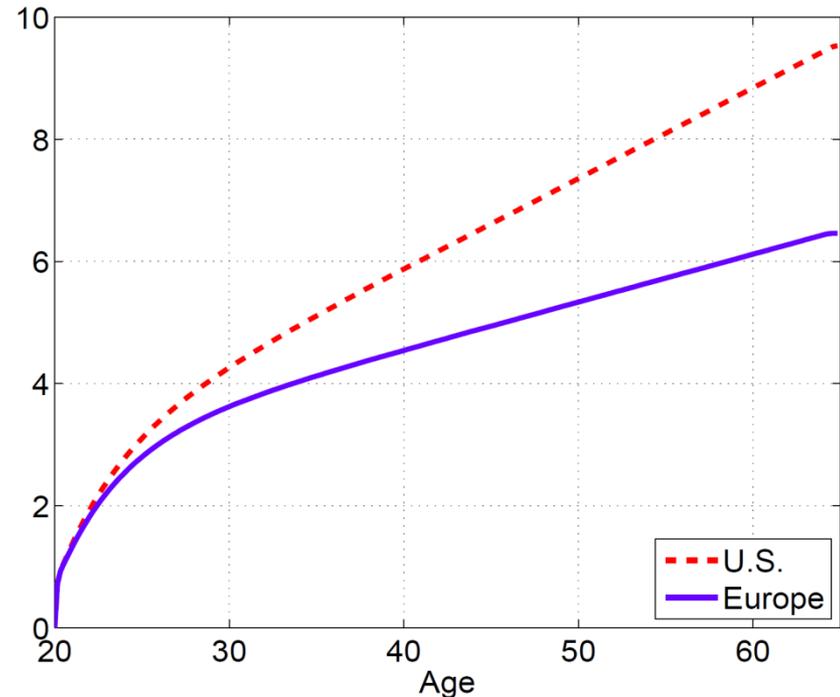
“by age 24, the average worker has held four jobs out of the ten he or she will hold in an entire career.”

Davis and Haltiwanger (NBER Macro, 1990):

“March-to-March establishment-level employment changes, we calculate that manufacturing’s rates of ... destruction averaged 11.3% per year ... quarter-to-quarter rates are larger yet ... 5.62% on a quarterly basis.”

## Calibration outcomes

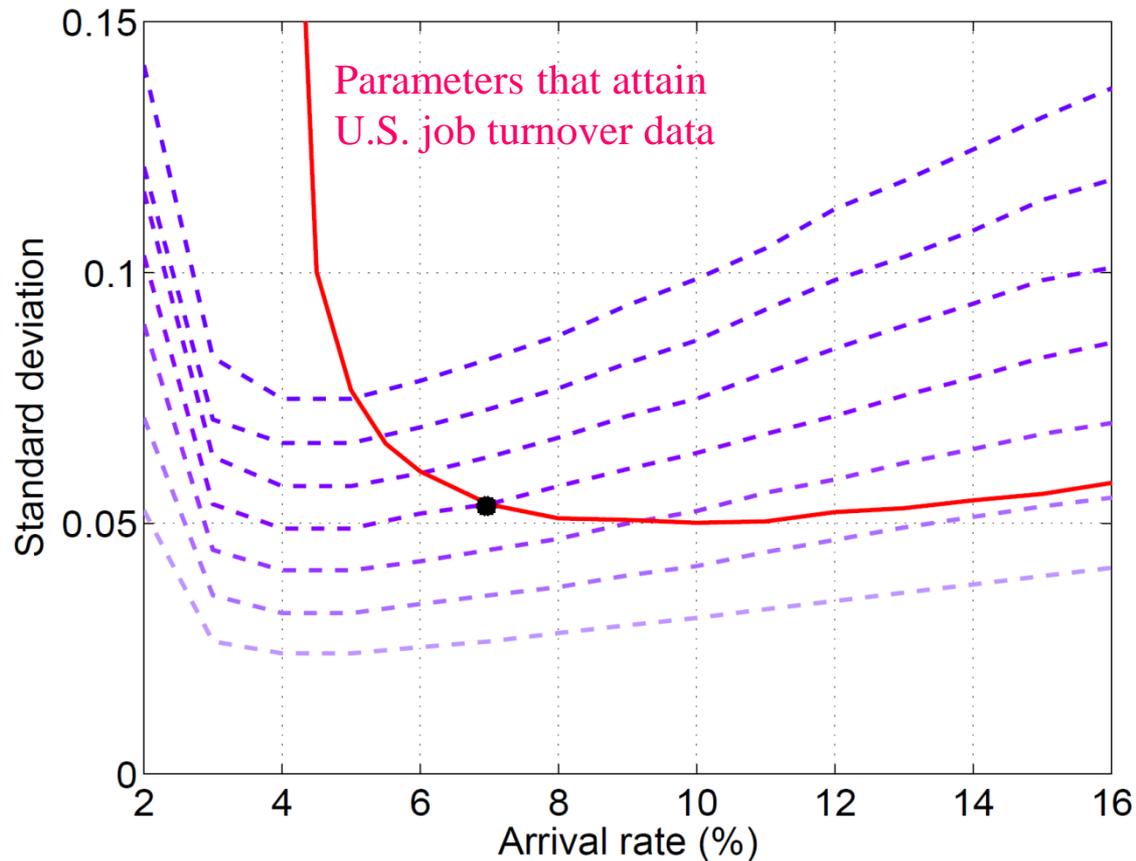
Average number of jobs held



... annual job destruction rate for experienced worker in the U.S. model economy is 14.4%

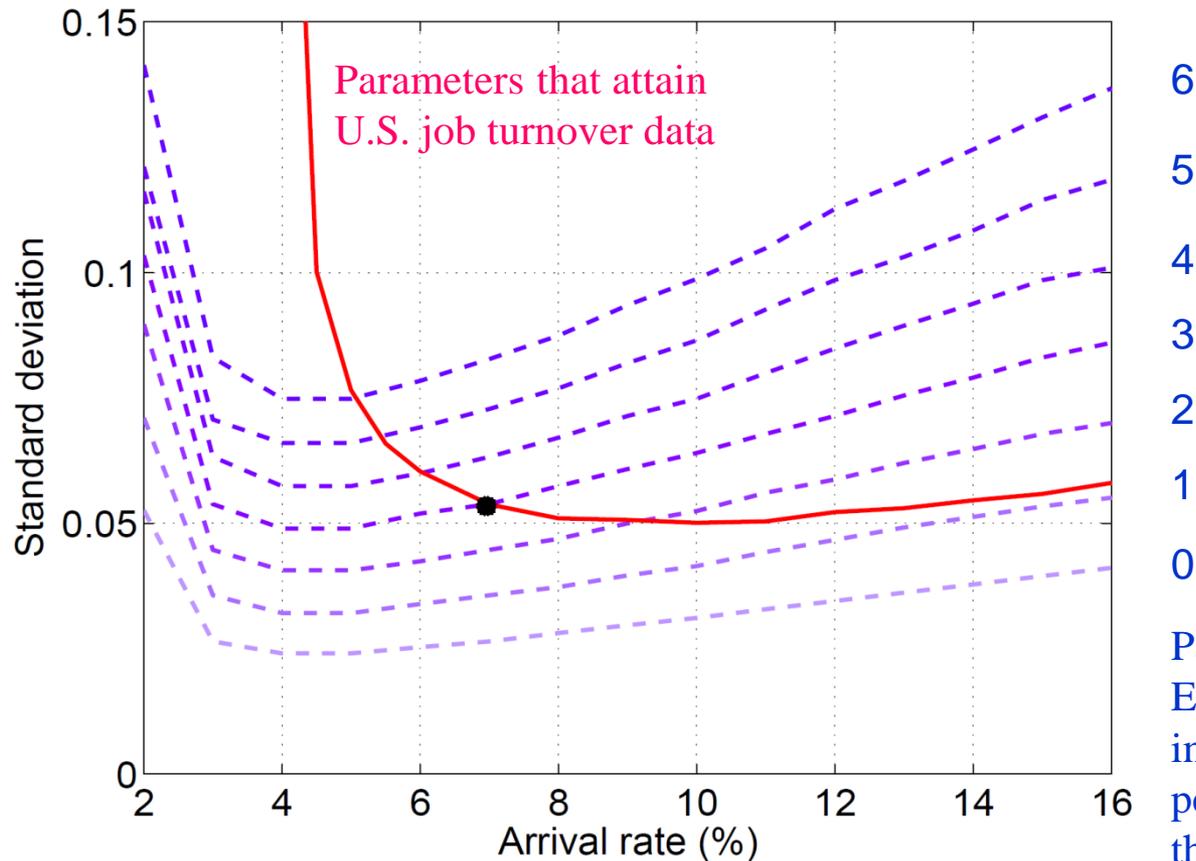
## Productivity process of firms

The productivity will remain the same at  $z$  with probability  $1-p_z$ . With probability  $p_z$ , the new productivity is a random draw from a normal distribution having mean 0.5 and standard deviation  $\sigma_z$  that has been truncated to the unit interval  $[0, 1]$ .



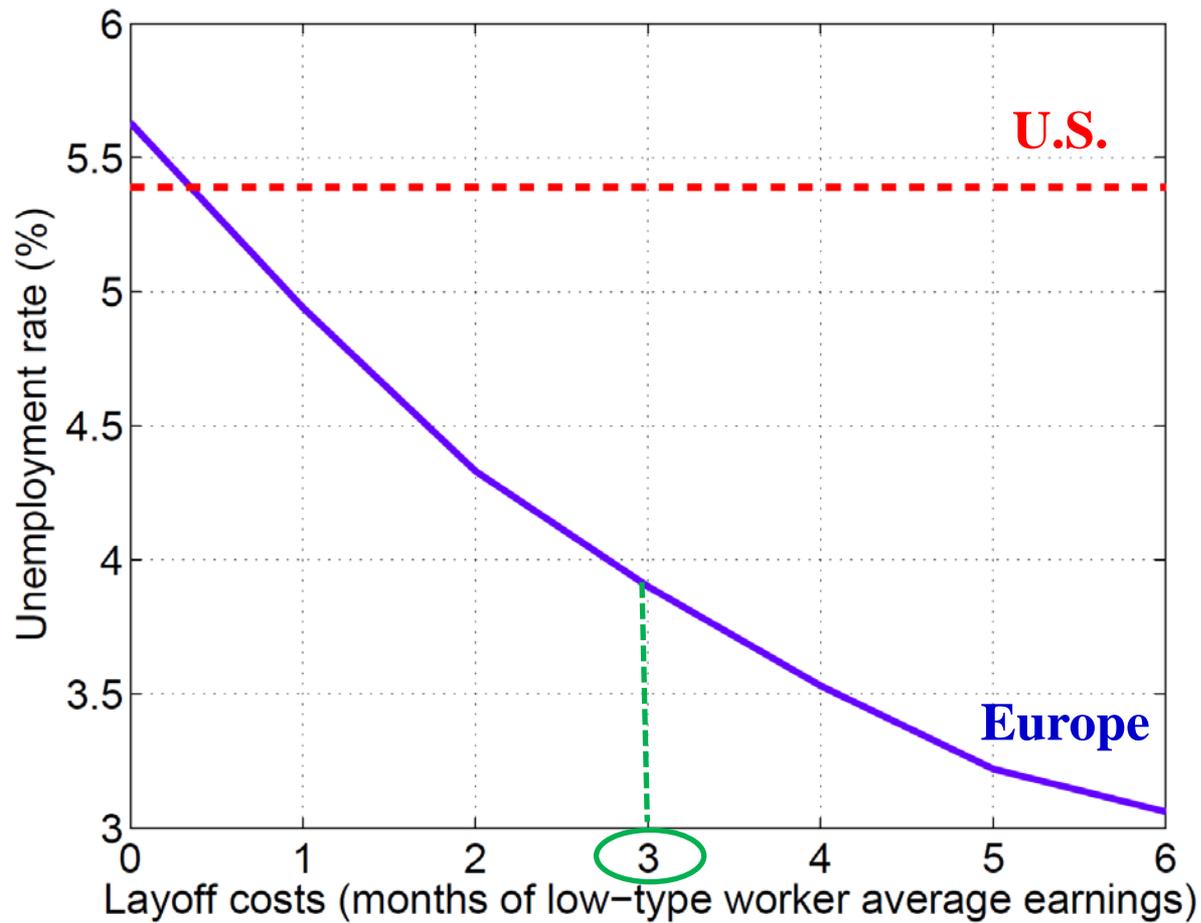
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6  
5  
4  
3  
2  
1  
0

