CHAPTER 5

The Empirics of Agglomeration Economies

Pierre-Philippe Combes*,†, Laurent Gobillon‡,§,‖

* Aix-Marseille University (Aix-Marseille School of Economics), CNRS & EHESS, Marseille, France
† Economics Department, Sciences Po, Paris, France
‡ Centre for Economic Policy Research (CEPR), London, UK
§ Institut National d’Etudes Démographiques, Paris, France
‖ Paris School of Economics, Paris, France

The Institute for the Study of Labor (IZA), Bonn, Germany

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Abstract

We propose an integrated framework to discuss the empirical literature on the local determinants of agglomeration effects. We start by presenting the theoretical mechanisms that ground individual and aggregate empirical specifications. We gradually introduce static effects, dynamic effects, and workers’ endogenous location choices. We emphasize the impact of local density on productivity, but we also consider many other local determinants supported by theory. Empirical issues are then addressed. The most important concerns are about endogeneity at the local and individual levels, the choice of a productivity measure between wages and total-factor productivity, and the roles of spatial scale, firms’ characteristics, and functional forms. Estimated impacts of local determinants of productivity, employment, and firms’ location choices are surveyed for both developed and developing economies. We finally provide a discussion of attempts to identify and quantify specific agglomeration mechanisms.

Keywords

Agglomeration gains, Density, Sorting, Learning, Location choices

JEL Classification Codes

R12, R23, J31

5.1. INTRODUCTION

Ongoing urbanization is sometimes interpreted as evidence of gains from agglomeration that dominate its costs, otherwise firms and workers would remain sparsely distributed. One can imagine, however, that the magnitude of agglomeration economies depends on
the type of workers and industries, as well as on the period and country. This is a first motivation to quantify agglomeration economies precisely, which is the general purpose of the literature reviewed in this chapter. Moreover, firms’ and workers’ objectives, profit and utility, are usually not in line with collective welfare or the objective that some policy makers may have in particular for productivity or employment. Even if objectives were identical, individual decisions may not lead to the collective optimum as firms and workers may not correctly estimate social gains from spatial concentration when they choose their location. Generally speaking, an accurate estimation of the magnitude of agglomeration economies is required when one tries to evaluate the need for larger or smaller cities. If one were to conclude that the current city size distribution is not optimal, such an evaluation would be necessary for the design of policies (such as taxes or regulation) that should be implemented to influence agents’ location choices toward the social optimum. Lastly, many a priori aspatial questions can also be indirectly affected by the extent to which firms and workers relocate across cities, as for instance, inequalities among individuals and the possible need for policies to correct them. Inequality issues might be less severe when workers are mobile and they rapidly react to spatial differences in the returns to labor. Addressing such questions requires beforehand a correct assessment of the magnitude of agglomeration economies.

*Agglomeration economies* is a large concept that includes any effect that increases firms’ and workers’ income when the size of the local economy grows. The literature proposes various classifications for the different mechanisms behind agglomeration economies, from *Marshall* (1890), who divides agglomeration effects into technological spillovers, labor pooling, and intermediate input linkages, to the currently most used typology proposed by *Duranton and Puga* (2004), who rather consider sharing, matching, and learning effects. Sharing effects include the gains from a greater variety of inputs and industrial specialization, the common use of local indivisible goods and facilities, and the pooling of risk; matching effects correspond to improvement of either the quality or the quantity of matches between firms and workers; learning effects involve the generation, diffusion, and accumulation of knowledge. Ultimately one would like an empirical assessment of the respective importance of each of these components. Unfortunately, the literature has not reached this goal yet, and we will see that there are only rare attempts to distinguish the various channels behind agglomeration economies. They are mostly descriptive and we present them at the end of this chapter. We choose rather to detail the large literature that tries to evaluate the overall impact on local outcomes of spatial concentration, and of a number of other characteristics of the local economy, such as its industrial structure, its labor force composition, or its proximity to large locations. In other words, what is evaluated is the impact on some local outcomes of local characteristics that shape agglomeration economies through a number of channels, not the channels themselves. Local productivity and wages have been the main focus of attention, but we also present the literature that studies how employment and firm location decisions are influenced by local characteristics.
When estimating the overall impact of a local characteristic, such as the impact of local employment density on local productivity, one cannot know whether the estimated effect arises mostly from sharing, matching, or learning mechanisms, or from all of them simultaneously. Most positive agglomeration effects can also turn negative above some city size threshold, or can induce some companion negative effects, and one cannot say whether some positive effects are partly offset by negative ones, as only the total net impact is evaluated. Moreover, while some mechanisms imply immediate static gains from agglomeration, other effects are dynamic and influence local growth. We take into account all these theoretical issues in our framework of analysis, as this is required to correctly choose relevant empirical specifications, correctly interpret the results, and discuss estimation issues. Crucially, even if the effects of mechanisms related to agglomeration economies are not identified separately, knowing, for instance, by how much productivity increases when one increases the number of employees per square meter in a city is crucial for the understanding of firms’ and workers’ location choices or for the design of economic policies.

We will see that the role of local characteristics is already not that trivial to evaluate. Beyond some interpretation issues that we will detail, the main difficulty arises from the fact that one does not seek to identify correlations between local characteristics and a local outcome but seeks to identify causal impacts. Basic approaches can lead to biased estimates because of endogeneity concerns at both the local level and the individual level. Endogeneity issues at the local level arise from either aggregate missing variables that influence both local outcomes and local characteristics, or reverse causality as better average local outcomes can attract more firms and workers in some locations, which in turn affects local characteristics. Endogeneity issues at the individual level occur when workers self-select across locations according to individual factors that cannot be controlled for in the specification, typically some unobserved abilities, or when they choose their location according to their exact individual outcome that depends on individual shocks possibly related to local characteristics. Dealing with these various sources of endogeneity is probably the area where the literature has made the greatest progress over the last decade. It is not possible anymore to evaluate the determinants of local outcomes without addressing possible endogeneity issues. Therefore, we largely discuss the sources of endogeneity and the solutions proposed in the literature.

Since various agglomeration mechanisms are at work and the impact of many local characteristics on different local outcomes has been studied, it is necessary to first clarify the theories that are behind the specifications estimated in the literature. Section 5.2 starts from a simple model and the corresponding specification that emphasizes the determinants of local productivity. This model is then progressively extended to encompass additional mechanisms, moving from static specifications to dynamic frameworks, while stressing the role of individual characteristics and individual location choices. This approach helps to clarify some of the endogeneity issues. Section 5.3 presents all the local
characteristics whose impact on productivity is studied in the literature, and relates them to theory. With such a theoretical background in mind, we systematically discuss a series of empirical issues in Section 5.4, mostly endogeneity concerns at the local and individual levels, as well as the solutions proposed to tackle them. We also discuss the choice of a productivity measure between wages and total-factor productivity (TFP), and the roles of spatial scale, firms’ characteristics, and functional forms. The magnitudes of estimated agglomeration effects on productivity are presented in Section 5.5, which covers in particular the effect of density, its spatial extent, and some possible heterogeneity of the impact across industries, skills, and city sizes. Section 5.5 also presents the results of some recent studies that use a structural approach or exploit natural experiments, as well as results on the role of the industrial structure of the local economy (namely, industrial specialization and diversity) and human capital externalities. Recent results for developing economies are detailed separately as the magnitudes are often not the same as for developed countries and their study is currently being expanded. In Section 5.6, estimated agglomeration effects on employment and firms’ location choices instead of productivity are discussed, after starting with considerations related to theory and the choice of a relevant empirical specification. Finally, Section 5.7 presents attempts to identify the channels through which agglomeration economies operate. The identification of such channels is one of the current concerns in the literature.

The organization of our chapter does not follow the development of the field over time. The literature started with the ambitious goal of estimating the impact of a large number of local determinants on employment growth at the city-industry level (Glaeser et al., 1992; Henderson et al., 1995). However, acknowledging some possibly serious interpretation and endogeneity concerns, the literature then became more parsimonious, focusing on static agglomeration effects on local productivity only (see Ciccone and Hall, 1996; Glaeser and Maré, 2001; Combes et al., 2008a). This was also made possible thanks to the availability of new datasets with a panel dimension at the individual level. More recent contributions incorporate additional effects such as the dynamic ones already suggested in the previous literature (see de la Roca and Puga, 2012), or consider richer frameworks through structural models involving endogenous location choices and different sources of heterogeneity across firms and workers (see Gould, 2007; Baum-Snow and Pavan, 2012). We choose to start with a simple but rigorous framework to analyze the effects of local determinants of productivity, which we then extend. Most of the contributions in the literature are ultimately encompassed, and this includes earlier ones focusing on employment growth. When referring to magnitudes of the effects, we focus more particularly on contributions later than those surveyed in Rosenthal and Strange (2004), but we refer to earlier contributions when they are useful for our discussion.

Still, there are a number of related topics that we do not cover, mostly because they involve too much material and the handbook editors made the choice of devoting
separate chapters to them. In particular, a specific case where the effect of an agglomera-
tion mechanism can be identified is technological spillovers and the links between
agglomeration and innovation. This topic is covered by Carlino and Kerr (2015),
who also discuss the literature on agglomeration and entrepreneurship, as it is often
grounded on technological spillovers. Similarly, we do not cover the literature on the
interactions between agglomeration economies and place-based policies, since it is con-sidered in Neumark and Simpson (2015). Finally, we do not present the various attempts
made to measure spatial concentration. Nevertheless, we refer to spatial concentration
indices in the last part of the survey as some articles use them in regressions to attempt
to identify mechanisms of agglomeration economies.

5.2. MECHANISMS AND CORRESPONDING SPECIFICATIONS

It is not possible to discuss the estimation of agglomeration economies without first clar-
ifying the theories and underlying mechanisms that are assessed empirically by the liter-
ature. This section presents these theories so that we can then correctly interpret estimates
and discuss possible estimation issues.

5.2.1 Static agglomeration effects and individual skills

5.2.1.1 Separate identification of skills and local effects

The earlier literature studies agglomeration economies at an aggregate spatial level, the
region or the city. An outcome in a local market is typically regressed on a vector of local
variables. In this section, we focus mostly on the impact of the logarithm of density on the
logarithm of workers’ productivity, measured by nominal wage. This corresponds to the
relationship considered by Ciccone and Hall (1996), who had a large impact on the
recent evolution of the literature. The role of other local determinants such as market
access, industrial diversity, or specialization has also been considered, and will be detailed
in Section 5.3. Other local outcomes such as industry employment growth or firms’ loca-
tion choices will be discussed in Section 5.6.

Let us first consider a setting without individual heterogeneity among firms and
workers. Let $Y_{c,t}$ be the output of a representative firm located in market $c$ at date $t$.
The firm uses two inputs, labor $L_{c,t}$, and other factors of production $K_{c,t}$, such as land,
capital, or intermediate inputs. The profit of the firm is given by

$$\pi_{c,t} = p_{c,t} Y_{c,t} - \omega_{c,t} L_{c,t} - r_{c,t} K_{c,t},$$

where $p_{c,t}$ is the price of the good produced, $\omega_{c,t}$ is the wage rate in the local labor market,
and $r_{c,t}$ is the unit cost of nonlabor inputs. Suppose that the production function is of the
Cobb–Douglas type and can be written as
where \( 0 < \alpha < 1 \) is a parameter, \( A_{c,t} \) is the local TFP, and \( \alpha_{c,t} \) corresponds to local labor skills. As long as all local firms and workers are assumed to be identical, these quantities depend on \( c \) and \( t \) only. In turn, this is also the case for \( p_{c,t}, w_{c,t} \) and \( r_{c,t} \). In a competitive equilibrium, an assumption we discuss below, the first-order conditions for the optimal use of inputs reduce to

\[
Y_{c,t} = \frac{A_{c,t}}{\alpha a(1-\alpha)^{1-\alpha}} (s_{c,t} L_{c,t})^a K_{c,t}^{1-\alpha},
\]

(5.2)

The local average nominal wage depends on labor skills, \( s_{c,t} \), as well as on a composite local productivity effect, \( B_{c,t} \). This equation is enough to encompass almost all agglomeration effects that the literature has considered. If one goes back as far as Buchanan (1965), cities are places where firms and consumers share indivisible goods such as airports, universities, and hospitals, which generate a first type of agglomeration economies. In that case, the composite labor productivity effect, \( B_{c,t} \), and therefore the local average wage, are higher in larger cities because \( A_{c,t} \) is larger owing to the presence of local (public) goods. This corresponds to a first type of pure local externality in the sense that it is not mediated by the market. A second type of pure local externality, very different in nature, emerges when spatial concentration induces local knowledge spillovers that make firms more productive, as put forward in early endogenous growth models such as that of Lucas (1988). Again, this type of mechanism makes \( A_{c,t} \) larger in larger cities. For the moment, we implicitly assume that all these effects are instantaneous and affect only current values of \( A_{c,t} \). This is an important restriction that we discuss further below.

Economists have also emphasized a number of agglomeration mechanisms operating through local markets, sometimes referred to as “pecuniary externalities.” Because access to markets is better in larger cities, the price of goods there, \( p_{c,t} \), can be higher, and the costs of inputs, \( r_{c,t} \), lower. Both effects again make \( B_{c,t} \) larger.\(^1\) Ultimately, one would like to assess separately whether pure externalities or local market effects have the most significant role effect on local productivity, or whether, among market effects, local

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\(^1\) When a firm sells to many markets, \( p_{c,t} \) corresponds to the firm’s average income per unit sold, which encompasses trade costs, and the present analysis can easily be extended, as shown by Combes (2011). Let \( Y_{c,t} \) denote the firm’s exports to any other market \( r \). The output value is the sum of the value of sales in all markets, \( p_{c,t} Y_{c,t} = \sum r (p_{c,t} - r_{c,t}) Y_{c,t} = \sum r (p_{c,t} - r_{c,t}) \phi_{c,r} Y_{c,t} \), where \( p_{c,t} \) is the firm’s price in market \( r \), \( r_{c,t} \) represents trade costs paid by the firm to sell in market \( r \), and \( \phi_{c,r} = \frac{Y_{c,t}}{Y_{c,r}} \) is its share of output that is sold there. As a result, \( p_{c,t} = \sum r (p_{c,t} - r_{c,t}) \phi_{c,r} \) is the average of the firm’s prices over all its markets net of trade costs and weighted by its share of sales in each market. The closer to large markets the firm is, the lower the trade costs and the higher this average price. Similarly, when firms sell inputs from many markets, the closer these markets are, the lower the firms’ average unit cost of inputs, \( r_{c,t} \).
productivity gains arise from price effects mostly related to goods or inputs. However, such assessments are difficult, and a large part of the empirical literature on agglomeration economies simply quantifies the overall impact on productivity of characteristics of the local economy. The previous discussion shows, in particular, that the positive correlation between wages and density can result from pure externalities as well as effects related to good or input prices.

Furthermore, city size generates not only agglomeration economies but also dispersion forces. Typically, the cost of inputs that are not perfectly mobile, $r_{c,t}$, land at one extreme, is higher in larger cities. If competition is tough enough relative to the benefits from market access in large cities, the price of goods there, $p_{c,t}$, can be lower than in smaller cities. Congestion on local public goods can also emerge, which reduces $A_{c,t}$. Note also that if local labor markets are not competitive, the right-hand side in Equation (5.3) should be multiplied by a coefficient that depends on the local bargaining power of workers. If workers have more bargaining power in larger cities, their nominal wages are higher, and this constitutes an agglomeration effect. Alternatively, a lower bargaining power in larger cities is a dispersion force. The correlation between wage and density reflects only the overall impact of both agglomeration economies and dispersion forces. While the net effect of spatial concentration can be identified, this is not the case for the channels through which it operates. Conversely, if one wants to quantify independently the impact of market effects operating through $r_{c,t}$ and $p_{c,t}$, a strategy is required involving controls for pure externalities arising, for instance, from the presence of local public goods or local spillovers.

One can also consider the inclusion of controls for dispersion forces if data on local traffic congestion or housing/land prices, for instance, are available. This is a start to disentangling agglomeration economies and dispersion forces. Importantly, the motivation for introducing housing/land prices is their influence on the costs of inputs and not compensation for low or high wages in equilibrium such that workers are indifferent between places as in Roback (1982). Indeed, we are focusing here on the determinants of productivity and not on equilibrium relationships. Typically, land price is expected to have a negative impact on nominal wages in accordance with Equation (5.3), while the equilibrium effect implies a positive correlation between the two variables. As wages and land prices are simultaneously determined in equilibrium, controlling for land or housing prices can lead to serious endogeneity biases that are difficult to deal with (see the discussion in Section 5.4). This suggests that if land represents a small share of input costs, which is usually the case, it is probably better not to control for its price in regressions.

Testing the relevance of a wage compensation model and quantifying real wage inequalities between cities are interesting questions but they require considering simultaneously the roles of nominal wages, costs of living, and amenities. These questions are addressed in a burgeoning literature (Albouy, 2009; Moretti, 2013), which we briefly discuss in the conclusion. As far as the effect of agglomeration economies on productivity
only is concerned, the nominal wage constitutes the relevant dependent variable and there is no need to control for land prices as illustrated by our model.

Let us turn to the role of local labor skills, captured in Equation (5.3) by $s_{c,t}$. If workers have skills that are not affected by their location, typically inherited from their parents or acquired through education, one definitively does not want to include the effect of skills among agglomeration economies, since it corresponds to a pure composition effect of the local labor force and not an increase in productivity due to local interactions between workers. It is possible that, for reasons not related to agglomeration economies, higher skills are over-represented in cities. This can arise, for instance, if skilled workers value city amenities (related, for instance, to culture or nightlife) more than unskilled ones do or if, historically, skilled people have located more in larger cities and transmit part of their skills to their children who stay there. If the estimation strategy does not control for the selection of higher skills in cities, other local variables such as density capture their role, and the impact of agglomeration economies can be overstated. Alternatively, it is also possible that people are made more skilled by cities, through stronger learning effects in larger cities, or that skilled people generate more local externalities, as suggested by Lucas (1988). In that case, not controlling for the skill level in the city is the correct way to capture the total agglomeration effect due to a larger city size. A priori, both the composition effect and the agglomeration effect can occur, and a local measure of skills or education captures both. The aggregate approach at the city level discussed here does not consider individual heterogeneity and does not allow the separate identification of the two effects. This is its first important limit, and an individual data approach is more useful for that purpose, as detailed below.

Finally, a crucial issue is the time span of agglomeration effects. One can accept that productivity and then wages adjust quickly to variations in market-mediated agglomeration effects (operating through changes in $r_{c,t}$ and $p_{c,t}$), but they definitely do not for variations of most pure local externalities that can affect $A_{c,t}$ and $s_{c,t}$. Therefore, the literature tends to distinguish between static and dynamic agglomeration effects. When agglomeration effects are static, $B_{c,t}$ is immediately affected by current values of local characteristics but not by earlier values. This means that a larger city size in a given year affects local productivity only in that year, and that any future change in city size will instantaneously translates into a change in local productivity. By contrast, recent contributions simultaneously consider some possible long-lasting effects of local characteristics that are called dynamic effects. We focus here on static affects and introduce dynamic effects from Section 5.2.2 onward.

Let us turn now to a first empirical specification encompassing static agglomeration effects where the logarithm of the composite productivity effect, $B_{c,t}$, is specified in reduced form as a function of the logarithm of local characteristics and some local unobserved effects. Average local skills, $s_{c,t}$, are specified as a log-linear function of local education and again some local unobserved terms. The sum of all unobserved components is supposed
to be a random residual denoted $\eta_{c,t}$. Denoting $y_{c,t}$ as the measure of the local outcome, here the logarithm of local wage, we obtain from Equation (5.3) the specification

$$y_{c,t} = Z_{c,t} \gamma + \eta_{c,t},$$  \hspace{1cm} (5.4)

where $Z_{c,t}$ includes local variables for both the local composite productivity component and skills. If explanatory variables reduce to the logarithm of density and local skills variables capturing only skill composition effects, and that there is no correlation between the random component and explanatory variables, then the ordinary least squares (OLS) estimate of the elasticity of productivity with respect to density is a consistent measure of total net agglomeration economies. This elasticity is crucial from the policy perspective even if the channels of agglomeration economies and dispersion forces are not identified. For instance, a value for the elasticity of the local outcome with respect to density of 0.03 means that a city twice as large (knowing that a factor of 10 is often obtained for the inter-quartile of local density in many countries) has $2^{0.03} - 1 \approx 2.1\%$ greater productivity, because of either pure local externalities or market agglomeration effects that dominate dispersion effects of any kind.

As mentioned in Section 5.1, the usual goal of the empirical works is to identify causal impacts—that is, what would be the effect on local outcomes of changing some of the local characteristics. Beyond other endogeneity concerns discussed below, a first issue with specification (5.4) is that density can be correlated with some of the local unobserved skill components entering the residual. For instance, proxies for local skills such as diplomas may not be enough to capture all the skills that affect productivity. If unobserved skills are randomly distributed across locations, the OLS estimate of the density parameter is a consistent estimator of the magnitude of agglomeration economies. Alternatively, if unobserved skills are correlated with density, there is an endogeneity issue and the OLS estimate is biased.

Unobserved skills can be taken into account with individual panel data. This requires us to extend our setting to the case where workers are heterogeneous. We assume now that local efficient labor is given by the sum of all efficient units of labor provided by heterogeneous workers—that is, $s_{c,t}L_{c,t} = \sum_{i \in \{c,t\}} si_i \ell_{i,t}$, where $\ell_{i,t}$ is the number of working hours provided by individual $i$ and $si_i$ is individual efficiency at date $t$. The wage bill is now $\sum_{i \in \{c,t\}} w_{i,t} \ell_{i,t}$, where $w_{i,t}$ is the individual wage. Profit maximization leads to

$$w_{i,t} = B_{i,t}s_{i,t}. \hspace{1cm} (5.5)$$

Let $X_{i,t}$ be time-varying observed individual characteristics and $u_i$ be an individual fixed effect to be estimated. We make the additional assumption that individual efficiency can be written as the product of an individual-specific component, $\exp(X_{i,t}\theta + u_i)$, and a residual, $\exp(\epsilon_{i,t})$, reflecting individual- and time-specific random effects. Here, $u_i$ captures the effects of individual unobserved skills which are supposed to be constant over time. Taking the logarithm of (5.5) and using the same specification of agglomeration effects as for (5.4) gives
\[ y_{i,t} = u_i + X_{i,t} \theta + Z_{c(i,t),t} \gamma + \eta_{c(i,t),t} + \epsilon_{i,t} , \]  

(5.6)

where \( y_{i,t} \) is the individual local outcome, here the logarithm of individual wage at date \( t \), and \( \epsilon(i,t) \) is the labor market where individual \( i \) is located at date \( t \). Note that we implicitly assume a homogeneous impact of local characteristics \( \gamma \) across all workers, areas, and industries. Heterogeneous impacts are considered in Section 5.2.1.2. For now, we consider that individual fixed effects are here only to capture unobservable skills, although we will discuss in Section 5.2.2 the fact that they can also capture learning effects that may depend on city size.

The use of individual data and the introduction of an individual fixed effect in specification (5.6) were first proposed by Glaeser and Maré (2001), and this should largely reduce biases due to the use of imperfect measures of skills. Most importantly, the individual fixed effect makes it possible to control for all the characteristics of the individual shaping skills that do not change over time and the effect of which can be considered to be constant over time. They include education, which is often observable, but also many other characteristics that are more difficult to observe, such as the education of parents and grandparents, the number of children in the family, mobility during childhood, and personality traits. Since the individual fixed effects are allowed to be correlated with local variables such as density, one can more safely conclude that the effects of local characteristics do not capture some composition effects owing to sorting on the individual characteristics.

The second advantage of individual data is that the local average of any observed individual characteristic can be introduced in the set of local variables simultaneously with the individual characteristic itself or with the individual fixed effect. In particular, while the individual fixed effect controls for the individual level of education, one can consider in \( Z_{c,t} \) the local share of any education level to assess whether highly skilled workers exert a human capital local externality on other workers.\(^2\) The estimated effects of local variables such as density then correspond to agglomeration economies other than education externalities. As discussed above, such a distinction cannot be made when using aggregate data.

The sources of identification of local effects can be emphasized by considering specification (5.6) in first difference, which makes the unobserved individual effect disappear. For simplicity’s sake, consider only two terms in the individual outcome specification such that \( y_{i,t} = Z_{c(i,t),t} \gamma + u_i \), where \( Z_{c,t} \) includes only density. For individuals staying in the same local market \( c \) at two consecutive dates, the first difference of outcome is given by \( y_{i,t} - y_{i,t-1} = (Z_{c,t} - Z_{c,t-1}) \gamma \), and time variation of density within the local market participates in the identification of the density effect, \( \gamma \). For individuals moving from market \( c \) to market \( c' \), we have \( y_{i,t} - y_{i,t-1} = (Z_{c',t} - Z_{c,t-1}) \gamma \), and both spatial and time variations of density contribute to identifying the density effect. If there is no mover,

\(^2\) The interpretation based on externalities requires further caution. It is discussed in Section 5.3.3.
agglomeration economies are still identified, but from time variations for stayers only. This is because there is a single parameter to estimate, and averaging the first-differenced outcome equation of stayers at the local-time level, one gets $Z \times (T - 1)$ independent relationships, where $Z$ is the number of local markets.

Note that we assume for the moment that the specification is the same for stayers and movers—that is, that the individual parameters $\theta$, the effects of local characteristics $\gamma$, and the distributions of random components are identical. Should this assumption be questioned, one could choose to estimate (5.6) separately on the subsamples of stayers and movers since identification is assured for each subsample, and one could in turn use the separate estimates to test the assumption of homogeneity across the two groups.

Specification (5.6) can be estimated directly by OLS once it has been written in first difference (or projected in the within-individual dimension) to remove the individual fixed effects, but the computation of standard errors is an issue. Indeed, the covariance matrix has a complex structure owing to unobserved local effects and the mobility of workers across labor markets. For mobile individuals, the first difference of the specification includes two different unobserved local shocks, $\eta_{c,t}$ and $\eta_{c,t-1}$, and the locations of those shocks ($c$ and $c'$) vary across mobile individuals, even for those initially in the same local market because they may not have the same destination after they move. There is thus no way to sort individuals properly to get a simple covariance matrix structure and to cluster standard errors at each date by location. It is tempting to ignore unobserved local effects, but this can lead to important biases of the estimated standard errors for effects of local variables, as shown by Moulton (1990).

Alternatively, it is possible to use a two-step procedure that both solves this issue and has the advantage of corresponding to a more general framework. Consider the following system of two equations:

\begin{align*}
y_{i,t} &= u_i + X_{i,t} \theta + \beta_{c(i,t),t} + \epsilon_{i,t}, \quad (5.7) \\
\beta_{c,t} &= Z_{c,t} \gamma + \eta_{c,t}, \quad (5.8)
\end{align*}

where $\beta_{c,t}$ is a local-time fixed effect that captures the role of any location-time variable whether it is observed or not. The introduction of such fixed effects capturing local unobserved components makes the assumption of independently distributed individual shocks more plausible. The specification is also more general since it takes into account possible correlations between local-time unobserved characteristics and individual characteristics. There are thus fewer possible sources of biases, and this in turn should lead to a more consistent evaluation of the role of local characteristics.

Estimating this model is more demanding in terms of identification, and having movers between locations is now required. Assume for simplicity’s sake that the first equation of the model is given by $y_{i,t} = \beta_{c(i,t),t} + u_i$. When one rewrites this specification in first difference for nonmovers and movers, one gets $y_{i,t} - y_{i,t-1} = \beta_{c,t} - \beta_{c,t-1}$ and $y_{i,t} - y_{i,t-1} =$
\( \beta'_{c,t} - \beta_{c,t-1} \), respectively. There is one parameter \( \beta_{c,t} \) to be identified for each location at each date. If there is no mover, one wishes to average the specification at the local-time level for stayers as before but ends up with \((Z - 1) \times T\) independent relationships, whereas there are \(Z \times T\) parameters to estimate. In other words, one can identify the time variations of local effects for any location but not their differences between locations.

By contrast, when there are both stayers and movers, identification is assured as can be shown rewriting the specification in differences in differences. The difference of the wage time variation between a mover to \(c'\), denoted \(i'\), and a nonmover \(i\) initially in the same location \(c\) is given by \((y_{i',t} - y_{i',t-1} - (y_{i,t} - y_{i,t-1})) = \beta'_{c,t} - \beta_{c,t}\). For any pair of locations, the difference in wage growth between movers and nonmovers identifies the difference of local effects between the two locations. Moreover, the wage growth of stayers identifies the variation of local effects over time as before. All parameters \( \beta_{c,t} \) are finally identified when local markets are well interconnected through stayers and flows of movers, up to one that needs to be normalized to zero as differences do not allow the identification of levels. Interconnection means that any pair of location-time couples, \((c,t)\) and \((c',t')\), can be connected through a chain of pairs of location-time couples \((j,\tau - 1)\) and \((j',\tau)\) such that there are migrants from \(j\) to \(j'\) between dates \(\tau - 1\) and \(\tau\) if \(j \neq j'\), or stayers in \(j\) between the two dates if \(j = j'\). In other words, assuming that there are some migrants between every pair of locations in the dataset, we have \(Z^2 \times (T - 1)\) independent relationships and only \(Z \times T - 1\) parameters to estimate. Crucially, the assumption that the specification is identical for both movers and stayers is now required, otherwise identification is not possible. Alternatively, more structural approaches can help to some extent to solve the identification issue, and we present them in Section 5.2.4.

Note finally that in practice specification (5.7) is estimated in a first step. Panel data estimation techniques such as within estimation are used because considering a dummy variable for each individual to take into account the fixed effect \(u_i\) would be too demanding for a computer. The estimates of \( \beta_{c,t} \) are then plugged into Equation (5.8). The resulting specification is estimated in a second stage using linear methods, including one observation for the location-time fixed effect normalized to zero. The sampling error on the dependent variable, which is estimated in the first stage, must be taken into account in the computation of standard errors, and it is possible to use feasible general least squares (see Combes et al., 2008a, for the implementation details). A more extensive discussion on the estimation strategy addressing endogeneity issues is presented in

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3 If local markets are not all interconnected, groups of fully interconnected location-time couples must be defined \(ex\ ante\) such that location-time fixed effects are all identified within each group up to one being normalized to zero. For more details, the reader may refer to the literature on the simultaneous identification of worker and firm fixed effects in wage equations initiated by Abowd et al. (1999).
Section 5.4, but we first augment the model to consider the role of more sophisticated agglomeration mechanisms.

**5.2.1.2 Heterogeneous impact of local effects**

The profit maximization we conducted above to ground our specification emphasizes that agglomeration effects may relate to pure externalities, or to good or input price effects. Obviously, the magnitude of these channels may differ across industries. For instance, the impact of density may be greater in high-tech industries owing to greater technological externalities, and good or input price effects depend on the level of trade costs within each industry. The consideration of agglomeration mechanisms that are heterogeneous across industries simply requires extending the specification such that

\[ y_{i,t} = u_i + X_{i,t} \theta + Z_{i(i,t),s(i,t)} + \eta_{i(i,t),s(i,t),t} + \epsilon_{i,t}, \]

(5.9)

where \( s(i,t) \) is the industry where individual \( i \) works at time \( t \), \( \gamma_s \) is the effect of local characteristics in industry \( s \), and \( \eta_{c,s,t} \) is a location–industry–time shock. This specification can be estimated in several ways. The most straightforward one consists in splitting the sample by industry and implementing the approach proposed in Section 5.2.1.1 for each industry separately. Nevertheless, this means that the coefficients of individual explanatory variables as well as individual fixed effects are not constrained to be the same across industries, which may or may not be relevant from a theoretical point of view. This also entails a loss of precision for the estimators. An alternative approach consists in considering among explanatory variables some interactions between density, or any other local characteristic, and industry dummies, and estimating the specification in the within-individual dimension as before to recover their coefficients which are the parameters \( \gamma_s \).

Again, estimated standard errors may be biased owing to heteroskedasticity arising from location–industry–time random effects, \( \eta_{c,s,t} \). To deal with this issue, it is possible to consider a two-step approach which makes use of location–industry–time fixed effects, \( \beta_{c,s,t} \), in the following system of equations:

\[ y_{i,t} = u_i + X_{i,t} \theta + \beta_{c(i,t),s(i,t),t} + \epsilon_{i,t}, \]

(5.10)

\[ \beta_{c,s,t} = Z_{c,i} \gamma_s + \eta_{c,s,t}, \]

(5.11)

Location–industry–time fixed effects are estimated with OLS once Equation (5.10) has been projected in the within-individual dimension, as done previously when estimating location–time fixed effects. They are identified up to one effect normalized to zero provided that all locations and industries are well interconnected by workers mobile across locations and industries.\(^4\) Their estimators are plugged into Equation (5.11), which is estimated in a second stage.

\(^4\) As before, groups of fixed effects should be defined ex ante if not all locations and industries are properly interconnected. Of course, the larger the number of industries, the more likely it is that location-industry-time fixed effects are not all identified.
Importantly, introducing the industry dimension increases the number of local characteristics that can have an agglomeration effect. It has become common practice to distinguish between urbanization economies and localization economies. Whereas urbanization economies correspond to externalities arising from characteristics of the location such as density, localization economies correspond to externalities arising from characteristics of the industry within the location. The determinants of agglomeration economies considered in the literature thus depend only on location for urbanization economies and on both location and industry for localization economies. The local determinant of localization economies most often considered is specialization, which is defined as the share of the industry in local employment. While the use of density makes it possible to assess whether productivity increases with the overall size of the local economy, the use of specialization allows the assessment of whether it increases with the local size of the industry in which the firm or worker operates. The pure externalities and market externalities distinguished above can operate at the whole location scale or at the industry-location level. In line with these arguments, one may rather want to estimate in the second step the following specification:

$$\beta_{c,s,t} = Z_{c,t} \gamma_s + W_{c,s,t} \delta_s + \eta_{c,s,t},$$  \hspace{1cm} \text{(5.12)}$$

where $W_{c,s,t}$ are determinants of localization economies including specialization and $Z_{c,t}$ are the determinants of urbanization economies. All the local characteristics considered in the literature are detailed in Section 5.3.