## Tranquil times: Layoff tax suppresses European unemployment



Tranquil times

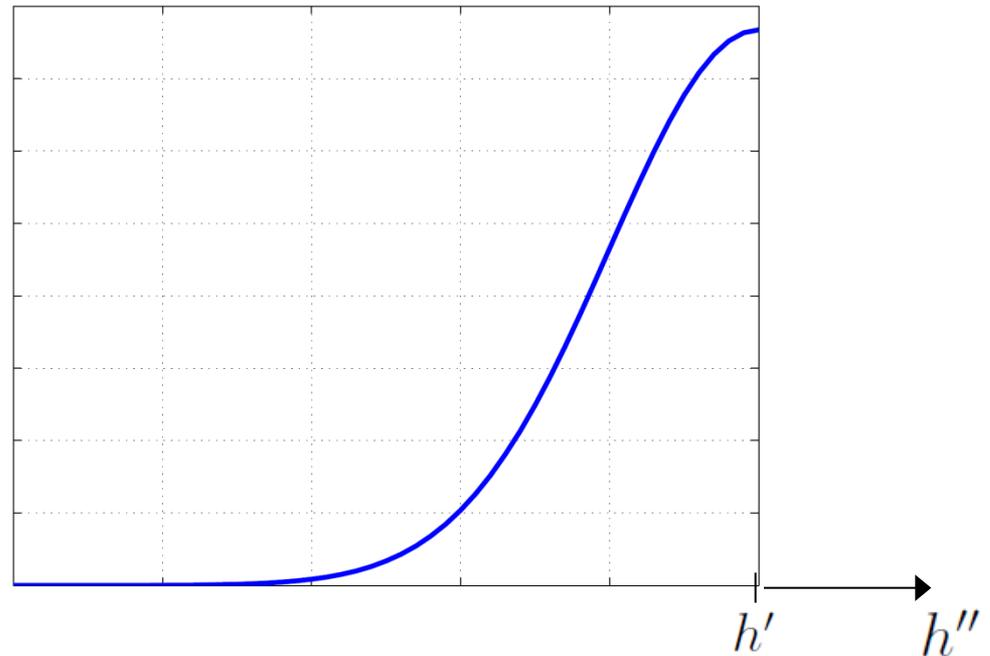
Turbulent times

Skill loss upon exogenous  
job destruction:

none

governed by transition  
probability  $H_i^\lambda(h', h'')$

A worker with skill level  $h'$   
whose job is exogenously  
terminated, her new skill  
level  $h''$  is distributed as



Tranquil times

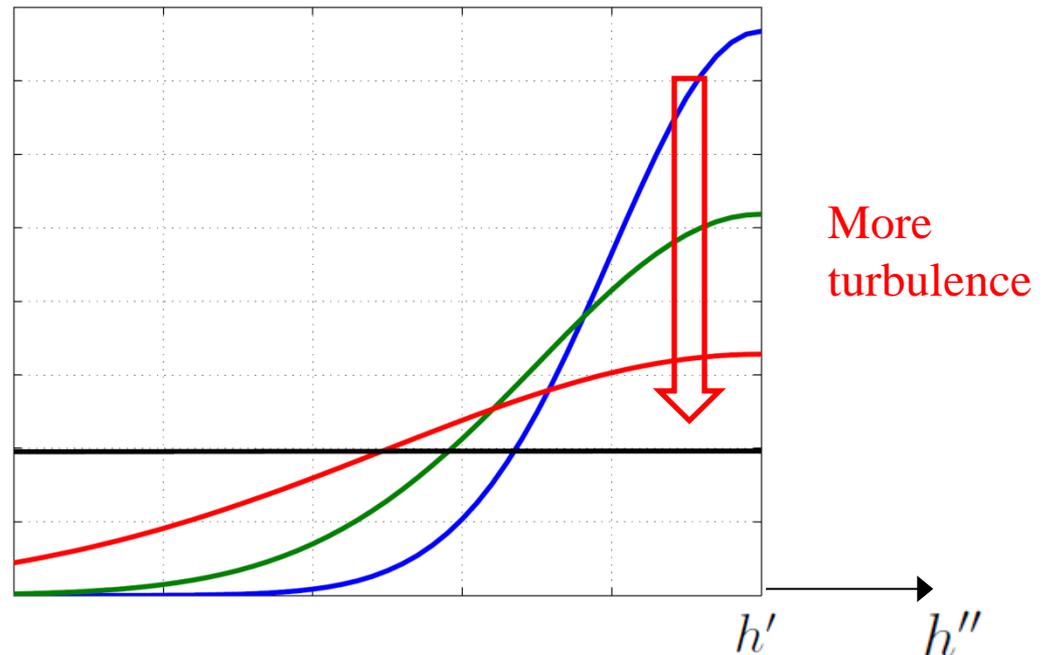
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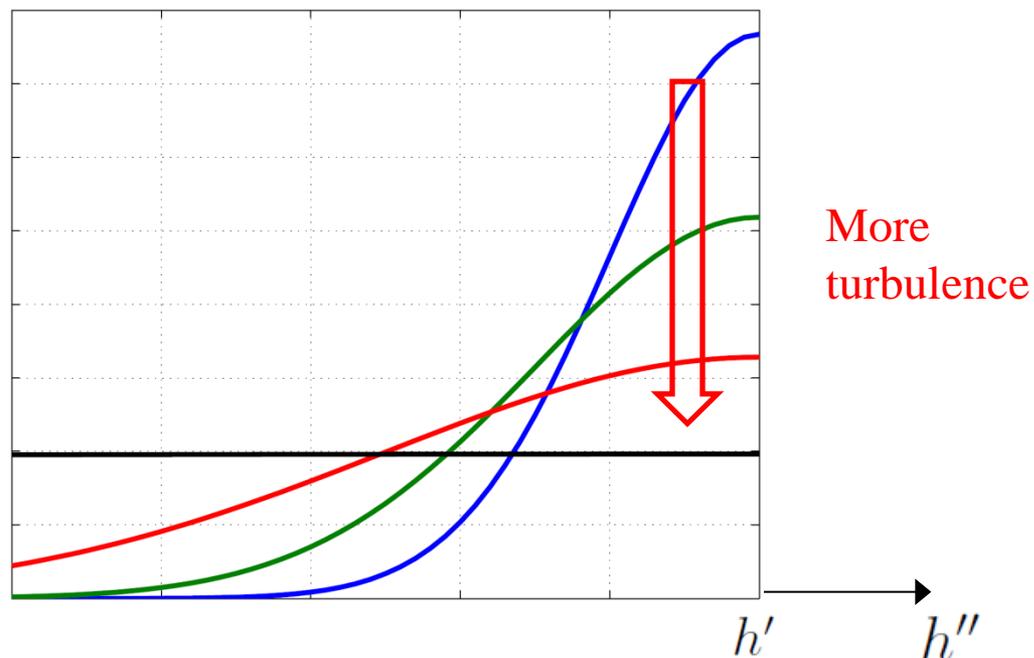
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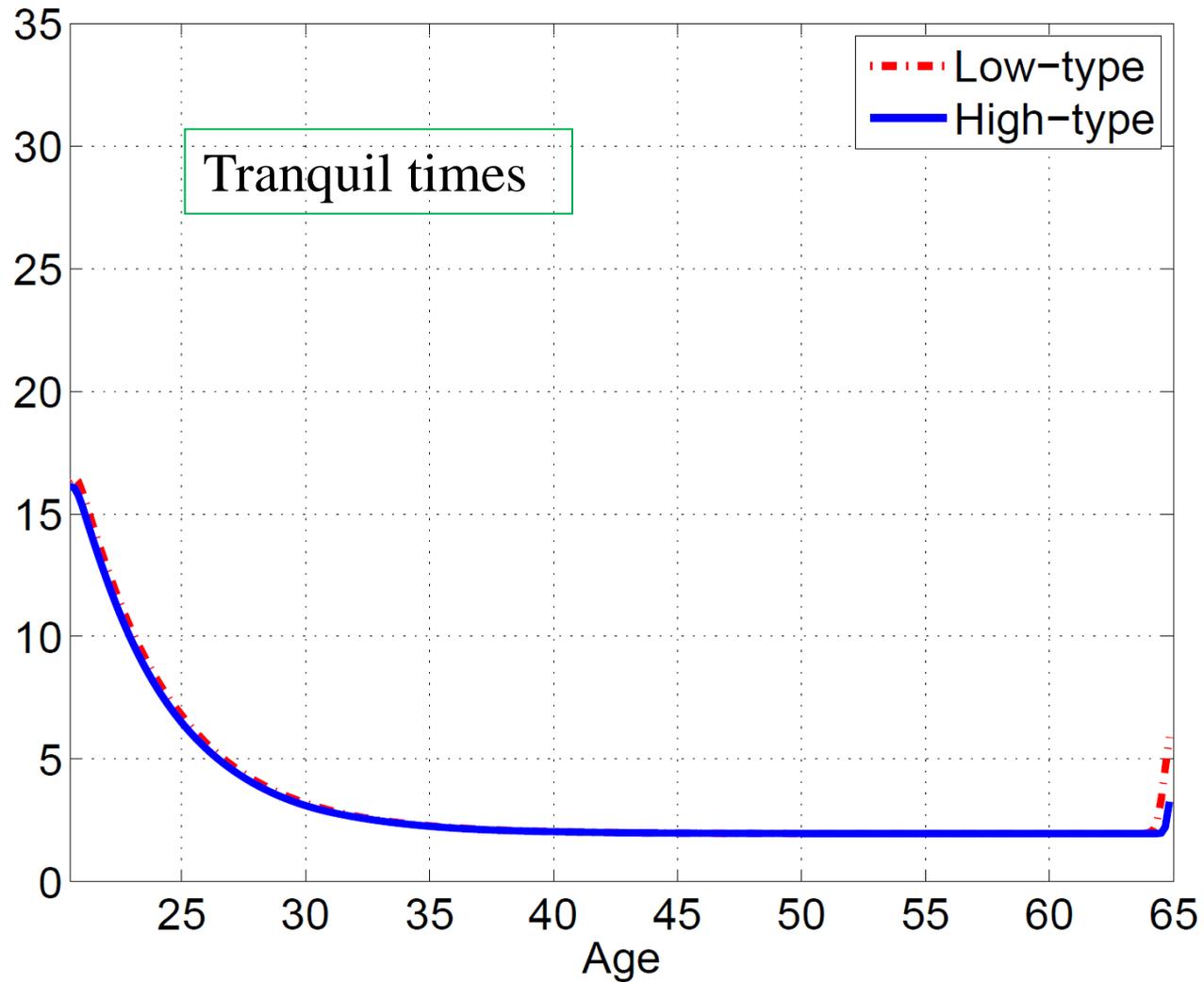


	Tranquil times	Turbulent times
Skill loss upon exogenous job destruction:	none	governed by transition probability $H_i^\lambda(h', h'')$
Europe-specific labor market institutions:	layoff tax and unlimited duration of benefits	same as before and a minimum wage

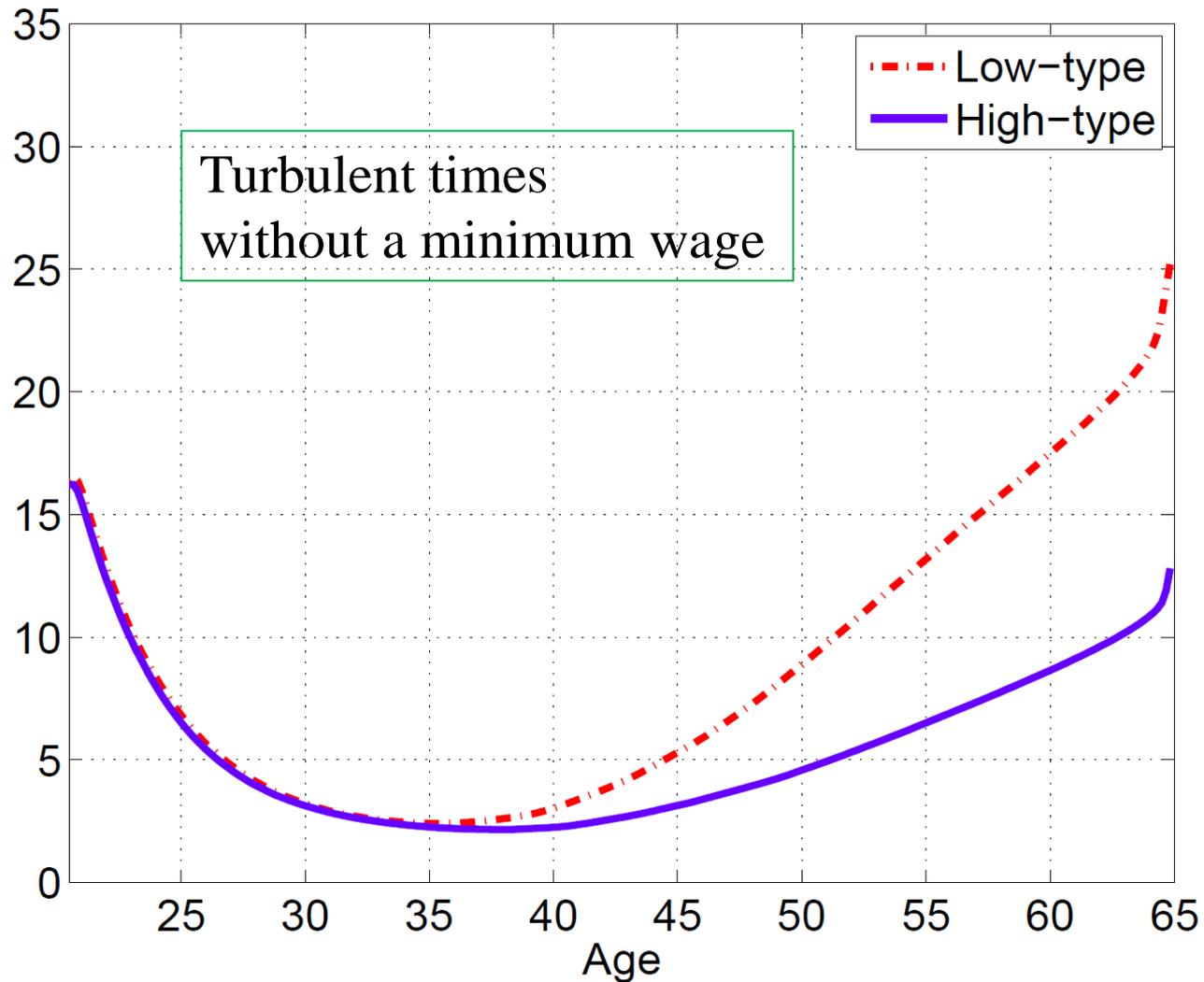
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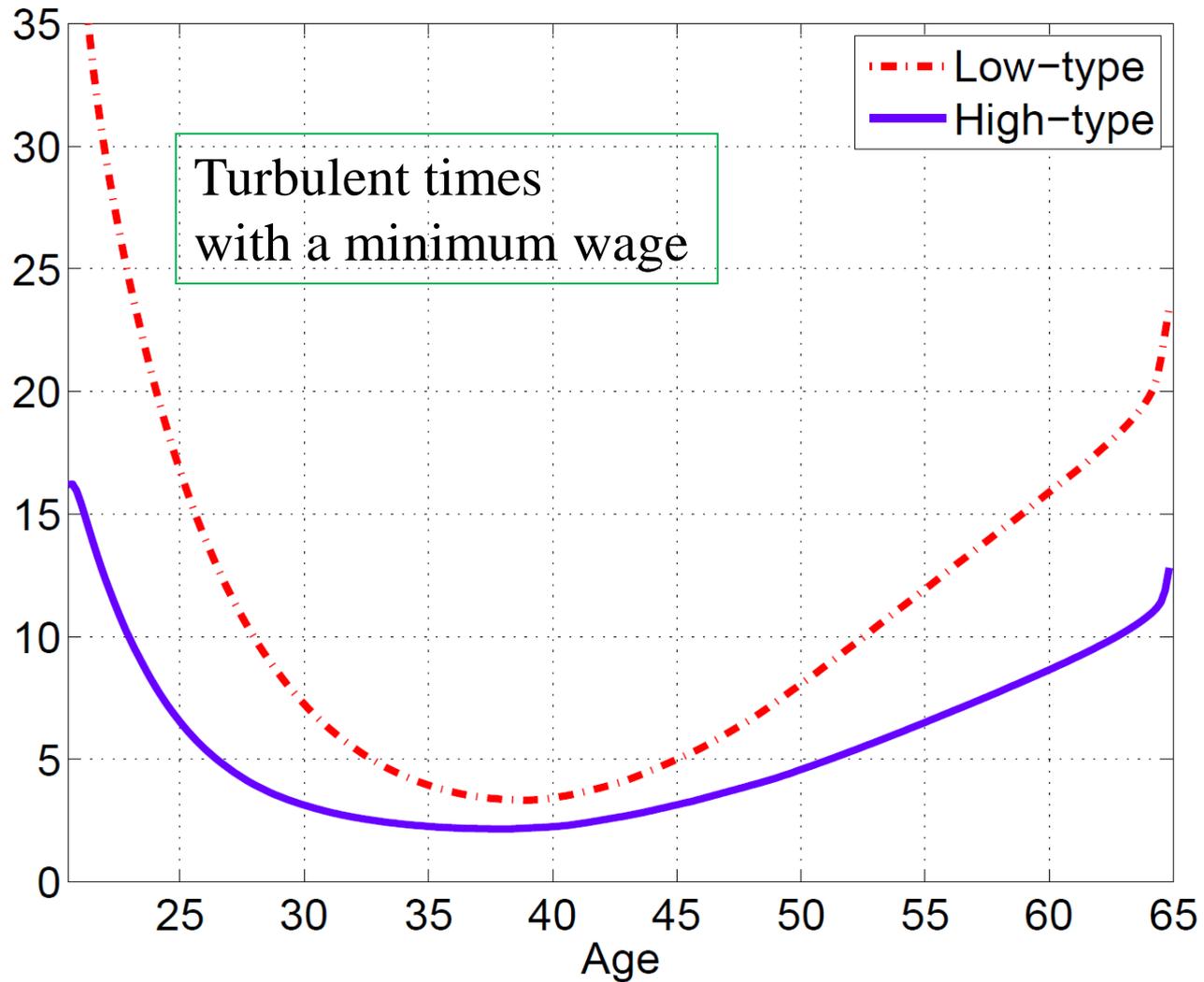
## European unemployment by type: turbulence and minimum wage



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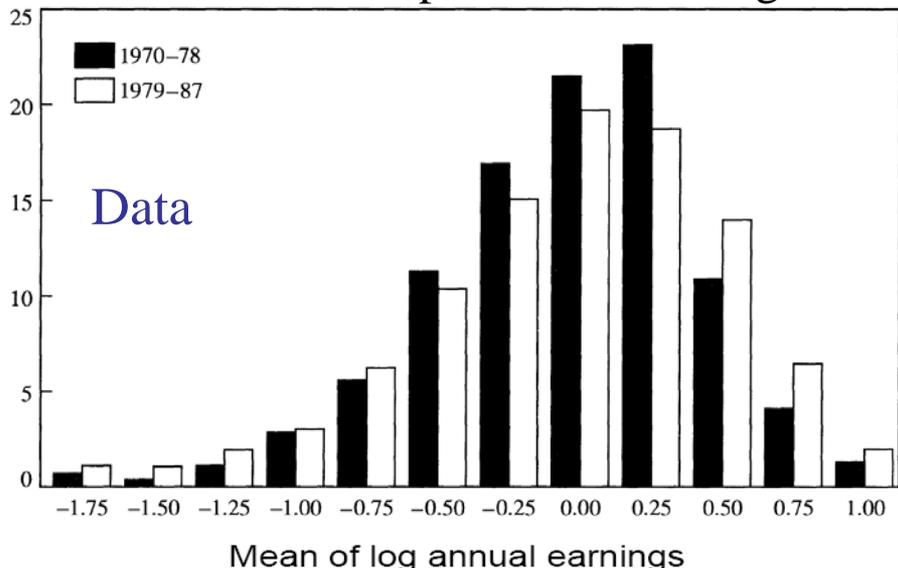


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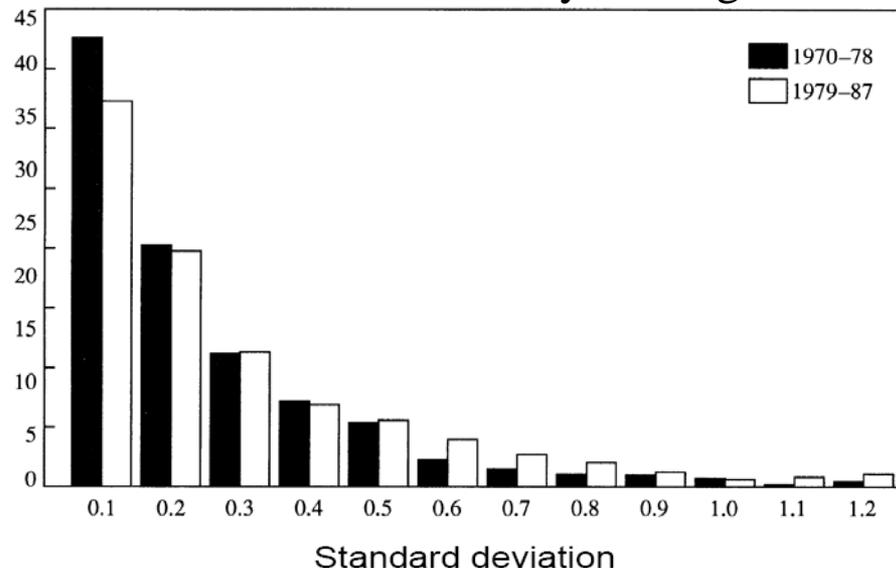