One estimation issue is that the number of fixed effects to estimate in the first stage increases rapidly with the number of locations, and we are not aware of any attempt to estimate the proposed specification. As an alternative, one can mix strategies as proposed by Combes et al. (2008a) and estimate

$$\gamma_{i,t} = u_i + X_{i,t} \theta + \beta_{c(i,t),t} + W_{c(i,t),i(t),t} \delta_i + \epsilon_{i,t},$$  \hspace{1cm} \text{(5.13)}$$

and

$$\beta_{c,t} = Z_{c,t} \gamma + \eta_{c,t}.$$  \hspace{1cm} \text{(5.14)}$$

This model is less general than (5.10) and (5.12) since unobserved location-industry-time effects are not controlled for in the first step, and determinants of urbanization economies are assumed to have a homogeneous impact across industries in the second step (as $\gamma$ does not depend on the industry). Still, heterogeneous effects of determinants of localization economies are identified in the first stage on top of controlling for unobserved location-time effects.

It is also easy to argue from theory that agglomeration effects are heterogeneous across different types of workers. Some evidence suggests, for instance, that more productive workers are also the ones more able to reap the benefits from agglomeration (see Glaeser and Maré, 2001; Combes et al., 2012c; de la Roca and Puga, 2012). A specification similar to (5.9) can be used to study, for instance, the heterogeneous effect of density across diplomas. One would simply consider diploma-specific coefficients for density instead of industry-specific ones. However, diplomas usually do not change over time. When a two-step procedure is used, this implies that one diploma-location-time fixed effect must be
normalized to zero for each diploma. The alternative strategy of estimating the two-step procedure on each diploma separately is not much less precise than it was for industries since all the observations for any given individual are in the same diploma subsample, and there is thus a unique individual fixed effect for each worker to be estimated.

However, diplomas may not be enough to fully capture individual skill heterogeneity. One may wish to consider that the effect of density is specific to each individual as in the following specification:

$$y_{i,t} = u_i + X_{i,t} \theta + Z_{c(i,t),t} \gamma_i + \eta_{c(i,t),t} + \epsilon_{i,t}, \quad (5.15)$$

where $\gamma_i$ is an individual fixed effect. Parameters can be estimated using an iterative procedure. For a given value of $\theta$, one can regress $y_{i,t} - X_{i,t} \theta$ on $Z_{c(i,t),t}$ for each individual. This gives some estimates for $\gamma_i$ and $u_i$. Then, $\theta$ is estimated by regressing $y_{i,t} - Z_{c(i,t),t} \gamma_i - u_i$ on $X_{i,t}$. The procedure is repeated using the parameter values from the previous iteration until there is convergence.

One can further extend the model and consider that location in general, and not density alone, has a heterogeneous effect on the local outcome. One considers in this case an interaction term between a local fixed effect and an individual fixed effect. This amounts to saying that it is not the effect of density but rather the combined effect of all local characteristics, whether they are observed or not, which is heterogeneous across individuals. The first step of the two-stage procedure in this case becomes

$$y_{i,t} = u_i + X_{i,t} \theta + \beta_{c(i,t),t} + \delta_{c(i,t),t} + \epsilon_{i,t}, \quad (5.16)$$

with the identification restriction that $\sum_i \nu_i = 0$ and one of the local terms $\delta_{c,t}$ is normalized to zero. As before, the specification can be estimated with an iterative procedure. The estimators of parameters $\delta_{c,t}$ are regressed in the second step on local variables to assess the extent to which agglomeration economies influence the local return of unobserved individual characteristics. An additional extension to make the specification even more complete would consist in having the coefficients of individual characteristics depend on the individual. Note that as there are many individual-specific effects entering the model in a nonadditive way, the time span should be large for the estimations to make sense, and there is no guarantee that a large number of periods is enough for the parameters to be properly estimated. In any case, most of the specifications in this last paragraphs are material for future research.

### 5.2.2 Dynamic impact of agglomeration economies

So far, we have considered that agglomeration economies have an instantaneous effect on productivity and then no further impact in the following periods. In fact, agglomeration economies can be dynamic and can have a permanent impact such as when technological

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5 This procedure is inspired from Bai (2009), who proposes such a procedure to estimate factor models.
spillovers increase local productivity growth or when individuals learn more or faster in larger cities as suggested by Lucas (1988). One can even argue that an individual moves from a large city to a smaller can transfer part of the individual’s productivity gains from agglomeration to the new location and be more productive than other individuals who have not worked in a large city. In that case, dynamic effects operate through the impact of local characteristics on the growth of $A_{c,t}$ and $s_{i,t}$, which are involved in Equation (5.5). One can also consider dynamic effects operating through $p_{c,t}$ and $r_{c,t}$. For instance, agglomeration can facilitate the diffusion of information about the quality of goods and inputs, and this in turn can have an impact on price variations across periods (e.g., when prices are chosen by producers under imperfect competition). Therefore, even if dynamic effects relate more plausibly to technological spillovers and learning effects, market agglomeration economies can also present dynamic features. As a result, the identification issues are like those for static agglomeration economies, and one usually estimates only the overall impact of dynamic externalities and not the exact channel through which they operate. Note that the literature that first tried to identify agglomeration effects on local industrial employment, which dates back to Glaeser et al. (1992) and Henderson et al. (1995), adopts this dynamic perspective from the very beginning. We present this literature in Section 5.6.1.

We explain in this section how the previous productivity specifications can be extended to encompass dynamic effects. The distinction between static and dynamic effects was pioneered by Glaeser and Maré (2001), and we elaborate the discussion below from their ideas and those developed by de la Roca and Puga (2012), which is currently one of the most complete studies on the topic. For a model with static local effects only (disregarding the role of time-varying individual and industry characteristics), written as $y_{i,t} = u_i + \beta_{c(i),t} + \epsilon_{i,t}$, the individual productivity growth rate is simply related to the time difference of static effects:

$$y_{i,t} - y_{i,t-1} = \beta_{c(i),t} - \beta_{c(i),t-1} + \epsilon_{i,t}, \quad (5.17)$$

where $\epsilon_{i,t}$ is an error term. Dynamic local effects in their simplest form are introduced by assuming for $t \geq 1$ that

$$y_{i,t} - y_{i,t-1} = \beta_{c(i),t} - \beta_{c(i),t-1} + \mu_{c(i),t-1} + \epsilon_{i,t}, \quad (5.18)$$

where $\mu_{c(i),t-1}$ is a fixed effect for city $c$ at date $t - 1$, which corresponds to the impact of city $c$ on productivity growth between $t - 1$ and $t$, and thus captures dynamic local effects. Interestingly, this implies

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6 In this chapter, we consider that $\epsilon_{i,t}$ is a generic notation for the residual and use it extensively in different contexts.
where $\zeta_{i,t}$ is an error term. This equation includes the past values of local effects and shows that dynamic effects, even when they affect only the annual growth rate of a local outcome, do have a permanent impact on its level. Nevertheless, we have made some major assumptions to reach this specification. We now detail them and discuss how to relax them.

A first implicit assumption is that dynamic effects are perfectly transferable over time. For instance, knowledge does not depreciate even after a few years. To consider depreciation, one could introduce in (5.18) some negative effects of past city terms $\mu_{c(i,t-1),t-k}$, $k > 1$ with coefficients lower than 1 in absolute value, and this would lead to an auto-regressive specification such that terms $\mu_{c(i,t-1),t-k}$ have an effect attenuated with a time lag when the model is rewritten in level.

Importantly, specification (5.19) makes more sense for individuals who stay in the same location than for movers. Dynamic local effects might also depend on where individuals locate at period $t$, and therefore on the destination location for movers. Individuals in a large city probably do not benefit from the same productivity gains from learning effects whether they move to an even larger city or to a smaller city (or if they stay where they are). In other words, dynamic gains are not necessarily fully transferable between locations, and the degree of transferability can depend on the characteristics of locations. Therefore, it might be more relevant to assume that dynamic effects depend on both the origin and destination locations and to rewrite the specification of local outcome as

$$y_{i,t} = y_{i,1} + \beta_{c(i,t),t} + \sum_{k=1}^{t-1} \mu_{c(i,t-k),c(i,t),t-k} + \zeta_{i,t}, \quad (5.20)$$

where $\mu_{j,c,\tau}$ is a time-varying fixed effect for being in city $j$ at period $\tau < t$ and in city $c$ at date $t$. The problem is that the number of parameters to be estimated for dynamic effects becomes very large (the square of the number of locations times the number of years in the panel). Moreover, restrictions on parameters must be imposed for the model to be identified. This can be seen, for instance, when writing the model in first difference for workers staying in the same location between dates $t-1$ and $t$, for which $c(i,t-1) = c(i,t)$:

$$y_{i,t} - y_{i,t-1} = \beta_{c(i,t),t} - \beta_{c(i,t-1),t-1} + \mu_{c(i,t-1),c(i,t),t-1} + \epsilon_{i,t}. \quad (5.21)$$

The evolution of the static agglomeration effect cannot be distinguished from the dynamic effect (and this is also true when considering movers instead of stayers). When one observes the productivity variation of stayers, one does not know whether it occurs because static local effects have changed or because some dynamic local effects take place.

de la Roca and Puga (2012) make some assumptions that allow the identification of the model and significantly reduce the number of parameters to be estimated. They assume that static and dynamic effects do not change over time—that is, $\beta_{c,t} = \beta$ and
$\mu_{j,c,t-k} = \mu_{i,c}$. Under these assumptions, $\mu_{c,c}$ captures both the dynamic effect and the evolution of static effects. This can be seen from Equation (5.21), where the evolution of static effects would be now fixed to zero. This should be kept in mind when assessing the respective importance of static and dynamic effects, as this cannot be done from the relative explanatory power of $\beta_c$ and $\mu_{j,c}$. Under these assumptions, it is also possible to rewrite the specification in a more compact form introducing the number of years the individuals have spent in each location:

$$y_{i,t} = u_i + X_{i,t} \theta + \beta_{c(i,t)} + \sum_j \mu_{j,c(i,t)} \epsilon_{i,j,t} + \epsilon_{i,t},$$

(5.22)

where $\epsilon_{i,j,t}$ is the experience acquired by individual $i$ until period $t$ in city $j$ (the number of years that individual spent there until date $t$), and $\mu_{j,c}$ captures the value of 1 year of this experience when the worker is located in city $c$. One can test whether the $\mu_{j,c}$ are statistically different from each other when $c$ varies for given $j$—that is, whether location-specific experience can be transferred or not transferred to the same extent to any location, as was assumed in (5.19). One can also quantify the respective importance of the effects $\beta_c$ and $\mu_{c,c}$ keeping in mind that it does not correspond to the respective importance of static and dynamic effects. Earlier attempts to evaluate dynamic effects on wages by Glaeser and Maré (2001), Wheeler (2006), and Yankow (2006) correspond to constrained and simplified versions of this specification, typically distinguishing only the impact on wage growth of moving or not moving to larger cities.

It is then possible in a second stage to evaluate the extent to which dynamic effects depend on the characteristics of the local economy, and to assess whether transferability relates to density of the destination location. One can consider the specification

$$\mu_{j,c} = Z_j,\psi + Z_c,\upsilon + \zeta_{j,c},$$

(5.23)

where $Z_{j,*}$ is the average over all periods of a vector of location–$j$ characteristics including density. In this specification, the effect of density in the location where learning took place is a linear function of variables entering $Z_{c,*}$ such as density. Clearly, all these dynamic specifications can be extended to encompass some heterogeneity across industries in the parameters of local variables, and possibly some localization effects.

An alternative approach that takes into account time variations in static and dynamic effects may consist in estimating density effects in one stage only, first specifying

$$\beta_{c,t} = Z_{c,t} \gamma + \eta_{c,t},$$

(5.24)

$$\mu_{j,c,t} = Z_{j,t}(\psi + Z_{c,t} \nu) + \zeta_{j,c,t},$$

(5.25)

and then plugging these expressions into Equation (5.20). This gives a specification where the coefficients associated with the different density terms can be estimated directly with linear panel methods. A limitation of this approach is again that it is difficult to compute standard errors taking into account unobserved local shocks because workers’
moves make the structure of the covariance matrix of error terms intricate when the model is rewritten in first difference or in the within dimension. On the other hand, the separate explanatory power of static and dynamic agglomeration effects is better assessed.

Finally, it is possible to generalize the framework to the case where both static and dynamic effects are heterogeneous across individuals. Specification (5.20) becomes

\[
y_{i,t} = u_i + X_{i,t} \theta + \beta_{c(i,t),t} + \delta_{c(i,t),t} v_i + \sum_{k=1}^{t-1} \left( \mu_{c(i,t-k),c(i,t),t-k} + \lambda_{c(i,t-k),c(i,t),t-k} r_i \right) + \epsilon_{i,t},
\]

(5.26)

where \( v_i \) and \( r_i \) are individual fixed effects verifying the identification assumption \( \sum v_i = \sum r_i = 0 \). Parameters can be estimated by imposing additional identification restrictions such as the fact that static and dynamic effects do not depend on time, and using an iterative procedure as in previous subsections. Note that such a specification has not been estimated yet. One of the best attempts is that of de la Roca and Puga (2012), who restrict the spatial dimension to three classes of city sizes only (which prevents the second-stage estimation and only allows them to compare the experience effect over the three classes). Importantly, they also make the further assumption that the impact of individual heterogeneity is identical for both static and dynamic effects—that is, \( v_i = r_i \).

D’Costa and Overman (2014) attempt to elaborate on the attempt of de la Roca and Puga (2012). They estimate the specification in first differences while allowing for \( v_i \neq r_i \), but they exclude movers to avoid having to deal with between-city dynamic effects.

### 5.2.3 Extending the model to local worker–firm matching effects

Marshall (1890) was among the first to emphasize that agglomeration can increase productivity by improving both the quantity and the quality of matches between workers and firms in local labor markets (see Duranton and Puga, 2004, for a survey of this type of mechanism). The better average quality of matches in larger cities can be considered as a static effect captured by the local fixed effects \( \beta_{c,i,t} \) estimated in previous subsections. The matching process in cities can also yield more frequent job changes, which can boost productivity growth. This dynamic matching externality can be incorporated into our framework by considering that at each period \( t \), a worker located in \( c \) receives a job offer with probability \( \phi_{c,t} \) to which is associated a wage \( \tilde{y}_{i,t} \). One assumes that workers change jobs within the local market at no cost and they accept a job offer if the associated wage is higher than the one they would get if they stayed with the same employer. To ease exposition, we suppose that migrants do not receive any job offer at their origin location, but receive one at the destination location once they have migrated. The probability of receiving such an offer is supposed to be the same as that for stayers in this market. We also assume for the moment that there is no dynamic effect other than through
job change. For workers receiving an offer, the wage at time $t$ is $y_{i,t} + \Delta_{i,t}$, where $y_{i,t}$ is given by Equation (5.7) and $\Delta_{i,t} = \max(0, y_{\tilde{i},t} - y_{i,t})$. The individual outcome is then given by

$$y_{i,t} = u_{i} + X_{i,t}\theta + \beta_{c,i} + \sum_{\tau=1}^{t-1} 1\{O(i,\tau)=1\} \Delta_{i,\tau} + \epsilon_{i,t},$$

(5.27)

where $O(i,\tau)$ is a dummy variable taking the value 1 if individual $i$ has received a job offer between dates $\tau - 1$ and $\tau$, and 0 otherwise.

For workers keeping the same job in location $c$ between the two dates, there is no dynamic matching gain, and wage growth is given by

$$y_{i,t} - y_{i,t-1} = (X_{i,t} - X_{i,t-1})\theta + \beta_{c,i} - \beta_{c,i-1} + \epsilon_{i,t},$$

(5.28)

where $\epsilon_{i,t} = \epsilon_{i,t} - \epsilon_{i,t-1}$.

For workers changing jobs within location $c$, improved matching induces a wage premium $\Delta_{i,t}$ and wage growth can be written as

$$y_{i,t} - y_{i,t-1} = (X_{i,t} - X_{i,t-1})\theta + \tilde{\beta}_{c,i} - \beta_{c,i-1} + \nu_{i,t},$$

(5.29)

where $\tilde{\beta}_{c,i} = \beta_{c,i} + E(\Delta_{i,t}|i \in (c,t), i \in (c,t))$ is the sum of the local fixed effect for stayers keeping their jobs and the expected productivity gain when changing job, and the new residual is $\nu_{i,t} = \epsilon_{i,t} + \Delta_{i,t} - E(\Delta_{i,t}|i \in (c,t-1), i \in (c,t))$.

For workers changing job between two locations $c$ and $\ell$, wage growth can be expressed as

$$y_{i,t} - y_{i,t-1} = (X_{i,t} - X_{i,t-1})\theta + \beta_{\ell,i} - \beta_{c,i-1} + \nu_{i,t},$$

(5.30)

where $\beta_{\ell,i} = \beta_{c,i} + E(\Delta_{i,t}|i \in (c,t), i \in (\ell,t))$ is the sum of the local fixed effect for stayers keeping their jobs in the destination location and the expected productivity gain when changing jobs from city $c$ to city $\ell$.\footnote{In fact, workers may move and take a wage cut if they expect future wage gains. This kind of intertemporal behavior cannot be taken into account in a static model as here but it can be taken into account in the dynamic framework developed in the next subsection.} This gain may depend on both cities as it could be related, for instance, to the distance between them or their industrial structure.