# Turbulent times: U.S. earnings volatility and European unemployment 10%

## Distribution of permanent earnings

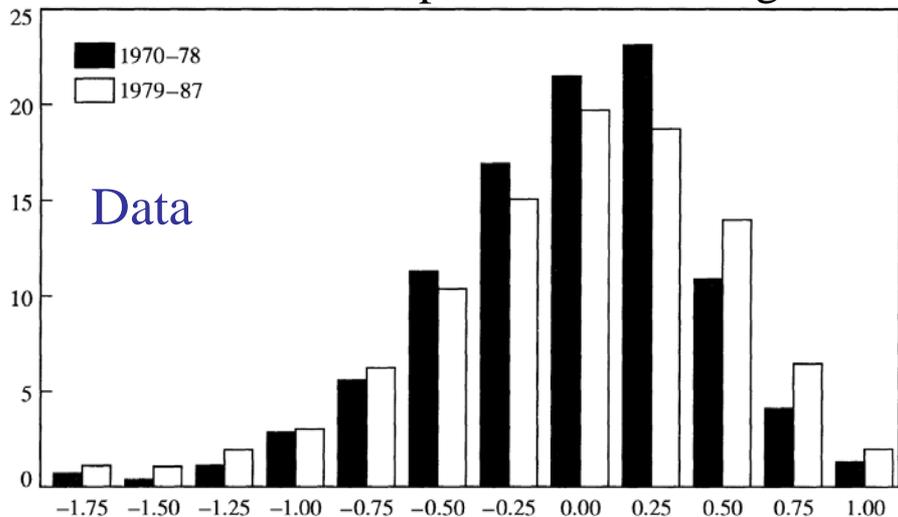


## Distribution of transitory earnings

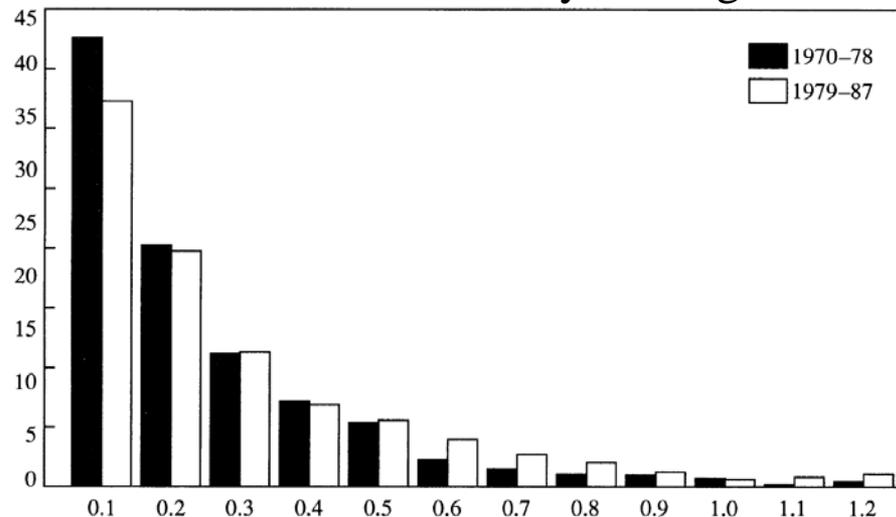


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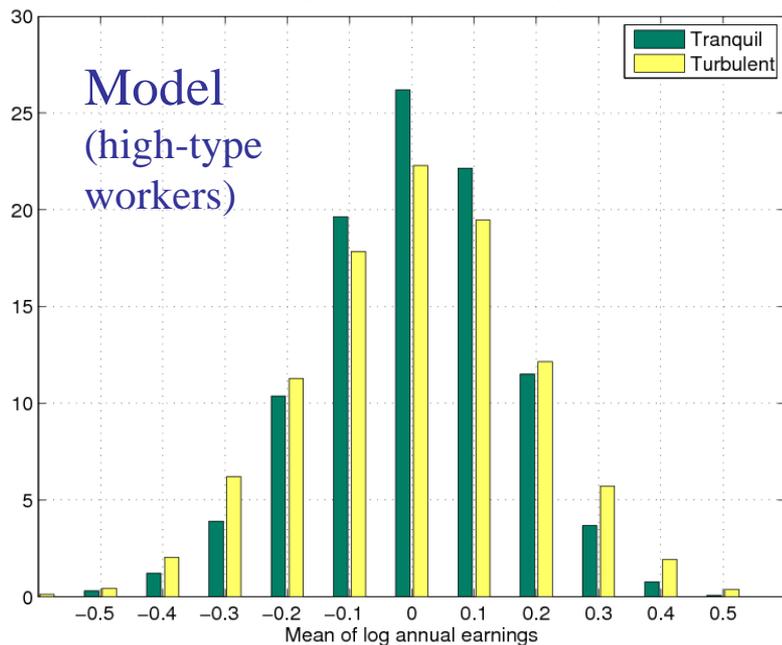
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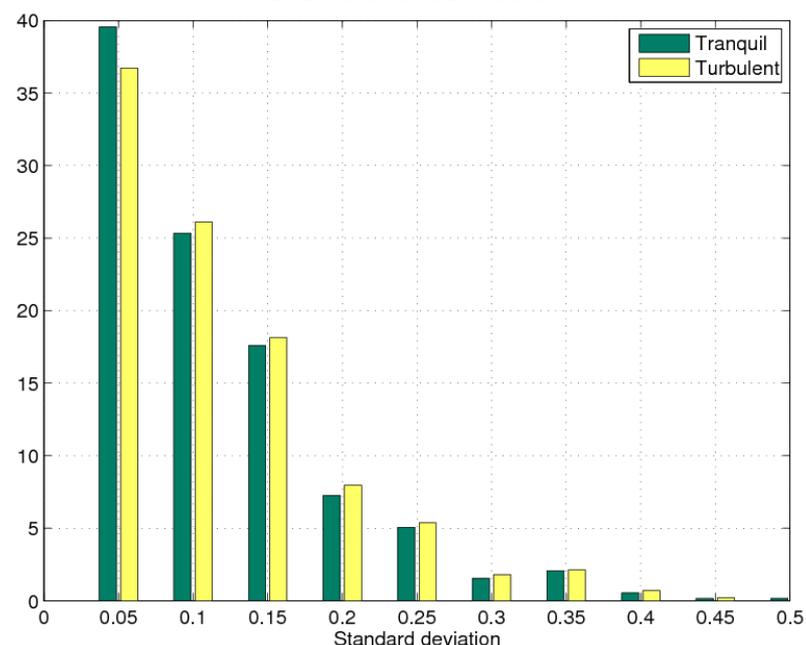
## Distribution of transitory earnings



## Mean of log annual earnings

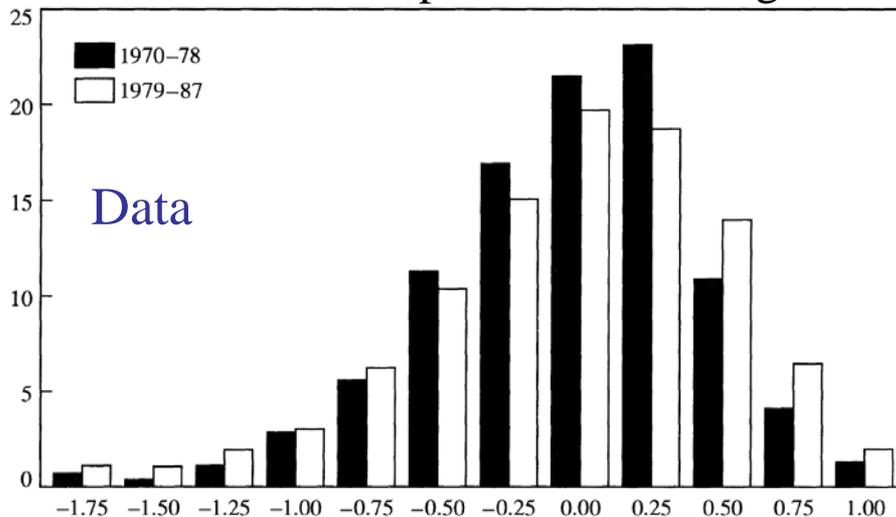


## Standard deviation

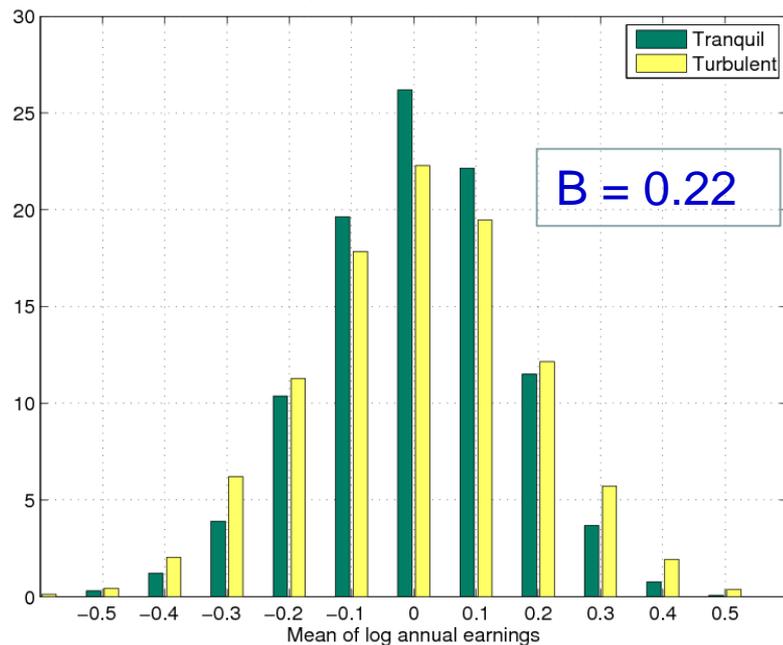


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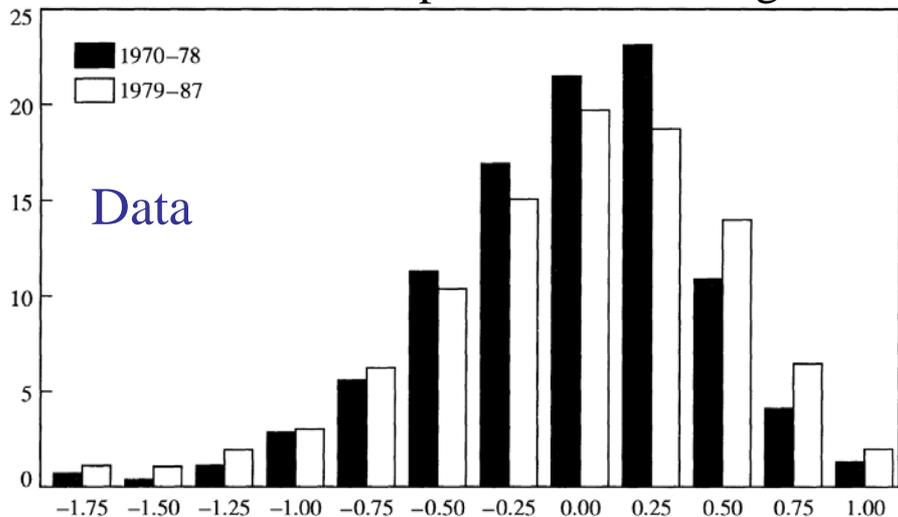


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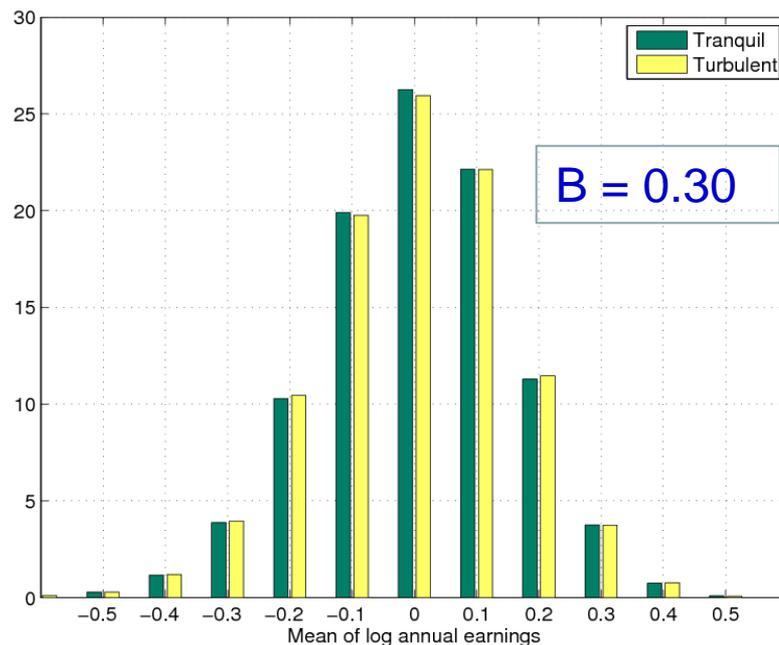
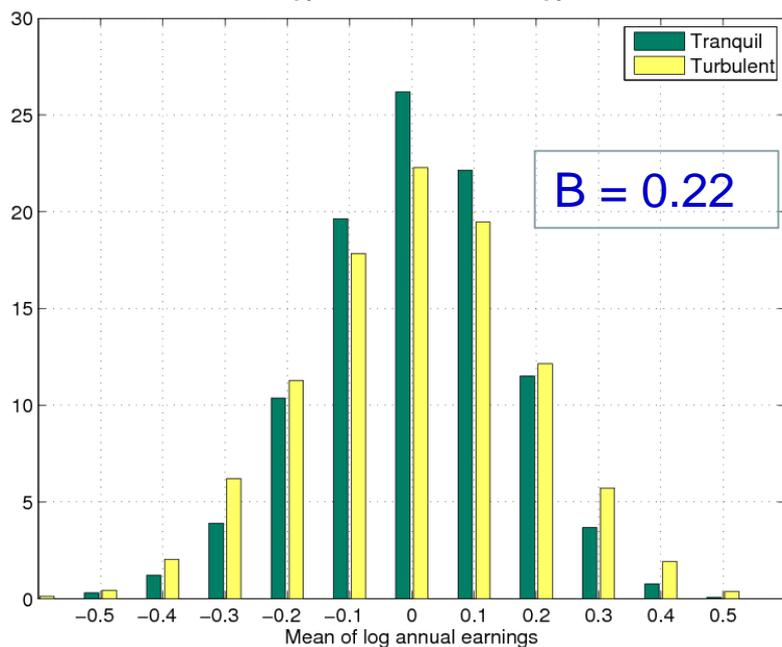


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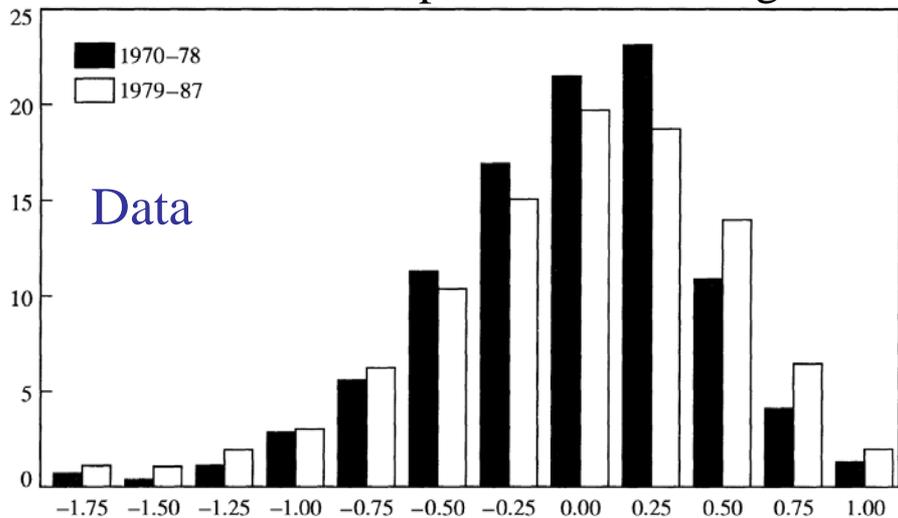


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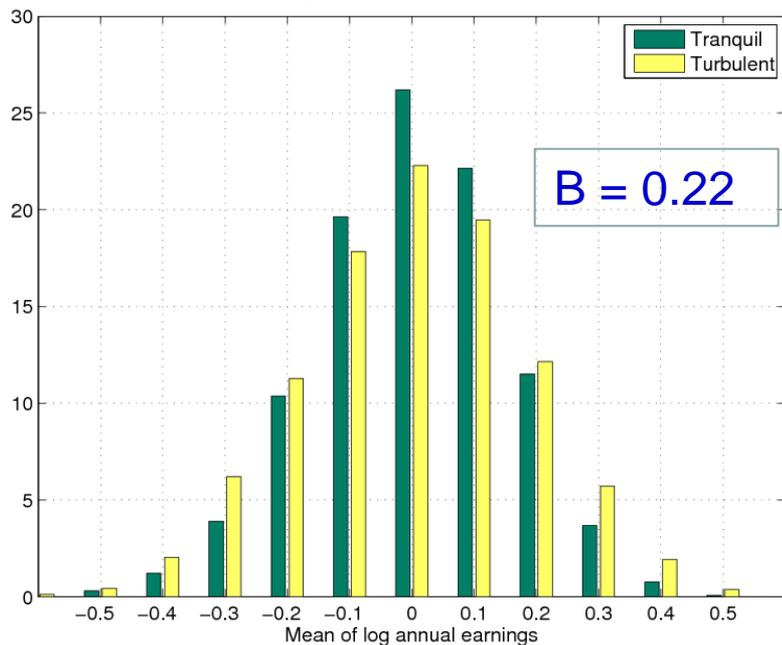
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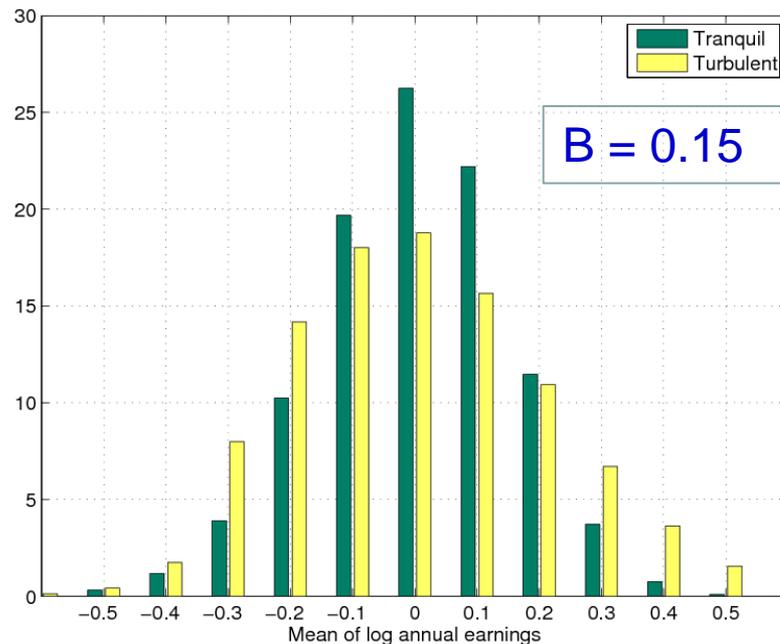