The difference in local effects from separate wage growth regressions for stayers changing jobs and stayers keeping the same job provides an estimate of the matching effect since $(\beta_{c,i} - \beta_{c,i-1}) - (\beta_{\ell,i} - \beta_{c,i-1}) = E(\Delta_{i,t}|i \in (c,t-1), i \in (\ell,t))$ If changing jobs increases productivity through improved matching, this difference should be positive for any location $c$. If agglomeration magnifies such dynamic matching effects, the probability of changing jobs should increase with density, and the difference $\tilde{\beta}_{c,i} - \beta_{c,i}$ should be larger in
denser areas. More generally, to assess which local characteristics are determinants of
dynamic matching effects, one can run the second-step regression:

$$\tilde{\beta}_{c,t} - \beta_{c,t} = Z_{c,t} \Phi + \eta_{c,t},$$

(5.31)

where $Z_{c,t}$ is a vector of local characteristics. Such a model has not been estimated yet, but
Wheeler (2006) makes one of the best attempts to do so. Owing to the small size of the
dataset, Wheeler (2006) cannot identify the role of local-time fixed effects, but his stra-
egy on the panel of workers changing job is equivalent to directly plugging (5.31), with
local market size as the single local characteristic, into the difference between (5.28) and
(5.29) to assess by how much the matching effect increases with local market size.

Exploiting wage growth for workers changing both job and city is more intricate, and
an important assumption which needs to be made (and was implicitly made in previous
sections) is that the location choice is exogenous. In order to get consistent estimates of
local effects when movers are used as a source of identification, the location choice should
not depend on individual-location shocks on wages conditional on all the explanatory vari-
ables and parameters in the model.8 This assumption is disputable since workers often
migrate because they receive a good job offer in another local labor market, or because
they had a bad original match with their firm. By the same token, we can argue that
job changes are endogenous for both movers and nonmovers, and this affects the estimates
of local effects obtained for specifications in this subsection. As this concern is certainly
important, it may be wise to use another kind of approach that explicitly takes into account
the endogeneity of location and job choices. This can be done with a dynamic model of
intertemporal location choices at the cost of imposing more structure on the specification
that is estimated. We now turn to this kind of structural approach, building on the same
underlying background.

5.2.4 Endogenous intertemporal location choices

So far, we have considered static and dynamic agglomeration effects within a static frame-
work where workers’ location choices are strictly exogenous: Workers do not take into
account wage shocks due to localized job opportunities in their migration or job change
decisions. When workers do consider alternative job opportunities when making their
decisions, it is also likely that they are forward-looking and take into account all future possible outcomes in alternative locations. As shown by Baum-Snow and Pavan (2012), it is possible to introduce static and dynamic agglomeration effects in a dynamic model of location choices that takes these features into account.9 Nevertheless, identification is achieved thanks to the structure of the model, and it is sometimes difficult to assess which conclusions

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8 This assumption is discussed at greater length from an econometric point of view in Section 5.4.2.
9 Gould (2007) also proposes a dynamic model where school attendance too is endogenous. See also Beaudry
et al. (2014) for a dynamic model with search frictions and wage bargaining with static agglomeration
effects but no dynamic agglomeration effects.
would remain under alternative assumptions. For simplicity’s sake, we present the main mechanisms of the model for employed workers and consider that there is no unemployment and no consumption amenities, these assumptions being relaxed in Baum-Snow and Pavan (2012). Unemployment can easily be added by considering that there is an additional state for workers and there are exogenous mechanisms (such as job destructions and job offers) leading to transitions between states. Consumption amenities can be considered by including location-specific utility components that do not affect local wages.

Individual unobserved heterogeneity is modeled as draws in a discrete distribution (instead of individual fixed effects). There are $H$ types of workers indexed by $h = 1, \ldots, K$. Worker $i$ getting a job in location $c$ draws a job match $\xi_{i,c}$ in a distribution which is specific to the location. For a given job, the match is drawn once and for all and does not vary over time. The wage of worker $i$ of type $h(i)$ located in market $c$ and occupying a job with match $\xi_{i,c}$ is a variant of Equation (5.22) given by

$$y_{i,t,c}(\xi_{i,c}) = X_{i,t} \theta + \beta_{h(i),c,t} + \sum_j \mu_{h(i),j,c} e_{i,j,t} + \xi_{i,c} + \epsilon_{i,c,t},$$

(5.32)

where $\beta_{h,c,t}$ is a static location effect depending on the worker type, $\mu_{h,j,c}$ is a location-specific experience effect depending on the worker type, and $\epsilon_{i,c,t}$ is a white noise. Note that whereas the wage depends on the draw of the white noise, we do not index the wage by it to keep the notation simple. A crucial difference from the specifications in previous sections is that we now have a specification for the potential outcome in any location $c$ at each date. Therefore, the wage is now indexed by $c$, and we write $y_{i,c,t}$ for any potential wage instead of $y_{i,t}$ as previously for the realized one.

The intertemporal utility and location choice are determined in the following way. Consider worker $i$ of type $h(i)$ located in city $c$ at period $t$. The worker earns a wage $y_{i,c,t}$ and, at the end of the period, has the possibility to move to another job within the same location or to a different location. Migration to another location can be achieved only if the worker gets a job offer in that location (as we have ruled out unemployment for simplicity). The probability of receiving a job within location $c$ for a worker of type $h$ is denoted $\phi_{h,c}$, and the probability of receiving a job in location $j \neq c$ is denoted $\phi_{h,c,j}$. There is a cost $C$ when changing jobs within the local market. If the worker moves between city $c$ and city $j$, the workers has to pay a moving cost $M_{c,j}$. Let us denote $V_{i,c,t}(\xi_{i,c})$ the intertemporal utility of an individual located in city $c$ at time $t$, and occupying a job with match $\xi_{i,c}$. This intertemporal utility can be expressed with the recursive formula

$$V_{i,c,t}(\xi_{i,c}) = y_{i,c,t}(\xi_{i,c}) + \phi_{h(i),c} E_{\xi_c} \max \left[ V_{i,c,t+1}(\xi_{i,c}), V_{i,c,t+1}(\xi_c) - C \right] + \sum_{j \neq c} \phi_{h(i),c,j} E_{\xi_j} \max \left[ V_{i,c,t+1}(\xi_{i,c}), V_{i,j,t+1}(\xi_j) - M_{c,j} \right],$$

(5.33)

where expectations are computed over the distributions of all future random terms including the matches $\xi_c$ when one changes jobs within location and $\xi_j$ when one changes jobs by moving to $j$ (but not the realized match $\xi_{i,c}$ for the current job). The first term
corresponds to the wage earned at the current location. The second term is the expected outcome associated with a possible offer of a job within the current location. It depends on the probability of receiving a job offer and on the expected future intertemporal utility, which is the one related to the new job if it is worth accepting the offer, or is the one related to the current job otherwise. The third term is the expected outcome associated with a possible job offer in other locations. It depends on the probability of receiving a job offer in every location and on the expected future intertemporal utility related to the location if it is worth moving there, or to the current location otherwise.

The model can be estimated by maximum likelihood after writing the contributions to likelihood of individuals that correspond to their history of events (whether they change jobs, whether they change location, and their wages at each period). The model is parameterized by making some assumptions on the distributions of random and matching components, supposing they follow normal distributions with mean zero and variance to be estimated. Unobserved heterogeneity is modeled through mass points with individuals having some probabilities of being of every type which enter the set of parameters to be estimated. The computation of contributions to likelihood involves the integration over the distribution of unobserved components in line with Heckman and Singer (1984).

Once estimates of the parameters $\beta_{h,c}$, $\mu_{h,j,c}$, $\phi_{h,c}$, and $\phi_{h,c,j}$ have been recovered, a variance analysis can be performed to assess the respective importance of static and dynamic local effects, as well as matching effects. Estimated parameters can also be regressed on density (or any other local variable), to evaluate how they vary with changes in the characteristics of locations. In practice, however, the numbers of locations and related parameters are usually too large for the model to be empirically tractable. An alternative is to aggregate locations by quartile of density and consider that each group is a single location in the model. Once the parameters have been estimated, it is possible to assess whether they take larger values for groups of denser locations.

Overall, structural approaches modeling jointly location choices and wages are an interesting tool for taking into account the endogeneity of workers’ mobility when assessing the impact of local determinants of agglomeration economies, whereas this has never been properly done with linear panel models. Nevertheless, it comes at the cost of making strong assumptions about the structure of the model, including parametric assumptions about random terms. More details on structural approaches in urban economics are provided by Holmes and Sieg (2015).

5.3. LOCAL DETERMINANTS OF AGGLOMERATION EFFECTS

We have already argued that the literature usually estimates the total net impact of local characteristics related to agglomeration economies rather than the magnitude of agglomeration channels (although there are some tentative exceptions that are presented in
The previous section alludes to some of these local characteristics, in particular employment density. This section details the definitions of all the characteristics that have been considered in the literature and explains to what extent they play a role in agglomeration economies. The outcome on which the impacts of local determinants of agglomeration economies are estimated often refers to a particular industry, either because data aggregated by location and industry are used or because one considers individual outcomes of firms or workers in a given industry. Considering this, two types of local characteristics may be included in the specification: those that are not specific to the industry and shape urbanization economies, and those that are specific to the industry and shape localization economies. We show successively how the size of the local market, the industrial structure of the local economy, and the composition of the local labor force can affect agglomeration economies and in turn local outcomes. We will see that in each case there can be both urbanization and localization economies.

5.3.1 Density, size, and spatial extent of agglomeration effects

Equation (5.3) shows which pure and market agglomeration mechanisms involve the size of the local economy. Depending on the mechanism, employment, population, or production can be the most relevant variable to measure local economy size. However, the correlation between these three variables is often too great to allow the identification of their respective effects separately, and one has to restrict the analysis to one of them. The results are, in general, very similar whichever variable is used. Employment is usually preferred to population, first because it better reflects the magnitude of local economic activity, and second because certain other local variables (described below) can be constructed from employment only. Production presents the disadvantage of being more subject to endogeneity issues than employment (see Section 5.4).

One usually considers models where both productivity and size are measured in a logarithmic specification because this eases interpretations, the estimated parameter being a constant elasticity. This also reduces the possibility of extreme values for the random component of the model and makes its distribution closer to the one of a normal law, which is usually used in significance tests.

Ciccone and Hall (1996) argue that the size of the local economy should be measured by the number of individuals per unit of land—that is, density. Indeed, there is usually a large heterogeneity in the spatial extent of the geographic units that are used, as these units are often based on administrative boundaries. This can also create arbitrary border effects, an issue related to what the literature calls the modifiable areal unit problem—that is, the fact that some conclusions reached by empirical works could depend on the spatial classification used in their analyses, in particular the size and shape of the spatial units. Using density should reduce issues about mismeasurement of the size of the local...
economy, which is in line with Briant et al. (2010), who show that using more consistent empirical strategies largely reduces modifiable areal unit problem concerns.

Importantly, from the theory point of view, depending on the microfoundations of pure and market local externalities entering (5.3), either local density or the level of local employment can affect the magnitude of the effects at stake. Therefore, there is no reason to restrict the specification to one variable or the other. Typically, if agglomeration gains outweigh agglomeration costs, one expects, in general, both the density and the size of the local economy to have a positive impact on local productivity. When variables are considered in a logarithmic specification, it is possible and convenient to capture the two effects using density and land area simultaneously (while leaving employment aside). The impact of density, holding land area constant, reflects the gains from increasing either the number of people in the city or the density, while the impact of land area, holding density constant, reflects the gains from increasing the spatial extent of the city (i.e., from increasing both land area and employment proportionally). In a logarithmic specification, any combination of employment and land area identifies the same fundamental parameters but one has to be careful with the interpretation of coefficients, since we have

\[ \beta \ln \text{den}_{c,t} + \mu \ln \text{area}_{c,t} = \beta \ln \text{emp}_{c,t} + \varrho \ln \text{area}_{c,t}, \quad \text{with } \varrho = \mu - \beta, \] (5.34)

where \( \text{emp}_{c,t} \) is total employment in location \( c \) at date \( t \), \( \text{area}_{c,t} \) is land area, and \( \text{den}_{c,t} = \frac{\text{emp}_{c,t}}{\text{area}_{c,t}} \) is density. This equation shows that whereas the effect of total employment for a given land area and the effect of density for a given land area correspond to the same parameter \( \beta \), the effect of land area for a given total employment \( \varrho \) is equal to the difference between the effect of land area for a given density \( \mu \) and the effect of density \( \beta \). In fact, \( \varrho \) can be negative even when agglomeration gains result from both density and spatial extent. It would be wrong to conclude that there are agglomeration costs from a negative estimated value, or no agglomeration gains from spatial extent from a nonsignificant estimated coefficient. When density and land area are used, agglomeration gains exist when any of the estimated coefficients is significantly positive.

Firms trade with distant markets, and communication exchanges occur between agents located sometimes quite far apart. A number of studies have attempted to evaluate the spatial extent of local spillovers beyond the strict limits of the local unit. These spillovers can occur for any of the urbanization and localization effects considered in this section, but most contributions in the literature consider them for local size only. Spatial econometric approaches usually consider spillovers for all the local determinants but at the cost of assuming for all of them an identical influence of distance on spillovers, and making it more difficult to deal with endogeneity issues (see Section 5.4.5.4). A flexible specification where density is considered at various distances from the worker’s or firm’s location may be envisaged. Typically, one can introduce in the specification many additional variables for density measured at 20, 50, 100, 150, 200 km, etc., from the location. However, there is sometimes not enough variation in the data to identify so
many effects of density. Therefore, some authors follow Harris (1954) and put more constraints on the impact of trade and communication costs by assuming that their impact is proportional to the inverse of distance, which typically leads to Harris’s following market potential variable:

$$\text{MP}_{c,t} = \sum_{\ell \neq c} \frac{\text{den}_{\ell,t}}{d_{c,\ell}}, \quad (5.35)$$

where $d_{c,\ell}$ is the distance between location $c$ and location $\ell$.

A number of variants for computing market potential exist since one can consider population, employment or production, in level form or in density form, as a measure of market size. Several market potential variables can be considered simultaneously (e.g., one for density and one for land area). One can also refine the way trade and communication costs are assessed by using, instead of as-the-crow-flies distances, real distances by road or real measures of trade and communication costs. Nevertheless, all the corresponding market potential variables are usually highly correlated, as illustrated by Combes and Lafourcade (2005), and the effect of only one of them can actually be identified. If density is used as the measure of the local economy size, computing market potential using densities is more consistent. Importantly, the own location is excluded from formula (5.35) for the Harris market potential to obtain an “external” market potential whose impact can usually be identified separately from the effect of the own location size. In any case, and as for the own density, one cannot say whether the impact of market potential is a market-based effect or a pure externality, and more generally which mechanism is at play.

Fujita et al. (1999) emphasize that in economic geography models based on Dixit–Stiglitz monopolistic competition, local nominal wages are an increasing function of a specific variable, called the “structural market access,” which is closely related to the Harris market potential. Intuitively Dixit–Stiglitz models suggest that Harris’s specification needs to be augmented with local price effects to take into account the role of imperfect competition that makes the price of the manufacturing good differ across locations owing to its differentiation affecting both its supply and its demand. In other words, there is now an impact of locations further away through $p_{c,t}$ in (5.3), which is captured by the structural market access variable. Note that the structural market access variable aggregates the effects of sizes of both the own and distant locations, and its computation thus requires a consistent measure of trade costs not only between locations, but also within locations. This is a concern by itself as internal trade costs are usually not available in datasets, and no fully satisfactory solution has been proposed yet to evaluate them. The most frequent strategy for coping with the issue, which is ad hoc, consists in assuming that, within a location, trade costs are proportional to the square root of land area.

Interestingly, Redding and Venables (2004) show that in a model where varieties are used as intermediate inputs, another variable very similar to the market access, called the “structural supply access,” determines the price of inputs, $r_{c,t}$, in (5.3). The greater
the supply access, the lower input prices and the higher nominal wages. Owing to the strong link to the theory of structural market access and supply access, which makes them dependent on the elasticity of substitution between varieties, for instance, no empirical counterpart can be directly constructed. Hanson (2005) was the first to suggest using also theory to relate market access to observables, and in particular local housing stocks. Redding and Venables (2004) take another route, where both market and supply accesses are estimated through a first-step trade gravity equation, and their predictors are then used in a second-step wage equation. Combes and Lafourcade (2011) show that a structural specification encompassing the role of market and supply access in agglomeration economies can also be obtained in a Cournot competition setting.

Unfortunately, structural market and supply access are highly correlated in general, precisely because circular causalities related to agglomeration effects lead households, firms, and intermediate input suppliers to choose the same locations. It is therefore difficult to identify their respective effects separately. One also has to keep in mind that the simultaneous presence of knowledge spillovers would suggest adding a standard Harris market potential in the specification in order to simultaneously take into account pure agglomeration effects coming from the local technological level and labor skills, \( A_{c,t} \) and \( s_{c,t} \). Nevertheless, it is itself highly correlated with the structural market and supply access, and only one of the three variables usually has a significant effect. When structural market access only is considered, one cannot exclude the possibility that it captures agglomeration effects other than those at play in economic geography models à la Dixit and Stiglitz for instance, even if the approach is structural.

### 5.3.2 Industrial specialization and diversity

The theory used to ground the role of location size on local productivity makes it obvious that most effects should be specific to the industry. They depend on structural parameters such as trade and communication costs, the degree of product differentiation, or the magnitude of increasing returns to scale, which are \textit{a priori} all specific to the industry. This suggests that, when a reduced form approach is used, heterogeneous effects of density, land area, and the Harris market potential across industries could be considered, as suggested in Section 5.2.1.2. In other words, the first way of considering the role of local industrial structure is to investigate industry-specific impacts of determinants of urbanization economies. At the other extreme, theory can be used to construct structural market and supply access variables that are specific to the industry, and which therefore correspond to what is referred to as localization economies. These are agglomeration

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10 Agglomeration economies increase productivity and thus attract firms. This leads to an increase in the demands for local labor and intermediate inputs as well as wages and input prices, which attract workers and input suppliers. In turn, the inflow of workers and suppliers magnifies productivity gains from agglomeration economies, attracting even more firms, and so on.
effects within the industry, the determinants of which are local characteristics that depend not only on location and date but also on industry, the triplet \( \{c, s, t\} \) with the previous notation.

Usually, authors do not construct structural market and supply access variables that are specific to the industry because necessary data are not available. Alternatively, one can consider in the specification other variables that characterize the industry within the local economy. One needs to be careful when introducing such variables related to localization economies in addition to the local economy size variables related to urbanization economies. Let us first consider the role of the size of the industry within the location. Typically, if all locations had the same share of all industries, the effect of such a variable would not be identified. A location with larger total employment would have more employment in all industries, and higher productivity in an industry could not be attributed more to higher employment in the industry than to higher total employment. Nevertheless, since localization effects seem to play no role in that case given that all locations have the same industrial composition, one may wish to attribute higher industry productivity in larger cities to higher overall employment in the local economy—that is, to urbanization effects. When the industrial share differs across locations for some industries, total and industrial employment are not proportional across locations, and one is faced with the same identification issue. Industrial employment can generate productivity gains both when it is higher because total employment at the location is higher, and when the share of the industry is higher for given total employment at the location. These two effects are captured by employment in industry \( s \) in location \( c \) at date \( t \), \( \text{emp}_{c,s,t} \), but they can be distinguished by decomposing this employment into the product of its share within the local economy, a variable often labeled specialization (or concentration in Henderson et al., 1995), and the local size of the economy: \( \text{emp}_{c,s,t} = \text{spe}_{c,s,t} \text{emp}_{c,t} \), with

\[
\text{spe}_{c,s,t} = \frac{\text{emp}_{c,s,t}}{\text{emp}_{c,t}}.
\]

To ease interpretation, Combes (2000) argues that in a specification in logarithmic form, one has to consider total employment (or employment density) next to specialization. Both these variables are expected to have a positive impact, when there are urbanization and localization economies respectively.

Because all variables are in logarithmic form, the same parameters would also be identified if total employment (or density) and industrial employment (not specialization) were considered. However, one needs again to be careful with interpretations. We have

\[
\beta \ln \text{emp}_{c,t} + \theta \ln \text{spe}_{c,s,t} = \varrho \ln \text{emp}_{c,t} + \theta \ln \text{emp}_{c,s,t}, \quad \text{with } \varrho = \beta - \theta.
\]  

This equation shows that whereas the effect of specialization for a given total employment and the effect of industrial employment for a given total employment take the same value \( \theta \), the effect of total employment for given industrial employment \( \varrho \) is equal to the difference
between the effect of total employment for a given specialization $\beta$ and the effect of industrial employment $\vartheta$. A nonsignificant estimate for $\varrho$, as obtained, for instance, by Martin et al. (2011) for France, does not imply that there is no urbanization effect, but rather means that the effect of specialization and the effect of total employment, which are usually both positive, compensate.\footnote{Earlier contributions by Glaeser et al. (1992) and Henderson et al. (1995) also consider the share and not the level of industrial employment to capture localization economies. However, because these authors study the determinants of industrial employment growth, and not the productivity level, they argue that the level of industrial employment must be introduced simultaneously, and its effect is identified because not all variables are expressed in logarithmic form. In that case, identification is assured thanks only to nonlinearities, and the results can be misleading, as emphasized by Combes (2000). We return to this point in Section 5.6.1.} Finally, note that one could consider the density of industrial employment (rather than its level), as we considered the density of total employment and not its level. We do not advise using this specification as it can lead to the same possible misinterpretations as for the industrial employment level.

Jacobs (1969) made popular the intuition that industrial diversity could be favorable as there could be cross-fertilization of ideas and transmission of innovations between industries. This has been formalized, for instance, by Duranton and Puga (2001), and many summary measures of diversity have been proposed. The most used is probably the inverse of a Herfindahl index constructed from the shares of industries within local employment:

$$\text{div}_{c,t} = \left( \sum_s \frac{\text{emp}_{c,s,t}}{\text{emp}_{c,t}} \right)^{-1}.$$

Since specialization is also introduced in the specification, interpretation is easier if one removes the own industry from the computation of $\text{div}_{c,t}$. In that case, whereas specialization relates to the role of the industry local share, diversity relates to the role of the distribution of employment over all other industries, and the two indices clearly capture two different types of mechanisms. In particular, whereas specialization is a determinant of localization economies, the Herfindahl index is a determinant of urbanization economies. Note that when the number of industries is large, it makes little difference to drop the own industry from computations, and the correlation between the Herfindahl indices obtained with and without the own industry is large.

The Herfindahl index has the bad property of taking values largely influenced by the number of units, industries here, from which it is computed. The range of variations of $\text{div}_{c,t}$ is $[1, S_{c,t}]$, where $S_{c,t}$ is the total number of industries active in location $c$ at date $t$. When detailed industrial classifications are used, $S_{c,t}$ can vary a lot across locations and the Herfindahl index reflects this number more than the actual distribution of employment between industries. For this reason, Combes et al. (2004) propose assessing the role
of industrial diversity by introducing the Herfindahl index in regressions simultaneously
with the number of locally active industries meant to capture the unevenness of the
distribution of industries over space.

Another solution consists in moving to other types of industrial diversity indices,
keeping in mind that all have weaknesses. For example, some authors propose using
the so-called Krugman index introduced by Krugman (1991a). The index is sometimes
called the Krugman specialization index, which is misleading since it actually measures an
absence of diversity, and specialization refers to another concept as we have just seen. The
Krugman index is a measure of the distance between the distributions of industry shares in
the location and at the global level:

\[
K\text{-index}_{c,t} = \sum_s \left| \frac{\text{emp}_{c,s,t}}{\text{emp}_{c,t}} - \frac{\text{emp}_{s,t}}{\text{emp}_t} \right|
\]

where \( \text{emp}_{s,t} \) is employment in industry \( s \) at the global level and \( \text{emp}_t \) is total employment.

As the Krugman index can take the value zero, it is not possible to express it in a
logarithmic form. A diversity index can be constructed as the logarithm of 1 minus
the Krugman index. Note that here diversity is maximal when the local distribution
of employment across industries is identical to the global one, while an equal share of
employment across all sectors at the local level corresponds to a less diverse situation.

Instead of using own-industry specialization and diversity variables in a specification,
one could introduce a full set of variables corresponding to specialization in each industry.
The coefficients of these variables could depend both on the that own industry and the
industry for which specialization is computed, so that one ends up with a matrix of coeff-
ficients. This way one could identify local externalities within each industry and exter-
ernals between any two industries (which would not be constrained to be symmetrical).
This would possibly correspond more to what Jacobs (1969) had in mind when she said
that a number of other industries have a positive effect on the own productivity but cer-
tainly not all of them as the diversity indices implicitly assume. The effect of specialization
at distant locations could also be assessed by introducing some Harris market potential
variables constructed using industrial employment. However, there may be a lack of var-
iation in the data to identify all the effects in these alternative specifications. Endogeneity
issues are also magnified, as explained in more detail in Section 5.4.2. All variables should
be instrumented at the same time, and this can prove to be very difficult in practice.

Finally, for given local total and industrial employment, another industrial character-
istic that may influence the magnitude of localization economies is whether local indus-
trial employment is concentrated in a small number of firms or is evenly split among many
firms. Typically large firms could be more able to internalize some of the local effects,
while small firms would have more difficulty avoiding outgoing knowledge spillovers
but could also simultaneously benefit more from spillovers. The local distribution of
firm sizes also influences the degree of competition in local input markets and in local
non-tradable good markets. With this type of intuition in mind, Glaeser et al. (1992) suggest considering the average firm size within the local industry (in fact they consider its inverse) as an additional determinant of localization economies:

\[ \text{size}_{c,s,t} = \frac{\text{emp}_{c,s,t}}{n_{c,s,t}}, \]

where \( n_{c,s,t} \) is the number of firms in industry \( s \) in location \( c \) at time \( t \). This variable can also be considered simultaneously with a Herfindahl index computed using the shares of firms within local industrial employment as proposed by Combes et al. (2004). This index captures local productive concentration and can be written as

\[ \text{pcon}_{c,s,t} = \sum_{j \in \{c,s,t\}} \left( \frac{\text{emp}_{j,t}}{\text{emp}_{c,s,t}} \right)^2, \]

where \( \text{emp}_{j,t} \) is the employment of plant \( j \). Note that the range of variations of this variable depends on the number of plants active in the local industry \( n_{c,s,t} \) and this number thus needs to be introduced simultaneously in the specification. Alternatively and more intuitively, one may prefer to introduce instead the average firm size, \( \text{size}_{c,s,t} \) (as, when expressed in logarithmic form, \( \text{spe}_{c,s,t} \), \( \text{size}_{c,s,t} \) and \( n_{c,s,t} \) are collinear).

Importantly, as \( \text{size}_{c,s,t} \) and \( \text{pcon}_{c,s,t} \) depend on the location choices of firms and their scale of production, which are directly influenced by the dependent variable (local productivity), their use leads to endogeneity concerns that are more serious than for the other local characteristics. These concerns are discussed in more detail in Section 5.4. Absent a solid instrumentation strategy, one should avoid introducing these determinants of localization economies in the specification.

### 5.3.3 Human capital externalities

Another strand of the literature has tried to identify human capital externalities. Local productivity is regressed on an indicator of local human capital, typically the share of skilled workers in local employment or the local ratio between the numbers of skilled workers and unskilled workers. Somewhat surprisingly, other local characteristics capturing agglomeration effects are most often not introduced simultaneously in the regressions except in a few cases, such as in Combes et al. (2008a). There is no underlying theoretical reason as we saw that the various agglomeration economy channels may depend on all local characteristics. Furthermore, the human capital variable may be correlated with local characteristics which are not controlled for, such as density, with which it is usually positively correlated, and therefore it does not capture the effect of human capital only.

Another difficulty arises from the fact that, beyond some human capital externalities, the estimated coefficient for the local share of skilled workers captures the imperfect
substitutability between skilled and unskilled workers. When this share increases, both
types of workers can benefit from the externalities, but unskilled workers benefit from
an extra positive effect because they become relatively less numerous, which increases
their marginal productivity. Conversely, skilled workers are negatively affected by this
substitution effect. We illustrate this identification issue by considering the following
local production function that extends our previous framework:

\[ y_{c,t} = \left( (A^H_{c,t} H_{c,t})^\rho + (A^L_{c,t} L_{c,t})^\rho \right)^{\frac{\alpha}{\rho}} K_{c,t}^{1-\alpha}, \]  

(5.37)

where \( A^j_{c,t} \) is the productivity of workers with skills \( j \) with \( j = H \) for high-skilled workers
and \( j = L \) for low-skilled workers, \( H_{c,t} \) is the number of high-skilled workers, \( L_{c,t} \) is the
number of low-skilled workers, and \( \rho \) is a parameter such that \( \rho < 1 \). The production
function is of Cobb–Douglas type in labor and other inputs, \( K_{c,t} \), and the labor compo-
nent is a constant elasticity of substitution (CES) function in high-skilled and low-skilled
workers with an elasticity of substitution equal to \(-1/(1-\rho)\). As previously, workers are
counted in terms of efficient units such that

\[ H_{c,t} = \sum_{i \in \text{high-skilled} \in \{c,t\}} s_{i,t} \ell_{i,t}, \]  

(5.38)

\[ L_{c,t} = \sum_{i \in \text{low-skilled} \in \{c,t\}} s_{i,t} \ell_{i,t}, \]  

(5.39)

with \( \ell_{i,t} \) the number of hours worked and \( s_{i,t} \) the number of efficient labor units per hour
of individual \( i \) at date \( t \). As regards the human capital externality, the ratio between the
numbers of high-skilled and low-skilled workers \( S_{c,t} = H_{c,t}/L_{c,t} \) is supposed to influence
the productivity of workers differently depending on their skills such that

\[ A^H_{c,t} = (S_{c,t})^{\gamma^H} \quad \text{and} \quad A^L_{c,t} = (S_{c,t})^{\gamma^L}, \]  

(5.40)

where \( \gamma^j \) captures the magnitude of human capital externalities for workers with skills \( j \).
For simplicity’s sake, we assume here that \( S_{c,t} \) does not affect any other agglomeration
channel—namely, the prices of output and other inputs—and that no other local char-
acteristic plays a role. It is possible to solve for wages at the individual level in the same
way we did in Section 5.2 using first-order conditions to determine the optimal use of
labor and capital. The wages of high-skilled and low-skilled workers, \( w^j_{i,t} \) for \( j = H, L \), is
obtained as

\[ w^H_{i,t} = \frac{\alpha}{(1-\alpha)^{1-\rho}} r_{c,t}^{1-1/\rho} \left( (A^H_{c,t})^\rho + (A^L_{c,t})^\rho S_{c,t}^{1-\rho} \right)^{\frac{1-\rho}{\rho}} \]  

(5.41)

\[ w^L_{i,t} = \frac{\alpha}{(1-\alpha)^{1-\rho}} r_{c,t}^{1-1/\rho} \left( (A^H_{c,t})^\rho + (A^L_{c,t})^\rho S_{c,t}^{1-\rho} \right)^{\frac{1-\rho}{\rho}} S_{c,t}^{\frac{\gamma^H}{\gamma^L}}. \]  

(5.42)
The wage elasticities with respect to $S_c,t$ for high-skilled and low-skilled workers, respectively, can be derived as

$$
\delta^H_{c,t} = \gamma^H - \phi_{c,t}(1 - \rho)(1 + \gamma^H - \gamma^L),
$$

(5.43)

$$
\delta^L_{c,t} = \gamma^L + (1 - \phi_{c,t})(1 - \rho)(1 + \gamma^H - \gamma^L),
$$

(5.44)

where $\phi_{c,t}$ is the ratio between the wage bill for high-skilled workers and the total wage bill.

Several comments can be made about these elasticities. Most importantly, they capture not only the effect of human capital externalities only but also the degree of substitution between high-skilled and low-skilled workers. Suppose that human capital externalities are present for both types of workers but their impact is greater on high-skilled workers than on low-skilled workers, $\gamma^H > \gamma^L$. In that case, the wage elasticity for low-skilled workers with respect to $S_c,t$, $\delta^L_{c,t}$, is always positive as both the externality and the substitution effects increase their productivity. By contrast, the wage elasticity for high-skilled workers, $\delta^H_{c,t}$, may be either positive or negative, as the substitution effect goes in the opposite direction from the externality effect. As acknowledged by Moretti (2004a) and Ciccone and Peri (2006), the magnitude of human capital externalities cannot be recovered from simple regressions of the logarithm of wage on $S_c,t$, even when conducted separately for high-skilled and low-skilled workers. However, the specification can be easily augmented to identify both externality and substitution effects.

Wage elasticities $\delta^H_{c,t}$ and $\delta^L_{c,t}$ in (5.43) and (5.44) vary across locations since there is no reason why the wage bill ratio $\phi_{c,t}$ should be constant over space. This suggests regressing the logarithm of wage not only on the human capital variable $S_c,t$ but also on its interaction with $\phi_{c,t}$ (while also including in the specification individual fixed effects, individual variables, and local variables affecting other types of agglomeration economies). Regressions should be run separately for high-skilled and low-skilled workers as the coefficients for the two variables are not identical for the two types of workers. According to (5.43) and (5.44), one recovers four coefficients that can be used to estimate the three parameters $\gamma^H$, $\gamma^L$, and $\rho$. The model is overidentified, which makes it possible to conduct a specification test.