Data

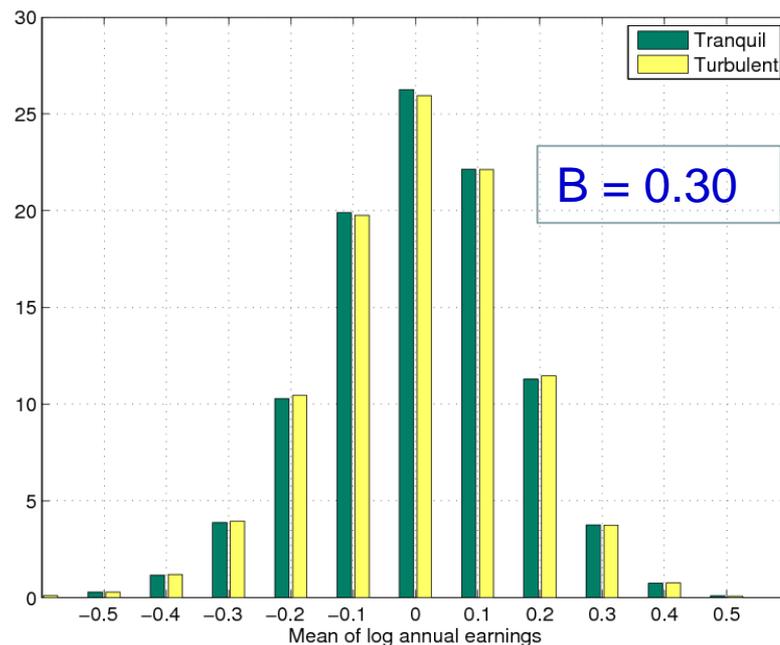
## Mean of log annual earnings



$B = 0.22$

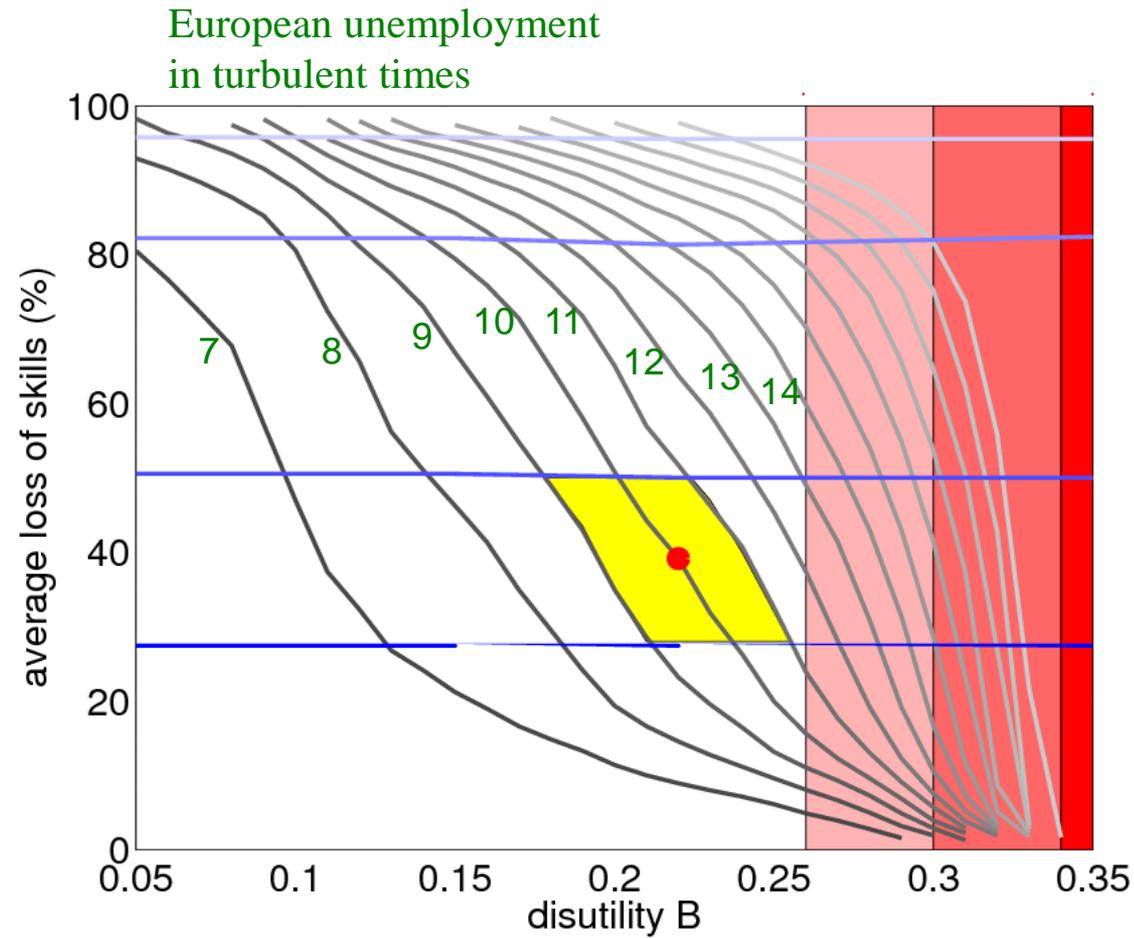


$B = 0.15$

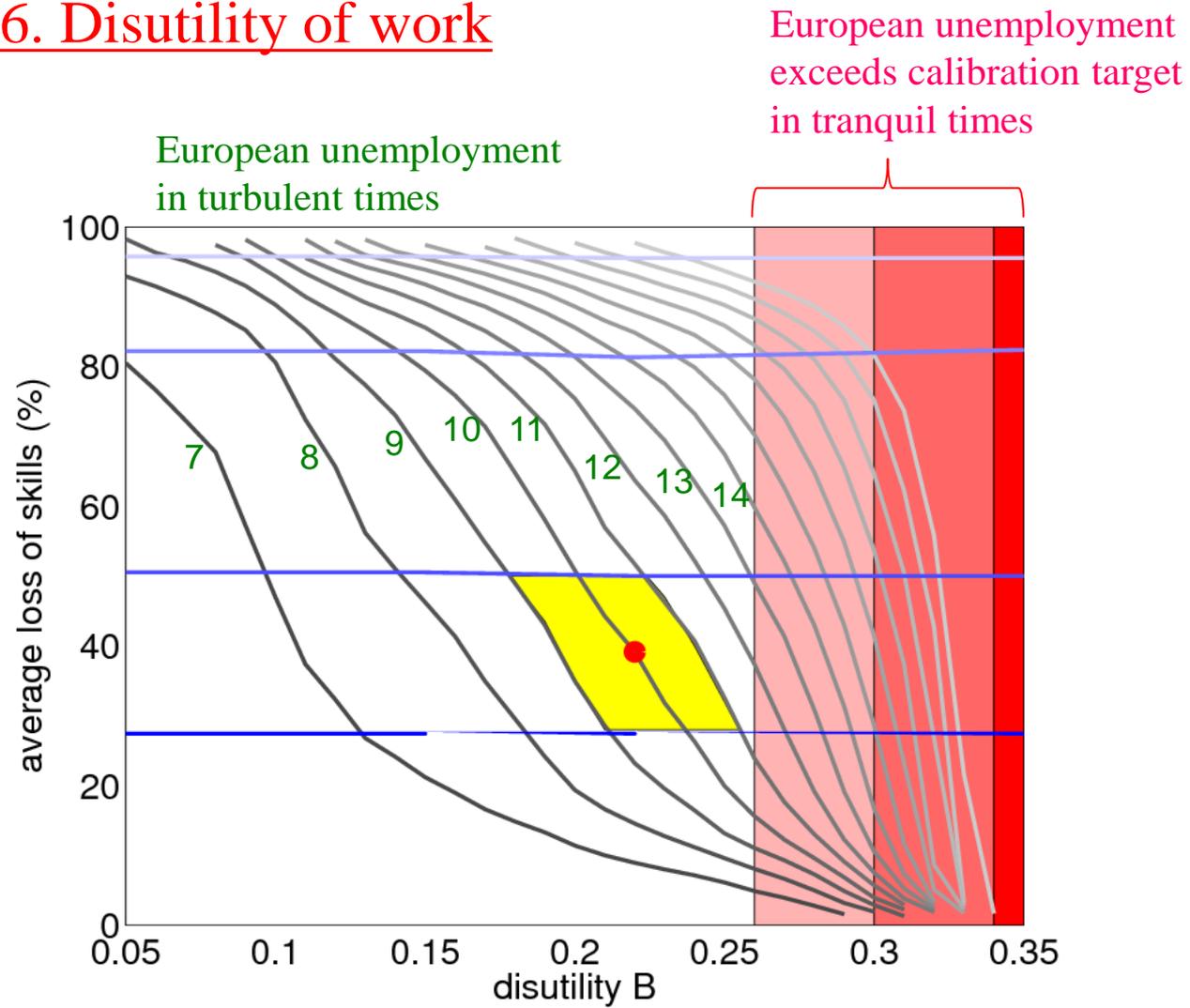


$B = 0.30$

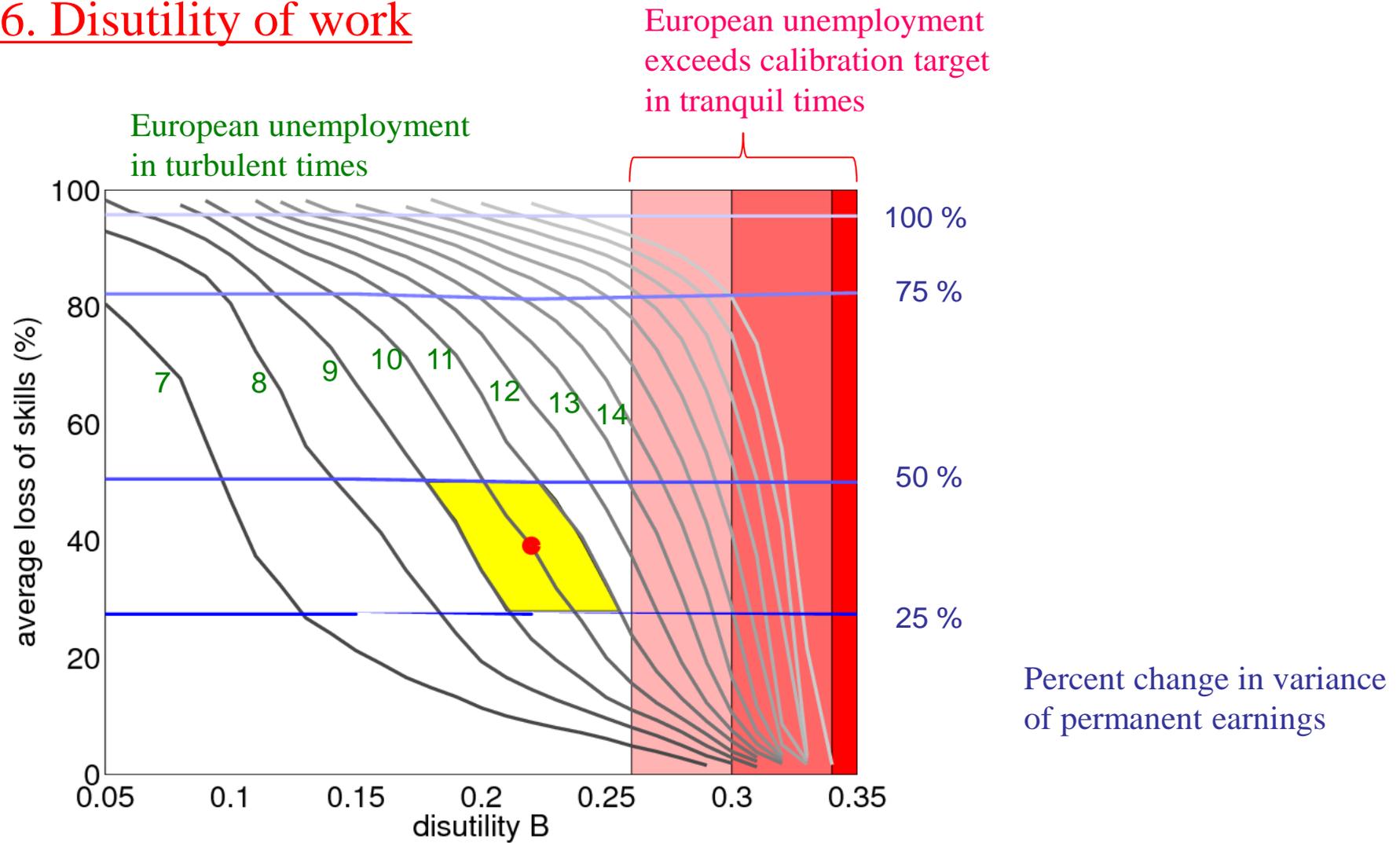
## 6. Disutility of work



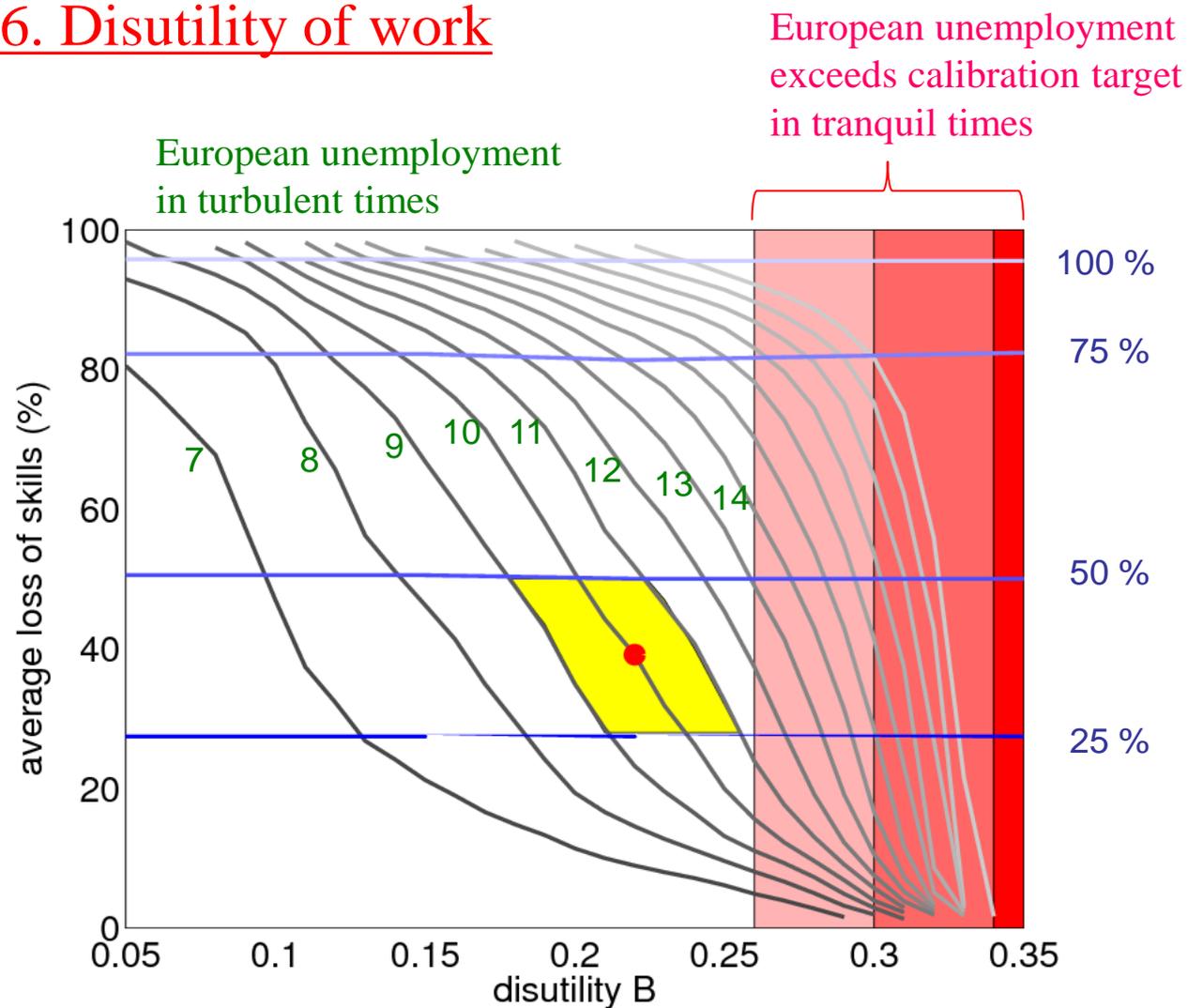
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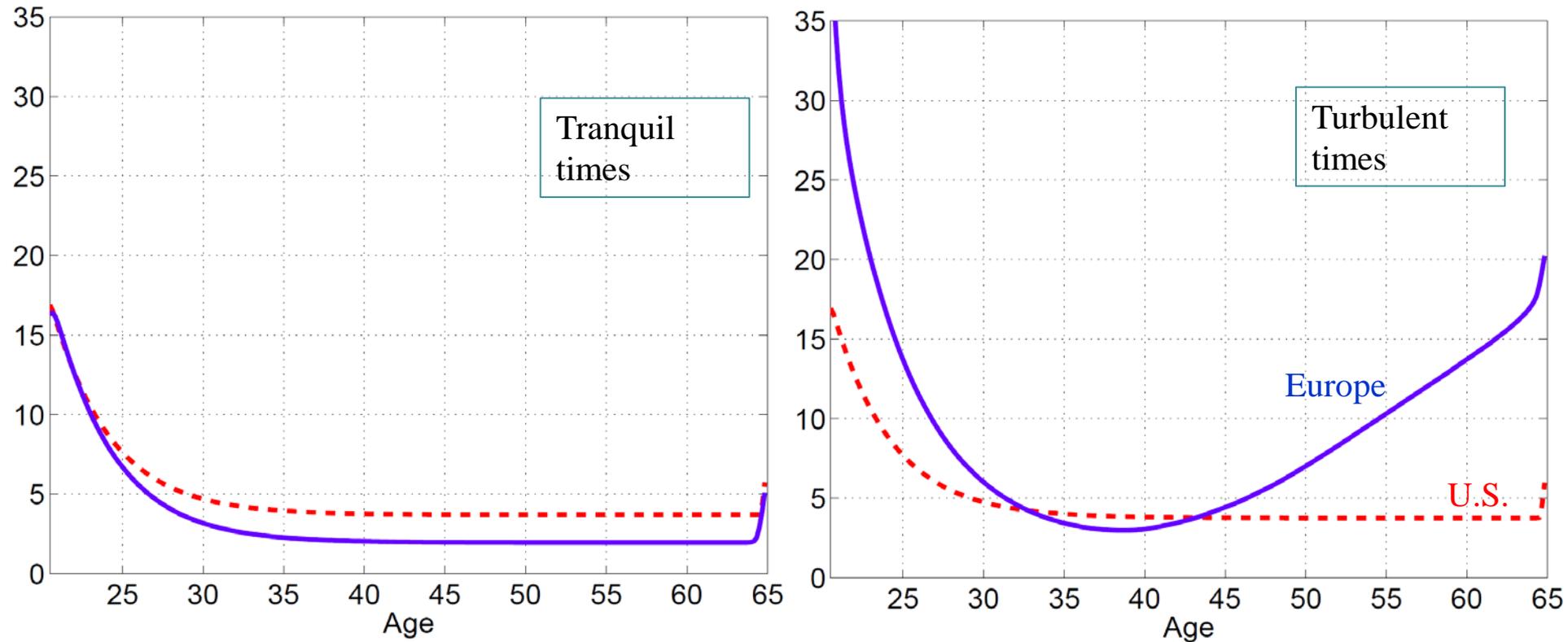


# 6. Disutility of work



Gottschalk and Moffitt (1994):	All workers	41%
	Years of education fewer than 12	55%
	12 or more	34%