An alternative approach has been proposed by Ciccone and Peri (2006), but only the average effect of human capital externalities can be recovered and not those specific to each type of worker. We present this approach in a simplified way. Ciccone and Peri (2006) first compute a local average wage weighted by the share of each worker type in local employment, $w_{c,t} = s_{c,t}w^H_{c,t} + (1 - s_{c,t})w^L_{c,t}$, with $s_{c,t}$ the share of high-skilled workers in local employment. The elasticity of this average wage with respect to $S_c,t$, holding $s_{c,t}$ constant, is given by
\[
\frac{\partial \log w_{c,t}}{\partial \log S_{c,t}} = \phi_{c,t} \gamma^H + (1 - \phi_{c,t}) \gamma^L.
\]  
(5.45)

This relationship is strictly valid for variations over time in the short run in line with the definition of the elasticity. Ciccone and Peri (2006) make the approximation that it can be used to study long-run variations of the logarithm of the wage between two dates \( t \) and \( t' \) (1970 and 1990 in their application) when the logarithm of \( S_{c,t} \) varies while holding constant the local share of workers. More precisely, they first construct a city wage index at date \( t' \) considering the local composition of workers at date \( t \):

\[
\tilde{w}_{c,t'} = s_{c,t} w^H_{c,t} + (1 - s_{c,t}) w^L_{c,t'}.
\]  
(5.46)

The log-wage difference \( \log \tilde{w}_{c,t'} - \log w_{c,t} \) is then regressed on \( \log S_{c,t'} - \log S_{c,t} \) to recover an effect supposed to be the weighted average of the effects of human capital externalities given by (5.45).

What remains unclear is the source of variations over time of \( S_{c,t'} \). Holding the share of high-skilled workers in total employment \( s_{c,t} \) constant implies that the ratio between the numbers of high-skilled and low-skilled workers, \( S_{c,t} \), is constant too. Another issue arises because the right-hand side of (5.45) is considered to be a constant coefficient, whereas it clearly varies across cities since \( \phi_{c,t} \) is specific to the city. Finally, even if the wage \( \tilde{w}_{c,t'} \) is supposed to be computed with the local composition of workers fixed to its value at date \( t \), its computation involves the wages of both skill groups at date \( t' \), \( w^L_{c,t'} \). These are not the wages that workers would have had when holding constant the composition of employment. Indeed the actual variation of wages between the two dates may have been influenced by the changes in the local composition of workers.

The use of a CES production function emphasizes the role of the elasticity of substitution between high-skilled and low-skilled workers, which can be recovered from the estimations. It is possible to conduct a similar analysis with a Cobb–Douglas production function although the elasticity of substitution is then fixed and equal to \(-1\) (in particular, we get a Cobb–Douglas specification in our setting when \( \rho \) tends to zero). In that case, local labor cost shares are constant and they are given by the Cobb–Douglas coefficients of the two groups. Nevertheless, the procedure we propose can still be applied if the coefficients of the Cobb–Douglas production function are allowed to differ across locations.

Finally, alternative variables can be considered to measure local human capital externalities, such as the share of high-skilled workers in total employment. The choice of a variable ultimately relies on the choice of an \textit{ad hoc} functional form. For instance, Moretti (2004a) and Combes et al. (2008a) regress the logarithm of individual wages on the local share of high-skilled workers in total employment, instead of the ratio between the numbers of high-skilled and low-skilled workers. Controlling for an individual fixed effect, as
well as individual and local characteristics. Even when the specification is estimated separately for high-skilled and low-skilled workers, the issue remains that only a composite of the externality effect and the substitution effect is identified. To go further and identify separately the two effects, it might be worth augmenting the specifications with the interaction of the human capital variable and the local share of high-skilled workers in the wage bill, as proposed above.

5.4. ESTIMATION STRATEGY

Now that the links between theory and empirical specifications, as well as the interpretation of estimated coefficients, have been clarified, we move to a number of empirical issues. First, we discuss the use of TFP rather than nominal wage as a measure of productivity. We then turn to endogeneity issues which emerge when estimating wage or TFP specifications. We present the solutions proposed in the literature to deal with these issues as well as their limits. We finally discuss a series of other empirical issues regarding spatial scale, functional forms, observed skills measures, and spatial lag models.

5.4.1 Wages versus TFP

So far, we have mostly considered nominal wage at the worker level as our measure of productivity. Alternatively, one may wish to use a measure at the firm level such as output value or value added. It is possible to derive a specification for such a measure that is consistent with the production function used in Section 5.2. Let us rewrite the production function at the firm level as

\[ Y_{j,t} = \frac{A_{c,t}}{\alpha^a(1 - \alpha)} \left( s_{j,t} L_{j,t} \right)^a K_{j,t}^{1-a}, \]  

(5.47)

where \( j \) denotes the firm, \( Y_{j,t} \) is the firm output, \( s_{j,t} \) corresponds to average labor skills, which are allowed to vary across firms, \( L_{j,t} \) and \( K_{j,t} \) are labor and other inputs, respectively, and \( A_{c,t} \) is the technological level supposed to be local (we could alternatively consider that it varies across firms within the same local labor market but this does not change the reasoning and we prefer to stick to a simple specification). The output value is given by \( p_{j,t} Y_{j,t} \), where \( p_{j,t} \) is the average income of the firm per unit produced (see footnote 1 for more details). The logarithm of TFP can be recovered as

\[ \ln p_{j,t} Y_{j,t} - \alpha \ln L_{j,t} - (1 - \alpha) \ln K_{j,t} = \ln \frac{p_{j,t} A_{c,t}}{\alpha^a(1 - \alpha)}^{\frac{\alpha}{1 - \alpha}}. \]  

(5.48)

Equation (5.48) for TFP is equivalent to (5.3) in logarithmic form for wage. It can be used to relate the logarithm of TFP (rather than wage) to some local characteristics, density among others, which are determinants of agglomeration economies operating through firm price \( p_{j,t} \), average labor skills \( s_{j,t} \), and local technological level \( A_{c,t} \).
If value added is reported in the dataset instead of output value, intermediate consumption can be taken into account in the production function. For instance, consider that production is Leontieff in intermediate consumption denoted $I_{j,t}$ with share in output $a$ and the Cobb–Douglas function (5.47):

$$Y_{j,t} = \min \left( \frac{I_{j,t}}{a}, \frac{A_{c,t}}{a^\alpha (1 - \alpha)} \left( s_{j,t} L_{j,t} \right)^\alpha K_{j,t}^{1 - \alpha} \right).$$

Profit maximization yields that intermediate consumption is proportional to production, and this leads to

$$\ln \left( \frac{p_{j,t} Y_{j,t} - \nu_{j,t} I_{j,t}}{\nu_{j,t}} \right) - \alpha \ln L_{j,t} - (1 - \alpha) \ln K_{j,t} = \ln \frac{p_{j,t} - a \nu_{j,t}}{\alpha^\alpha (1 - \alpha)^{1 - \alpha}},$$

where the left-hand side is TFP measured now in terms of value added, with $\nu_{j,t}$ the unit price of intermediate input. This makes it possible to conduct the analysis in a similar way as when TFP is measured in output value. The interpretation of estimated parameters is slightly different since the output price is now net of the unit cost of intermediate consumption.

There are two important differences with a wage analysis, which arise because the term that depends on local characteristics is $p_{j,t} A_{c,t} s_{j,t}^\alpha$ when one considers TFP in output value, whereas it was $\left( \frac{p_{c,t} A_{c,t}}{(s_{c,t})^{1 - \alpha}} \right)^{1/\alpha} s_{c,t}$ in the case of the nominal wage (see Equation (5.3)). The local cost of inputs other than labor does not enter the expression for output value and the determinants of agglomeration economies only capture effects related to technological level, output price, and average skills. This means that land and housing prices no longer play a role. This is clearly an advantage since we saw that the interpretation of the effect of housing price is difficult for wage regressions, and the use of this price as an explanatory variable raises serious endogeneity concerns. Moreover, the elasticity of agglomeration economies obtained from TFP regressions must be multiplied by $1/\alpha$ over the share of labor in the production function $1/\alpha$ to be directly comparable with the one obtained from wage regressions. For these two reasons, the economic interpretation of the impact of local characteristics is not the same when studying TFP or wages.

It is also important to note that wages are usually only proportional to and not equal to labor productivity by a factor that depends on the local monopsony power of the firm. This proportionality factor may be correlated with some local determinants of agglomeration economies, but one may wish to avoid considering its spatial variations as part of agglomeration effects. This may be the case when differences in local monopsony power result from differences in institutional features, which occur, for instance, between countries, and not from differences in the degree of competition in local labor markets. The use of TFP avoids making any assumption about the relationship between the local monopsony power and agglomeration economies. Finally, note that in the framework proposed here, agglomeration effects may operate at the firm level and not only at the local level as in previous sections, since the output price $p_{j,t}$ and average
labor skills $s_{j,t}$ are now specific to the firm. This may also be considered for wages, but we postpone the related discussion until Section 5.4.4.

Additionally, an empirical concern is that firm TFP, the left-hand side in (5.48), is not directly observable in datasets, and computing its value requires estimating parameter $\alpha$.\footnote{One can relax the assumption of constant returns to scale and also estimate parameters for inputs other than labor without requiring that their total share in input costs is equal to $1-\alpha$.} However, output, labor, and other inputs are simultaneously determined by the firm, which causes an endogeneity issue that can potentially bias the estimated coefficient obtained from OLS. Several methods have been proposed to estimate $\alpha$ consistently, such as a generalized method of moments (GMM) approach applied to the specification of output value in first difference (to deal with firm unobservables) using lagged values of labor and other inputs as instruments in the spirit of Arellano and Bond (1991) and followers, or sophisticated semiparametric approaches to control for unobservables which make use of additional information on investment (Olley and Pakes, 1996) or intermediate consumption (Levinsohn and Petrin, 2003). There is no consensus on a method that would be completely convincing, and robustness checks have to be conducted using several alternative approaches.

Moreover, agglomeration variables may be endogenous too for the reasons we develop in the next subsection, and this issue needs to be addressed. One way to proceed consists in applying a two-stage approach where the production function is estimated in the first stage with one of the alternative methods we have just cited and no local variable is introduced. Local-time averages of residuals are then computed and regressed in a second stage on some local characteristics. We detail below approaches to deal with the endogeneity of local characteristics in the second stage. Alternatively, local-time fixed effects can be introduced in a first stage and their estimators regressed in a second stage, in the spirit of what was proposed for individual wages (see Combes et al., 2010, for more details). This second approach has the advantage of properly controlling at the individual level for unobserved local shocks that may be correlated with firm variables. A last approach consists in estimating a specification of output value $p_{j,t}Y_{j,t}$ including both inputs and local characteristics as explanatory variables, instrumenting variables all at once. This was proposed, for instance, by Henderson (2003), who estimates an output value specification with the GMM.

### 5.4.2 Endogeneity issues

We now detail the various endogeneity problems that can occur and approaches that have been proposed to solve them. When the effect of local characteristics on individual
outcome is estimated, endogeneity can occur both at the individual level and at the local economy level. To see this, we rewrite Equation (5.6) as

$$ y_{i,t} = u_i + X_{i,t} \theta + \sum_c \left[ Z_{c,t} \gamma + \eta_{c,t} \right] 1_{\{c(i,t)=c\}} + \epsilon_{i,t}, \quad (5.51) $$

where $1_{\{c(i,t)=c\}}$ is a dummy variable equal to 1 when individual $i$ locates in $c$ at date $t$. This expression involves local effects related to observables, $Z_{c,t}$, and unobservables, $\eta_{c,t}$, on every local market, and makes explicit the location choice $1_{\{c(i,t)=c\}}$ which is made at the individual level.

There is an endogeneity issue at the local level when a variable in $Z_{c,t}$, density for instance, is correlated with the local random component $\eta_{c,t}$. This can happen because of reverse causality or the existence of some missing local variables that affect directly both density and wages. Reverse causality is an issue when higher local average wages attract workers, as this increases the quantity of local labor and thus density. In that case, one expects a positive bias in the estimated coefficient of density (provided that density has a positive effect on wages owing to agglomeration economies).

There is a missing variable problem when, for instance, some local amenities not included in $Z_{c,t}$ are captured by the local random term and they determine both local density and wages. Productive amenities such as airports, transport infrastructures, and universities increase productivity and attract workers, which makes the density increase. In that case, a positive bias in the estimated coefficient of density is also expected. In line with Roback (1982), consumption amenities such as cultural heritage or social life increase the attractiveness of some locations for workers and thus make density higher. Such amenities do not have any direct effect on productivity, but the increase in housing demand they induce makes land more expensive. As a result, local firms use less land relatively to labor, and this decreases labor productivity when land and labor are imperfect substitutes. This causes a negative bias in the estimated coefficient of density since density is positively correlated with missing variables that decrease productivity.

Finally, the unobserved local term captures among other things the average of individual wage shocks at the local level. This average may depend on density as workers in denser local markets may benefit from better wage offers owing, for instance, to better matching. One may consider that matching effects are part of agglomeration economies and then there is no endogeneity issue. Alternatively, one may be interested solely in the effects of knowledge spillovers and market access for goods captured by density, in which case there is an expected positive bias in the estimated effect of density owing to the contamination by matching mechanisms.

Endogeneity concerns can also arise at the individual level when location dummies $1_{\{c(i,t)=c\}}$ are correlated with the individual error term $\epsilon_{i,t}$. This occurs when workers sort across locations according to individual characteristics not controlled for in the specification such as some of their unobserved abilities. We emphasize in Section 5.2.1 the
importance of considering individual fixed effects $u_t$ to capture the role of any individual characteristic constant over time. However, workers might still sort across space according to some time-varying unobserved characteristics entering $\epsilon_{i,t}$.

Endogeneity at the individual level also emerges when workers’ location choices depend on the exact wage that they get in some local markets, typically when they receive job offers associated with known wages. Notice that this type of bias is closely related to matching mechanisms although there is here an individual arbitrage between locations, whereas the matching effects mentioned earlier rather refer to a better average situation of workers within some local markets. Importantly, as long as individual location decisions depend only on the explanatory terms introduced in the specification, which can go as far as the individual fixed effect, some time-varying individual characteristics such as age, and a location-time fixed effect, there is no endogeneity bias. Combes et al. (2011) detail these endogeneity concerns.

5.4.3 Dealing with endogenous local determinants

The literature has mostly addressed endogeneity issues at the local level using several alternative strategies. A simple approach consists in including time-invariant local fixed effects in specifications estimated on panel data to deal with missing local variables that are constant over time. Some authors instrument the local determinants of agglomeration economies using additional variables such as local historical or geological variables. Estimations with GMM, where lagged values of local determinants themselves are used for instrumentation, have been considered too but their validity relies on stronger assumptions. Finally, other articles exploit natural experiments involving a shock on local characteristics related to agglomeration economies. This section examines these various strategies. The reader may also refer to the chapter by Baum-Snow and Ferreira (2015) for additional considerations on causality.

By contrast, we are not aware of nonstructural contributions dealing with endogeneity at the individual level, to the extent that some concerns would remain in the most complete specifications including both individual and location-time fixed effects. Structural approaches considering dynamic frameworks like those presented in Section 5.2.4 are clearly a natural way to consider endogenous individual location choices.

5.4.3.1 Local fixed effects

One reason why local determinants of agglomeration economies can be endogenous is that some missing variables determine them simultaneously with the local outcome. In particular, this is the case when there are missing amenities that affect both local productivity and the local population. A strategy for coping with this issue when panel data are at hand is to include time-invariant local fixed effects in the estimated specification. There are several reasons why this strategy may not work well. First, it does not deal with missing variables that evolve over time: for instance, new airports or stations are built or
improved over the years depending precisely on their local demand and the performance
of local firms and workers. Second, time-invariant local fixed effects do not help in solv-
ing the endogeneity issue due to reverse causality, such that higher expected wages or
productivity in a location attract more firms and workers. Third, identification relies
on time variations of the local outcome and local determinants of agglomeration econ-
omies only. If the variations of local determinants are mismeasured, which is likely to
happen as local determinants are often computed from samples of limited size and var-
iations are often considered only in the short run because the time span of panels is, in
general, quite short, estimated effects can be highly biased because of measurement errors.
This kind of problem can be particularly important for local characteristics which vary
little across time—for instance, because the economy is close to a spatial equilibrium. Their effect is difficult to identify separately from the role of permanent characteristics
that affect productivity without being related to agglomeration economies. Nevertheless,
one can try to identify their effect by using an instrumentation strategy applied to a spec-
ification in level.

5.4.3.2 Instrumentation with historical and geological variables
An alternative strategy for coping with endogeneity at the local level consists in finding
instruments that deal with both reverse causality and missing amenities. Instruments
should verify two conditions: relevance and exogeneity. Instruments are relevant when
they are correlated with the instrumented variables \( Z_{c,t} \), and they are exogenous when
they are not correlated with the aggregate random term \( \eta_{c,t} \). Two necessary conditions
for exogeneity are that instruments are not correlated with missing local variables and not
determined by the outcome.

Several sets of instruments have been proposed. The first one consists of historical
instruments and more particularly long lagged values of variables measuring agglomera-
tion economies (see Ciccone and Hall, 1996; Combes et al., 2008a). Historical values of
population or density are usually considered to be relevant because local housing stock,
office buildings, and factories last over time and create inertia in the local population and
economic activity. If the lags are long enough (say, 150 years), instruments are believed to
be exogenous because of changes in the type of economic activities (agriculture to
manufacturing then services) and sometimes wars that reshaped the area under study.
Local outcomes today are therefore unlikely to be related to components of local out-
comes a long time ago that probably affected the historical population. However, there
are local permanent characteristics that may have affected past location choices and still
affect local productivity today, such as the centrality of the location in the country, a suit-
able climate, or geographical features such as access to the coast or the presence of a large

\[ \text{This does not necessarily mean that they do not shape the magnitude of agglomeration economies.} \]
river. If these features are not properly controlled for in regressions, the local historical population may not be exogenous.

The second set of instruments consists of geological variables related to the subsoil of the location (see Rosenthal and Strange, 2008; Combes et al., 2010). These variables typically describe soil composition, depth to rock, water capacity, soil erodibility, and seismic and landslide hazard. They are believed to be relevant because the characteristics of soils were important for agriculture centuries ago, even millennia ago, and manufacturing and services have since developed where human settlements were already located. They are believed to be exogenous because people may have had only a negligible effect on soil and geology, and these do not influence the productivity of most modern activities.

Some authors argue that consumption amenities can be used as instruments since according to the Roback (1982) model, they are relevant because they attract workers and therefore determine the local population, and they are exogenous as they would not directly affect local productivity. This is not certain, however, because the inflow of workers puts pressure on local land markets, which in turn gives firms incentives to substitute labor for land in the production process, as we have argued above. As a result, productivity can be affected and consumption amenities are not exogenous. Therefore, we advocate using consumption amenities as control variables rather than as instruments when they are available in datasets.

In practice, historical variables are usually found to be extremely relevant instruments, in particular past population, indicating major inertia in the distribution of population over space. Geological variables are also found to be relevant but to a lesser extent, and their power to explain instrumented variables is not very high. Exogeneity can only be properly tested by confronting different sets of instruments with each other, under the assumption that at least one set of instruments is valid. Indeed, the Sargan exogeneity test implicitly compares the estimators obtained with all the alternative combinations of instruments. The test is passed when these estimators are not significantly different from each other. One has to make the assumption that at least one set of instruments is valid such that the instrumental variable estimator obtained with that set of instruments is consistent. Otherwise, the test could be passed with all instruments being invalid and the instrumental variable estimators obtained with the different combinations of instruments all converging to the same wrong value. As an implication, making an exogeneity test using only very similar instruments (e.g., population 150, 160, and 180 years ago) is not appropriate since the estimated coefficient could be biased the same way in all cases and the overidentification test would then not reject exogeneity. An overidentification test using different types of instruments which are not of the same nature is more meaningful. For instance, it is likely that historical and geological variables satisfy this property: even if geology initially influenced people’s location choices a very long time ago, many other factors have also determined the distribution of the population across space since
then and make the local historical population a century ago less related to local geology. Some authors, such as Stock and Yogo (2005), have started to develop weak instrument tests that assess whether different instruments have enough explanatory power of their own and can be used together to conduct meaningful overidentification tests. Such tests should be reported systematically.

Lastly, since Imbens and Angrist (1994), it has been emphasized that instrumentation identifies a local average treatment effect only—that is, an effect specific to the instruments chosen, and not necessarily the average treatment effect. Some differences between the two occur when instruments differently weight observations, locations here, in regressions. For instance, the current total population may be instrumented with the historical urban population rather than the historical total population because of data availability issues (see Combes et al., 2008a). In that case, the instrument is more relevant for locations with a current population which is large. Indeed, the instrument takes the value zero for all locations with no urban population a long time ago, and varies for locations of large size with positive urban population a while ago. Overall, this also argues for considering different sets of instruments, testing whether they lead to similar estimates as mentioned earlier, and keeping in mind the arguments developed here for the interpretation of different estimates.

5.4.3.3 Generalized method of moments

A third strategy that has been used to cope with endogeneity issues when having panel data is to use a GMM approach to estimate the specification in first difference while using lagged values of variables as instruments, both in level and in first difference. Two main types of specification involving determinants of agglomeration economies have been estimated that way: dynamic specifications of employment at the city–industry level (Henderson, 1997; Combes et al., 2004) and static or dynamic specifications of TFP or wages (Henderson, 2003; Mion, 2004; Graham et al., 2010; Martin et al., 2011). As detailed in Section 5.4.1, articles on productivity typically specify in logarithmic form the firm production or value added as a function of labor, other inputs (usually physical capital), local variables determining agglomeration economies, possibly earlier in time, and a firm fixed effect capturing time-invariant firm and local effects. The specification is rewritten in first difference between \( t \) and \( t - 1 \) to eliminate the firm fixed effect. A similar strategy is implemented at the local level when no firm-level data are available. When the effects of all variables are estimated in a single step, first differences of labor, capital, and local variables are simultaneously instrumented by their past values in \( t - k \), with \( k \geq 2 \), and/or by their past levels. When a two-step strategy is implemented such that a TFP specification is first estimated and then either local-time averages of residuals or local-time fixed effects are regressed on local characteristics in a second step, the same kind of instrumentation can be implemented at each step. Lastly, an alternative approach has been proposed by Graham et al. (2010), who specify a vector autoregressive model.
where the first equation relates current labor productivity to its past values and those of local characteristics, and additional equations relate current values of local characteristics to their past values and those of productivity. All equations are simultaneously estimated with dynamic GMM, and Granger tests are used to assess the presence of reverse causality between productivity and local characteristics.

As detailed in Section 5.6.1, studies of employment dynamics specify city–industry employment at time $t$ as a function of its lags at times $t - 1, \ldots, t - k$, with $k \geq 1$, other time-varying local characteristics, and a city–industry fixed effect. Lags of the dependent variable capture both mean-reversion and agglomeration size effects as argued by Combes et al. (2004), while local characteristics capture other types of agglomeration economies. Again the specification is rewritten in first difference between $t$ and $t - 1$, and first-differenced lags of city–industry population are instrumented with past levels before $t - k$, with $k \geq 3$, and other local variables with their value in $t - 2$.

The approach is valid when the two conditions of relevance and exogeneity of instruments are verified. The relevance of instruments is usually not an issue as there is some inertia in local variables and the time span is usually short (a couple of decades at most). Exogeneity can be the most problematic issue. Take the example of city–industry employment $y_{z,s,t}$ written in first difference $\Delta y_{z,s,t} = y_{z,s,t} - y_{z,s,t-1}$ and regressed on its lagged value $\Delta y_{z,s,t-1}$. The practice consists in instrumenting $\Delta y_{z,s,t-1}$ with the past level $\Delta y_{z,s,t-2}$. The exogeneity condition is not verified if the shock in the outcome specification—say, $\nu_{z,s,t}$—is serially correlated. This causes the shock in first difference $\Delta \nu_{z,s,t}$ to be correlated with the past employment level $y_{z,s,t-2}$. For instance, industry–city shocks probably last several years, and the exogeneity condition is thus unlikely to hold. One may wish to use as instruments more remote past levels $y_{z,s,t-k}$, with $k$ much larger than 2 to attenuate the bias, but this strategy will also probably fail when the data span 15 or 20 years only. A common practice for testing the validity of the exogeneity condition is to use several lags of the outcome before $t - 1$ as instruments and conduct a Sargan overidentification exogeneity test. This practice is dubious since the test relies on instruments all from the same source, the dependent variable itself. As suggested earlier, variables of a different kind should be used as instruments together with past values of the outcome for the overidentification test to be meaningful. Overall, we advise against relying on approaches based on GMM with lagged values as instruments to identify the role of local determinants on local outcomes.

5.4.3.4 Natural experiments

Another strategy for dealing with an endogenous local determinant consists in exploiting the context of a natural experiment that has induced a sizeable localized shock on that determinant which is not directly related to the outcome variable. The general idea of the approach is to evaluate the effect of the variable from the comparison of the average

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14 Note that there are also specific interpretation issues that are discussed in Section 5.6.1.
variation in outcome in places which have experienced the shock with the average variation in outcome in comparable places which have not experienced the shock. Sometimes, the quantitative value of the shock is not known, and only its effect (i.e., the change in the agglomeration determinant times the coefficient of the variable) is identified. To see this, consider the aggregate model:

$$\beta_{c,t} = Z_{c,t} \gamma + \theta_c + \eta_{c,t},$$

(5.52)

where $\beta_{c,t}$ is a local outcome such as a location–time fixed effect estimated in the first step on individual data, $Z_{c,t}$ includes the local characteristics that determine agglomeration effects, and $\theta_c$ is a location fixed effect capturing among others the role of local time-invariant characteristics. A common practice is to make the city fixed effect disappear by rewriting the model in first difference:

$$\Delta \beta_{c,t} = \Delta Z_{c,t} \gamma + \Delta \eta_{c,t}.$$  

(5.53)

Beyond the fact that controlling for time-invariant local effects can raise measurement issues as discussed above, another problem is that the variation in local variable $\Delta Z_{c,t}$ may be correlated with the variation in residual $\Delta \eta_{c,t}$ because of unobserved time-varying amenities or reverse causality. This problem can be circumvented in the case of a natural experiment. Consider that there is a subset denoted tr (for “treated”) of $N_{tr}$ locations experiencing a shock, or “treatment,” that affects the local variable from date $\tau$ onward such that $Z_{c,t} = \bar{Z}_{c,t} + \phi 1_{t \geq \tau}$, where $\bar{Z}_{c,t}$ is the value of the local variable in the absence of the shock, and $1_{t \geq \tau}$ is a dummy for being affected by the shock. Consider also that there is a subset denoted ntr (for “nontreated”) of $N_{ntr}$ locations that do not experience any shock from date $\tau$ onward. The difference–in–differences estimator of the effect of the shock between dates $\tau - 1$ and $\tau$ is the difference between the average outcomes of the treated and nontreated locations, given by

$$\hat{\phi \gamma} = \frac{1}{N_{tr}} \sum_{c \in tr} \Delta \beta_{c,t} - \frac{1}{N_{ntr}} \sum_{c \in ntr} \Delta \beta_{c,t}.$$  

(5.54)

This estimator converges to the true effect of the shock $\phi \gamma$ provided that the numbers of locations in the treated and nontreated groups tend to infinity and that there is similarity between treated and nontreated locations in terms of the growth of local variables and shocks in the absence of treatment:

$$E[\Delta \bar{Z}_{c,t} | c \in tr] = E[\Delta \bar{Z}_{c,t} | c \in ntr] \text{ and } E[\Delta \eta_{c,t} | c \in tr] = E[\Delta \eta_{c,t} | c \in ntr].$$  

(5.55)

Note that when the value of the shock $\phi$ is observed, it is then possible to recover the marginal impact of the local variable, $\gamma$.

The challenge when using a natural experiment is to find a control group which is similar to the treated group such that locations in the two groups would have experienced similar variations in local characteristics absent the shock and such that their unobserved
characteristics would have evolved similarly (condition 5.55). If this is not the case, strategies based on matching can lead to further comparability between the two groups, or regression discontinuity approaches can be used to identify the effect of treatment locally.

A limitation when exploiting a natural experiment, in particular when using these two complementary strategies, is that external validity is not certain. The shock may be specific to a particular context, and locations in the treated and nontreated groups may not be representative of the overall set of cities. Therefore, the estimator obtained from the natural experiment may not correspond to the average effect of the shock for the whole set of cities.

Some articles such as those by Hanson (1997), Redding and Sturm (2008), and Greenstone et al. (2010) have achieved some success in using natural experiments when studying the effect of local determinants of agglomeration economies on outcomes of firms. We detail their strategies and conclusions in Section 5.5.4 concerning the results obtained in the literature.

5.4.4 Tackling the role of firm characteristics

We have so far considered a production function where the TFP of firms is influenced by location but not by any intrinsic characteristic of firms. It is possible to argue though that firms differ in their management teams, with some being more efficient than others, and this creates some heterogeneity in productivity. Moreover, there can be some sorting of firms across space depending on management efficiency—for instance, with firms with the better management teams being created in larger locations. International trade models with heterogeneous firms also imply that only the most able firms can survive in larger markets (see, e.g., Melitz and Ottaviano, 2008) owing to competition effects that are not related to agglomeration gains. If such firm selection effects exist and firm heterogeneity is not properly taken into account, estimated effects of local characteristics such as city size are biased.

Heterogeneity in firm productivity can be taken into account in the specifications of firm output value derived in Section 5.4.1 by making the TFP specific to the firm rather than to the area in the same way we did for output and input prices. A possible way of taking into account firm heterogeneity in wage regressions is to include firm fixed effects in wage specifications such as (5.6), which becomes

\[ y_{i,t} = u_i + v_{j(i)} + X_{i,t} \theta + Z_{e(i,t),t} \gamma + \eta_{j(i),t} + \epsilon_{i,t}, \]  

where \( j(i) \) is the firm of individual \( i \) and \( v_j \) is a firm fixed effect. Two estimation issues need to be discussed. First, it is never possible to control properly for all productive amenities by including explanatory variables at the local level in the regression. Firm fixed effects are thus bound to capture the effect of any omitted local variable not varying over time, and they thus cannot simply be interpreted as firm effects. From a theoretical point of
view, this is crucial when trying to interpret the correlation between worker and firm fixed effects. This correlation does not necessarily capture the effect of a worker–firm match, but could also capture the effect of a worker–area match with some sorting of firms depending on unobserved local characteristics.

Second, it is difficult, if not impossible, to take into account time-varying local unobservables in the computation of standard errors. Indeed, the two-step approach proposed in Section 5.2.1.1 cannot be applied since local-time fixed effects cannot be identified separately from firm fixed effects. This occurs because firms do not move across space and the local average of their effects is then confounded with local effects. The larger the unobserved local effects, the larger the possible bias in standard errors derived from least squares estimation. Some determinants of agglomeration economies could appear to have a significant effect, whereas they would not have a significant effect if unobserved local effects were properly considered.

An alternative approach consists in introducing proxies in the specification for firm characteristics related, for instance, to management or organization, instead of firm fixed effects. One can then apply the two-stage approach to properly take into account local unobservables in the computation of standard errors. Such proxies are hard to find, however, and when estimations are conducted in a single step, firm variables may also capture the effects of local unobservables, which can be due to agglomeration economies. In particular, some authors use firm size as a regressor and do not control for local-time fixed effects (see, e.g., Mion and Naticchioni, 2009). Firm size may capture not only firm productivity but also agglomeration gains from increasing returns to scale due to a better market access. One may try to distinguish firm productivity by rather using firm size centered with respect to its local average. Another clear limitation to controlling for firm size is that it depends on time-dependent shocks that also affect wages. This causes a simultaneity bias in the estimations. Note that all these issues are common to most firm observed characteristics.

Firm heterogeneity can itself be used to distinguish agglomeration effects from competition effects as proposed by Combes et al. (2012b). That article considers a value-added specification where only labor, capital, and skills are introduced. Firm TFP is measured with the residual computed at the firm level. An economic geography model with heterogeneous firms shows that a test for the presence of agglomeration and competition effects can then be conducted by comparing firms’ TFP distributions in small and large cities. If the distribution in large cities is a right-shifted version of the distribution in small cities, all firms in large cities benefit from agglomeration effects. If the distribution in large cities is rather a left-truncated version of the distribution in small cities, competition is fiercer in large cities, which leads to a larger share of the least productive firms being unable to survive there. Estimations from French data taking into account both the right-shift and left-truncation transformations support the presence of agglomeration effects but not the presence of competition effects.
5.4.5 Other empirical issues

5.4.5.1 Spatial scale

Articles differ in the spatial scale at which the impact of local determinants is measured. There are two main reasons for that: there is no real consensus on the spatial scope at which each agglomeration mechanism takes place, and any local determinant captures, in general, several mechanisms, the relative intensity of which can differ across spatial scales. Theory makes it clear that the spatial scope of agglomeration effects depends on their type. For instance, whereas technological spillovers often require face-to-face contacts, other agglomeration effects such as input–output linkages could take place at a larger scale such as the region. The issue is in fact more complicated as changing the size of the spatial units usually involves changing their shape, and both changes create modifiable areal unit problems, which were mentioned above. However, Briant et al. (2010) show in the particular case of the effect of local density on individual wages that changing shapes is of secondary importance for the estimates compared with taking into account individual unobserved heterogeneity with individual fixed effects. Changing the size of units has a slightly larger effect but an order of magnitude lower than biases related to misspecifications. Hence, choosing the right specification when measuring the impact of local characteristics appears to be more important than choosing the right spatial units. In practice, differences in estimates when the spatial scale varies can give a clue to the various agglomeration mechanisms at play at the various scales. Knowledge spillovers, human capital externalities, and matching effects should be the most prevalent agglomeration forces at short distances—say, within cities or even neighborhoods. By contrast, the effects of market access for both final and intermediate goods emphasized by economic geography models should be the main agglomeration forces driving differences in local outcomes at a larger scale, such as the region.

Keeping these remarks in mind, some articles have tried to evaluate the spatial extent of the impacts of local characteristics, and the scale at which they are the strongest. A common approach is to consider an individual or location defined at a fine scale and to draw rings with increasing radius around it. The value of any local characteristic can be computed using only locations within each ring separately. The spatial extent of agglomeration effects related to the local characteristic is then tested by including within the same specification its values for all rings. Among the first studies using this strategy on US data, Rosenthal and Strange (2003) were aiming at explaining local firm creation and Desmet and Fafchamps (2005) were aiming at explaining local employment. In Rosenthal and Strange (2003), local activity is considered to be located within 1 mile of the zip code centroid, and three rings around it are considered. The first ring contains activities located between 1 and 5 miles, the second between 5 and 10 miles, and the third between 10 and 15 miles. In Desmet and Fafchamps (2005), the first ring contains activities located between 0 and 5 km from the county, the second between 5 and
10 km, the third between 10 and 20 km, and so on every 10 km up to 100 km. Agglomeration effects are considered to attenuate with distance when a decreasing impact is obtained the further away the rings are from the location. The spatial scope of agglomeration effects is given by the distance after which the local characteristic does not have a significant effect anymore. It can happen that agglomeration effects first increase with distance before decreasing. The turning point gives the spatial scale at which they are the strongest.