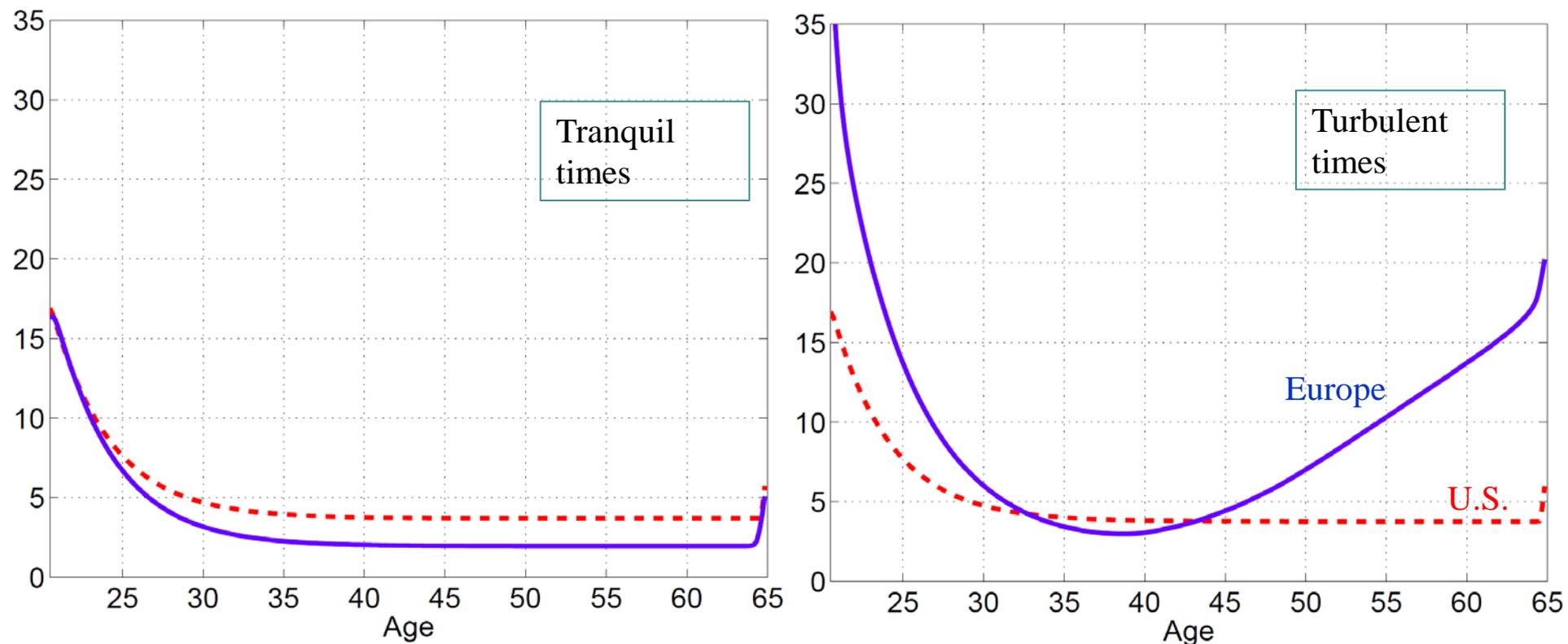
# Unemployment in Europe and in the U.S.



Unemployment (percent)

	Europe		U.S.	
	Tranquil	Turbulent	Tranquil	Turbulent
Low type	3.93	11.73	5.41	5.47
High type	3.83	5.91	5.39	5.40
All	3.90	9.99	5.39	5.45

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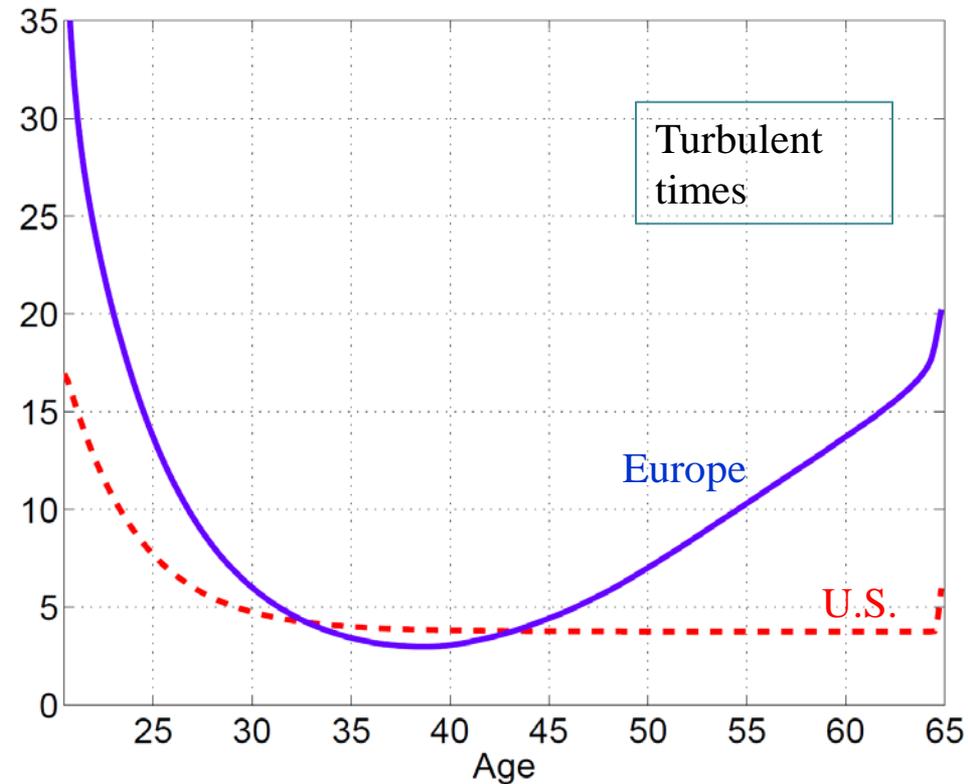
Flow rates into and out of unemployment (in bi-monthly model frequency)

	Europe		U.S.	
	Tranquil	Turbulent	Tranquil	Turbulent
Inflow rate	2.16	2.22	3.41	3.45
Outflow rate	62.85	23.24	66.60	66.55

# Unemployment in Europe and in the U.S.

## Europeans by age groups

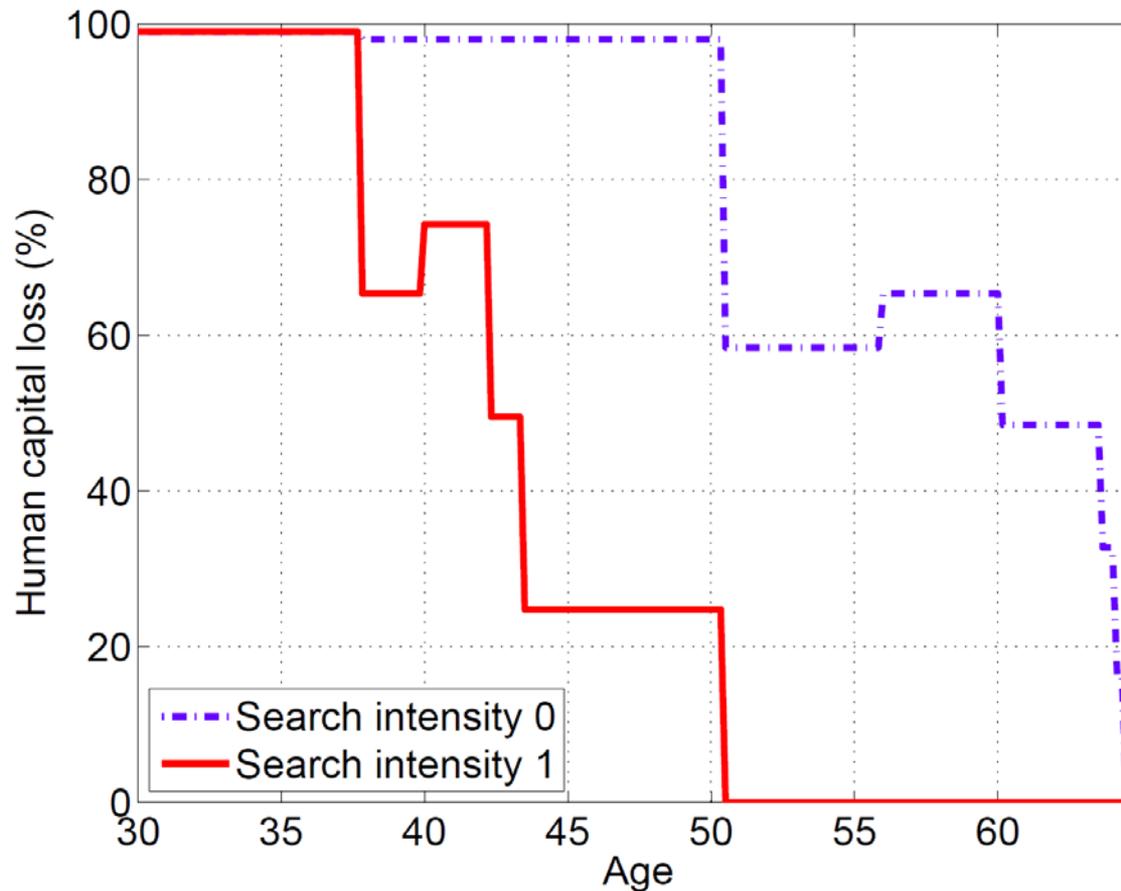
Age	Unempl. duration (months)		Long-term unempl. (percent of unempl.)	
	Tranquil	Turbulent	Tranquil	Turbulent
20-29	3.29	7.51	0.51	16.42
30-39	3.17	6.20	0.37	11.61
40-49	3.01	7.58	0.17	16.13
50-59	2.99	17.34	0.14	47.94
60-	3.35	26.36	0.29	63.77
All	3.21	12.93	0.40	31.40



## Unemployment (percent)

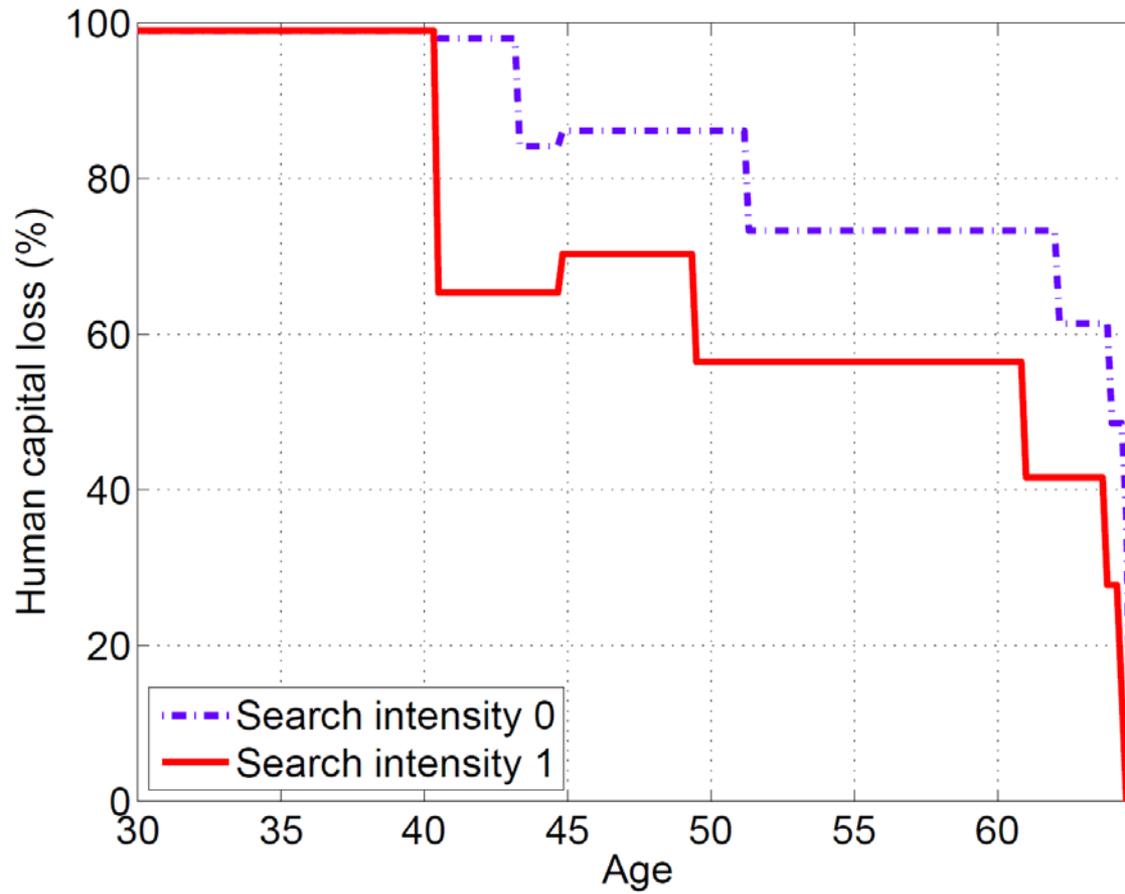
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## Search intensity of low-type workers in Europe in tranquil times

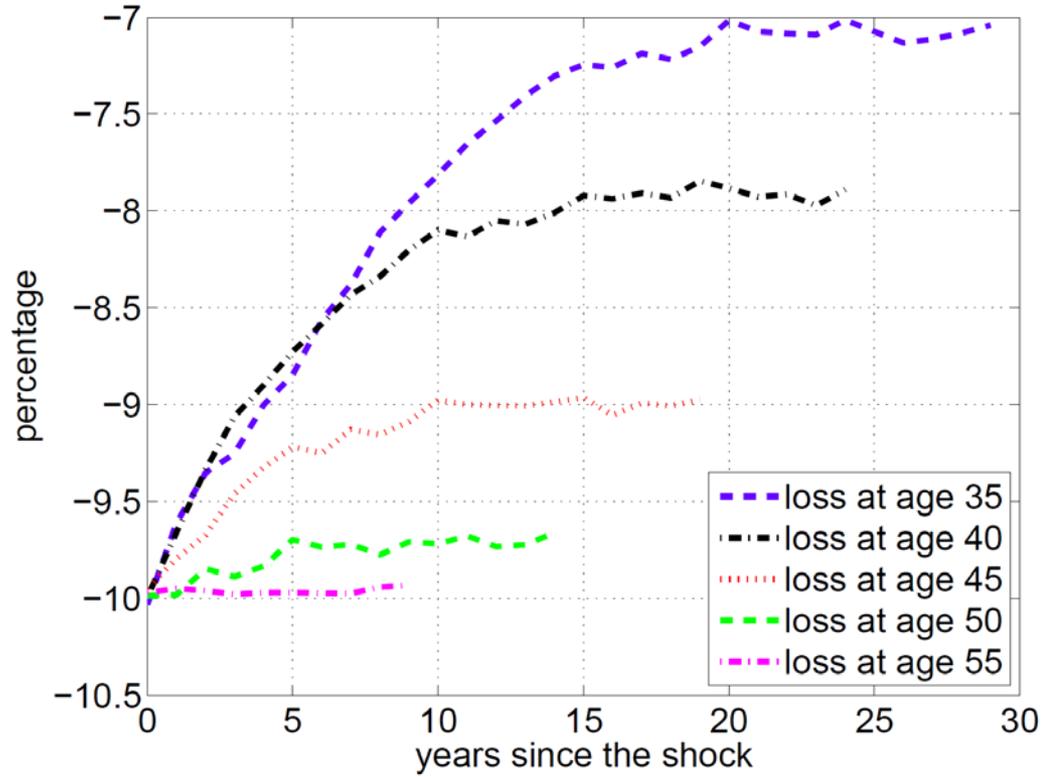


Optimal search intensity of the average low-type worker in Europe in tranquil times, as a function of age and ‘human capital loss’. The agent is assumed to hold the average wealth level and to be entitled to benefits based on average earnings in her age group. The search intensity is plotted for different levels of human capital below the average level in her age group, where the difference between these numbers is interpreted as her ‘human capital loss’. The solid (dashed) line is the contour curve for full (zero) search intensity.

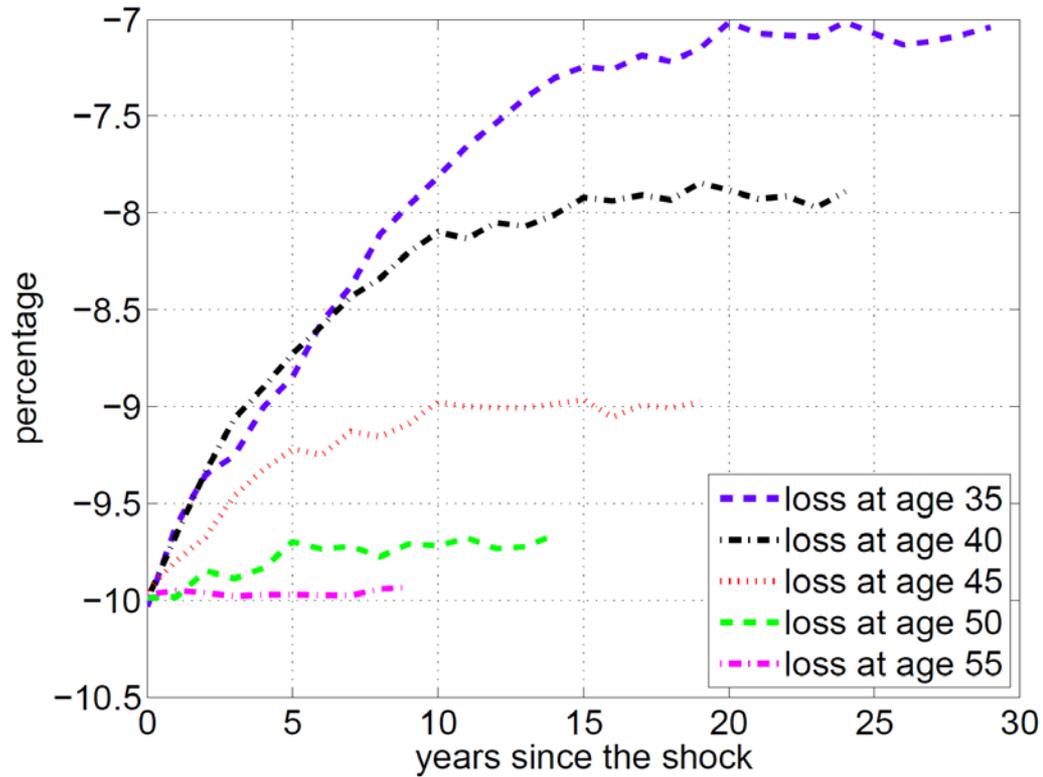
# Search intensity of high-type workers in Europe in tranquil times



High-type workers loss of earnings relative to the age-earnings profile, after an 'earnings shock' of 10%, in the U.S.



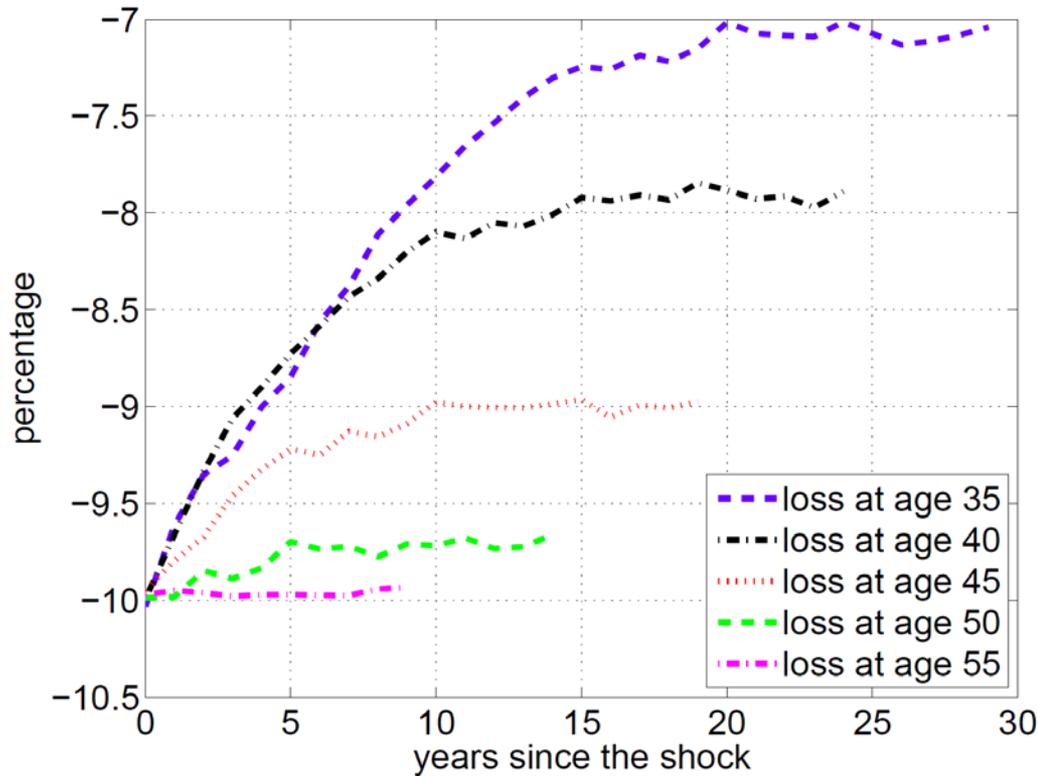
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Percentage increase in earnings autocovariances between tranquil and turbulent times

Lag order	Age group		
	25-34	35-44	45-54
1-4	5.4	25.3	54.1
5-9	2.6	15.0	39.4
10-15	3.0	5.3	23.4

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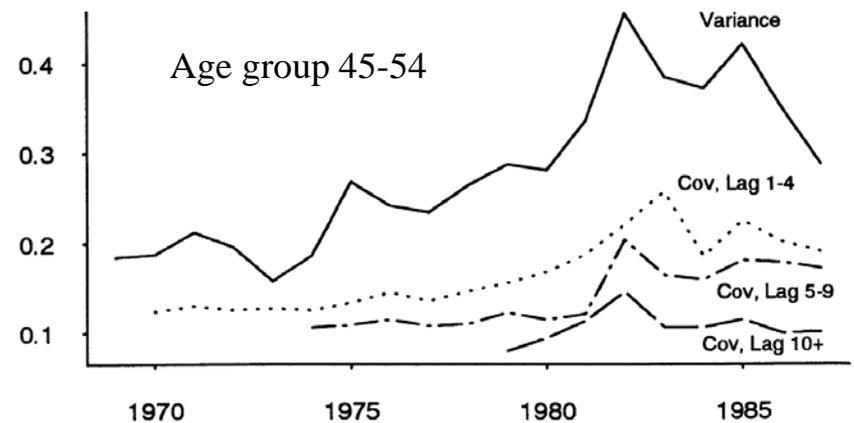


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Moffitt & Gottschalk (1995):

Over the 1970s and 1980s, “an increase in covariances ... larger for the older age groups and for the low-order covariances”



## Connections to Ljungqvist and Sargent's earlier inquiries

### Turbulence and generous European benefits (JPE 1998)

- Turbulence increases European unemployment
- ... but leaves U.S. unemployment unchanged.

### European layoff costs / stochastic aging (ECMA 2008)

- In tranquil times, European unemp. below that of the U.S.
- In turbulent times, older Europeans suffer long-term unemp.

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### This paper OLG Bewley growth model

#### Ben-Porath human capital technology

#### Ex ante heterogeneity (high school / college)

- earlier findings carry over to and are consistent with research on aggregate growth models, life-cycle dynamics and job creation/destruction
- European minimum wage causes youth unemployment
- Low-type workers are more prone to shorten careers
- Endogenous age-dependent earnings persistence (Moffitt and Gottschalk, working paper 1995)

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## Framework robustness

- Yes, matching and search-island (JME 2007a)
- No, employment-lottery rep. family (JME 2007b)

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## Probing the “tax story” for European unemployment

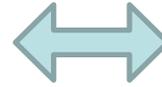
- Complete markets and employment lotteries are not necessary. Given indivisible labor, an agent can instead vary length of labor market career (“time averaging”) and save for consumption (NBER Macro Annual 2006)
- .... social security can put careers at a corner solution
- .... permanent neg. earnings shocks can shorten careers
- .... agents with “steeper” earnings profiles choose longer careers (RED 2014)



# Random matching in the labor market

## Realization of stochastic events

Workers supply labor  $\hat{n}$   
and invest in human capital



Firms with productivity  $z$   
demand labor

Earnings shock  $\theta$



Firms rent capital and produce  
 $F(z, k, \theta\hat{n})$

Human capital  
invest. outcome



$H_i^n(h, \bar{h}; \ell)$

Exogenous job destruction rate  $\lambda$

(the same fraction of workers must leave the labor market)

Human capital loss



$H_i^\lambda(\bar{h}, h')$

Additional forced layoffs of inexperienced workers at rate  $\tilde{\lambda} - \lambda$   
(but no jobs are destroyed)

Firm productivity



$Z(z, z')$

Endogenous job destruction by firms at rate  $q$   
(the same fraction of workers must leave the labor market)

Continuing employed  
inexperienced workers  
become experienced  
with prob.  $\pi$



Workers quit voluntarily  
(but no jobs are destroyed)

Workers consume and make decisions for next period