5.4.5.2 Measures of observed skills

Individual skills are not evenly distributed across locations. Combes et al. (2008a) show, for instance, that individual fixed effects and location fixed effects obtained from the estimation of a wage equation from French data are largely positively correlated. The uneven distribution of traits, intelligence, and education is documented for the United States by Bacolod et al. (2010). Bacolod et al. (2009a) show that city size is positively correlated with cognitive and people skills, but is negatively correlated with motor skills and physical strength. Bacolod et al. (2009b) also provide evidence that workers in the right tail of the people skill distribution in large cities have higher skills than those in small cities, and that the least skilled are less skilled in large cities than in small cities. This is in line with Combes et al. (2012c), who measure skills with individual fixed effects, and Eeckhout et al. (2014), who measure skills with diplomas. Both articles conclude that there is a distribution of skills with larger variance and shifted to the right in larger cities. As discussed above, skills have two specific roles to play when estimating the effects of agglomeration economies on an economic outcome. First, skills can themselves be one of the determinants of agglomeration economies. Second, there can be some sorting of skills across locations, and it is important to control for this to avoid biases when measuring the impact of local characteristics related to agglomeration economies.

As mentioned above, it is possible to keep the form of skills unspecified in wage equations by introducing individual fixed effects when using panel data. This has the two drawbacks that one has to rely on mobile individuals for identification, and individual characteristics that matter for productivity cannot be identified. This strategy cannot be implemented when panel data are not available, but various measures of observed skills can be used at the cost of not controlling for unobservable individual characteristics. There is a long tradition in labor economics of using obvious measures such as diplomas or years of schooling, and we mention Duranton and Monastiriotis (2002) for the United Kingdom and Wheaton and Lewis (2002) for the United States as two early attempts that followed that route. It is also tempting to use the socioprofessional category, “occupation,” which is often recorded in labor force surveys. It captures the exact job done by workers and part of the effects of the past career, and may thus be considered as a measure that should be more correlated with current skills than education.
On the other hand, there is an endogeneity concern since occupation is attached to the job and is jointly determined with the wage. There is no obvious solution for this endogeneity issue, except to use a more structural approach that would jointly model wages and occupational choice.

An interesting alternative is to introduce measures of traits and intelligence. Bacolod et al. (2009a, 2010) build on psychological approaches and use detailed occupations from the Dictionary of Occupational Titles to construct such measures using information on job requirements and principal component analysis. They end up with four indices related to cognitive skills, people skills, motor skills, and physical strength. It is possible to assess how individuals score on these four dimensions from the job they have just after completion of their education. Bacolod et al. (2009a), in line with studies in labor economics, also use the Armed Forces Qualification Test, the Rotter index, and the SAT scores for college admission in the United States to control further for worker ability and better capture the quality of education. Some attempts have also been made to use other indirect proxies to control for skills. Fu and Ross (2013) use dummies for locations of residence, with the idea that the choice of a residential location is based on tastes, which are themselves likely to be partially correlated with individual productivity. At the same time, the location of residence can be endogenous as it is chosen while taking into account the location of the workplace and the wage.

5.4.5.3 Functional form and decreasing returns to agglomeration
Most articles estimate a log-linear relationship between local outcome and local characteristics. When the elasticity is between 0 and 1, this corresponds to a function in levels which is concave but nondecreasing. This is an approximation and there is no theoretical reason why the relationship between the logarithm of local outcome and the logarithm of local determinants should be linear. Theory rather predicts that the marginal returns to agglomeration should decrease with city size, for instance, because local congestion increases as the city grows. Gains from human capital externalities from the first skilled workers in a location may be rather large, but the more numerous skilled workers are, the lower the marginal gain from one additional skilled worker. A similar line of argument may hold for most technological spillovers. Economic geography models with variable markups and strategic interactions, such as the one proposed by Combes and Lafourcade (2011), do present the feature that in the short run gains from agglomeration dominate costs as long as the asymmetry between locations is not too large, but further agglomeration in the largest locations can lead to a reverse result. As illustrated in Section 5.2.1, local productivity is negatively affected through some channels, such as the increase of land prices with the population, whatever the city size. This kind of effect can become dominant when cities are very large. More generally, one expects gains from agglomeration to increase and be concave with a steep slope at the beginning, and costs to increase and be convex with an initial slope close to zero. In that case, the difference between the
two is concave and bell shaped. The relationship between the determinants of agglomeration economies, in particular population size, and local outcomes is then expected to decrease beyond some threshold.

The simplest way to test for the presence of non-log-linear relationships consists in augmenting the specification with the square of the logarithm of local determinants, but more complex functions of local determinants such as higher-order polynomials can also be used. For instance, Au and Henderson (2006b) regress the value added of a city on a nonlinear specification of its size using a sample of Chinese cities. Graham (2007) develops an original strategy based on a translog production function and two measures of effective urban density. Effective density is computed as a market potential function using either straight-line distances or generalized transport costs that consider road traffic congestion. Corresponding measures are used to estimate the magnitude of diminishing returns from agglomeration—that is, the concave impact of density, and its link with transport congestion. Note finally that the presence of concave effects can be studied for other local characteristics and outcomes. For instance, Martin et al. (2011) quantify the nonlinear effect of specialization on firm value added. Overall, the literature is rather suggestive of diminishing returns to agglomeration (see Section 5.5). In practice, when estimating a nonlinear effect, one should always check that the support of observations covers the whole interval where the nonlinear effect is interpreted. Otherwise, interpretation is based on extrapolation rather than an empirical feature of the data.

5.4.5.4 Spatial lag models

There is a strand in spatial econometrics considering that spatial lag models can be informative on the effect of local determinants of agglomeration economies. In these models, a local outcome is regressed on a weighted average of neighbors’ outcomes or on a weighted average of neighbors’ exogenous characteristics, or both, where weights decrease with distance, and the spatial correlation of residuals is sometimes taken into account (see Lesage and Pace, 2009, for details). The weighted averages of neighbors’ outcomes or characteristics are considered to capture agglomeration effects. It is now standard to estimate this kind of model with maximum likelihood. An important limitation to this approach is that the model is identified as a result of parametric assumptions, in particular as regards the impact of space on agglomeration effects and the distribution of residuals.

As emphasized by Gibbons and Overman (2012), spatial specifications face a reflection problem à la Manski, which is known to be very difficult to deal with properly. For instance, consider the case where individual wage is regressed on neighbors’ composition in terms of diplomas because one expects human capital externalities to spill over the boundaries of spatial units. This composition may be endogenous as highly educated workers may be attracted to the vicinity of workers earning high wages, in particular because they can finance local public goods.
The reflection problem is usually addressed in spatial econometrics by using spatial lags of higher order as instruments, in the spirit of panel estimation strategies which consist in instrumenting variables by long time lags of their first difference. However, this kind of approach relies on assumptions on the extent of spatial effects. Indeed, one needs to assume that these effects involve only close neighbors, whereas more distant neighbors do not have any direct effect on the outcome, which is the reason why they can be used to construct instruments verifying the exclusion restriction. Nevertheless, it is possible that neighbors located further away also directly affect the outcome, and the instruments are thus invalid. An additional issue is that the validity of instruments cannot be properly assessed using an overidentification test as all instruments are built from the same underlying variables, computed at various distances but fundamentally affected by common shocks.

Overall, the main identification concern remains: one needs to find a strategy to identify the effect of local determinants of agglomeration economies using a natural experiment or valid instruments, and unfortunately spatial lag models are of no help for that. Corrado and Fingleton (2012), Gibbons and Overman (2012), McMillen (2012), and Gibbons et al. (2015) propose a more thorough discussion of the concerns regarding spatial econometrics.

5.5. MAGNITUDES FOR THE EFFECTS OF LOCAL DETERMINANTS OF PRODUCTIVITY

Previous sections presented relevant strategies that could be used to estimate the impact of local determinants of agglomeration economies, and clarified the underlying econometric assumptions and interpretations. Contributions in the literature rarely adopt exactly these empirical strategies and often use variants. This makes it rather difficult to compare their results and it can sometimes explain discrepancies in their conclusions. We survey these contributions as well as their results, and try to emphasize the main assumptions that are made in the estimation strategies in light of previous sections. We first present the large body of articles on the average impact of density on productivity. We then turn to the scarce articles estimating heterogeneous effects across city sizes, workers’ skills, or industries. We also review contributions on the spatial extent of agglomeration effects, which include some using natural experiments to address endogeneity issues. Results on specialization, diversity, and human capital externalities are then described, and a final section is devoted to the results obtained for developing countries.

5.5.1 Economies of density

It is now established that the local density of economic activities increases the productivity of firms and workers. This conclusion emerges from a large number of studies mentioned below. Some of them use aggregate data and regress the logarithm of regional
wage or TFP on the current logarithm of employment or population density. Typical values for the elasticity when controlling for some local variables but disregarding both reverse causality and individual unobserved heterogeneity to deal with spatial sorting are between 0.04 and 0.07. The estimates are rather diverse because different countries, industries, or periods of time are considered, as emphasized by Melo et al. (2009). Some studies estimate even larger magnitudes but usually use fewer control variables. The elasticity range 0.04–0.07 implies that when the density is twice as great, productivity is between 3 and 5% higher. Density in the last decile in developed countries is usually at least two to three times greater than in the first decile, and may even be 15 times greater (when considering European regions, or regions within some countries). The productivity gap associated with the interdecile difference may be as large as 20%.

Correcting for aggregate endogeneity is generally found to have a small effect on elasticities. Instrumentation decreases them by 10–20%, and sometimes leaves the estimates unaffected or may even make them increase slightly. By contrast, using individual data and introducing individual fixed effects to control for spatial selection can change the estimated elasticity of productivity with respect to density much more. This elasticity can be divided by a factor larger than 2 and can reach a value typically around 0.02. As detailed below, depending on the country and on the precise method used to control for skills (individual fixed effect or observed skills variables), the magnitude of the sorting bias can differ significantly.

Turning to specific estimates, the two benchmark studies using aggregate data for the United States—those of Ciccone and Hall (1996) and Rosenthal and Strange (2008) for the years 1988 and 2000, respectively—report similar values for the elasticity of productivity with respect to density, at around 0.04–0.05. The first study uses historical variables (e.g., lagged population, lagged population density, or lagged railroad network) as instruments for density and the second study uses geological variables (seismic and landslide hazard, percentage of area underlain sedimentary rock). In both cases, instrumentation barely affects estimates, and if anything, slightly increases the elasticity of productivity with respect to density.

Some studies attempt to estimate this elasticity for European regions. Ciccone (2002) replicates Ciccone and Hall (1996) on NUTS 3 regions in France, Germany, Italy, Spain, and the United Kingdom. His main instrument is land area, which is not very convincing since we argue in Section 5.3.1 that land area can have a direct effect on productivity. He gets an elasticity of around 0.05 for 1992. Interestingly, he also finds no evidence that agglomeration effects significantly differ across countries. Two more recent studies extend the set of countries considered in the analysis, although at the cost of using larger spatial units. Brülhart and Mathys (2008) consider 245 NUTS 2 regions in 20 western and eastern European countries, with data on the 1980–2003 period for western European countries but only on the 1990–2003 period for eastern European countries, and eight broad industries covering both manufacturing and financial services. They consider first
differences and resort to GMM to deal with endogeneity issues in the estimations. Unfortunately, the results seem to differ widely depending on the empirical strategy they adopt. Still, they estimate quite large agglomeration gains with a long-run elasticity of productivity with respect to density reaching 0.13. Interestingly, the strength of agglomeration effects seems to have increased over time. This result is consistent with economic geography models that predict a bell-shaped curve for trade costs versus agglomeration gains. The European economy, which has experienced a decline in trade costs over the last decades, appears to lie on the right-hand side of the curve, where agglomeration effects are reinforced when trade costs become smaller. Foster and Stehrer (2009) obtain estimates closer to those of Ciccone (2002) when using a panel of over 255 NUTS 2 regions in 26 European countries for the 1998–2005 period that covers six industries, including “agriculture, forestry and fishing,” which is not considered by Brülhart and Mathys (2008). They also obtain the further result of a larger magnitude of agglomeration economies for new member states than for old ones. Nevertheless, they use land area as the only exogenous instrument, as in Ciccone (2002), and consider that the regional skill composition is exogenous, which is not very convincing. Marrocu et al. (2013) further extend the number of countries, regions, and time span while leaving aside the endogeneity issues, and conclude that specialization gains would be more prevalent in new member states and diversity would be more prevalent in older ones.

A number of early studies estimate agglomeration economies for separate countries on either wages or TFP aggregated by region. We do not summarize the results of all these studies as they have already been covered by Rosenthal and Strange (2004). We rather focus on recent articles that use richer datasets at the individual level that include workers’ or firms’ precise location.

Glaeser and Maré (2001) were the first to evaluate agglomeration effects on wages net of individual fixed effects, the analysis being conducted on US data. Unfortunately, the size of their dataset does not allow them to evaluate the elasticity of wages with respect to density but allows them to evaluate only the impact of a couple of dummies for city size. For the same reason, it is also difficult to compare the magnitude of the effects estimated by Wheeler (2006) and Yankow (2006), still from US data, with the magnitudes in the rest of the literature. Combes et al. (2008a) are able to estimate the effect of density on wages across all French cities at the individual level while considering individual fixed effects and taking into account aggregate endogeneity with the two-step estimation procedure involving instrumentation that is described in Section 5.2.1.1. They find an elasticity of wages with respect to density of around 0.030, which is half that obtained when individual unobserved heterogeneity is not taken into account. Using a more elaborate instrumentation strategy, Combes et al. (2010) obtain a value of 0.027. This figure is very close to the one obtained for Spain by de la Roca and Puga (2012) when they do not control for dynamic agglomeration effects, which is 0.025. Mion and Naticchioni (2009) replicate the strategy of Combes et al. (2008a) with Italian data and get an even
smaller estimate of 0.01, which is still significantly different from zero. From UK data, D’Costa and Overman (2014) get an elasticity of 0.016, and from Dutch data, Groot et al. (2014) get 0.021, controlling for many individual variables and city-industry-time fixed effects but not individual fixed effects.\textsuperscript{15}

Combes et al. (2008a) also show that individual abilities do not distribute randomly across locations. Workers who have higher skills are more often located in productive cities, which are denser. The correlation between individual and area fixed effects is 0.29, and the correlation between individual fixed effects and density is as high as 0.44. This is the fundamental reason why controlling for individual characteristics has so much influence on the estimate of the elasticity of productivity with respect to density. Mion and Naticchioni (2009) find that sorting is slightly weaker in Italy, as they obtain a correlation between individual fixed effects and density of 0.21. There is also some evidence of spatial sorting in Spain as shown by de la Roca and Puga (2012) when dynamic agglomeration effects are not taken into account, and in the United Kingdom as shown by D’Costa and Overman (2014) when both static and dynamic effects are considered.

The role of skills has been debated further by de la Roca and Puga (2012), who show from Spanish data that the explanatory power of individual fixed effects largely falls once dynamic agglomeration effects are taken into account in the specification. As detailed in Section 5.2.2, dynamic effects are captured with variables measuring the time spent in different classes of city size. When these variables are not included in the specification, having spent more time in larger cities is captured by the individual fixed effect. The inclusion of city experience variables allows de la Roca and Puga (2012) to disentangle the effects of individual skills captured by individual fixed effects from dynamic agglomeration gains. In order to assess the magnitude of dynamic gains, de la Roca and Puga (2012) consider a quantity defined at the city level as the sum of the time-invariant city fixed effect and the effect of experience accumulated in the city for a worker who stayed there for 7 years (which is the average length of time for workers in their sample). The elasticity of this quantity with respect to density that captures both static and dynamic agglomeration effects is 0.049, which is almost twice as large as the elasticity of city fixed effects evaluated as 0.025. This indicates major dynamic gains which would be even larger for more able workers as shown by the estimation of a specification allowing for an interaction between the individual fixed effect and city experience. Perhaps surprisingly, dynamic gains are found to be independent of the size of the city to which workers move subsequently. There would thus be a transferability of learning effects, which is homogeneous across locations.

\textsuperscript{15} In contrast with these references, when considering individual data on siblings from the United States, Krashinsky (2011) finds that the average urban wage premium becomes nonsignificant when introducing family fixed effects because there is a sorting of families across urban areas.
Following an empirical strategy close to that of de la Roca and Puga (2012), D’Costa and Overman (2014) show for the United Kingdom that dynamic effects are also present but weaker than in Spain. In particular, dynamic gains appear to be one-shot only, the first year of stay in a city, and do not cumulate over time (except for the youngest workers, below 21 years old). These results are consistent with those of Faberman and Freedman (2013), who study the impact of the age of firms on earnings returns to density with US data and find that almost all of the gains occur at the birth of firms. The structural exercise conducted by Baum-Snow and Pavan (2012) allows them to consider endogenous individual location choices, static and dynamic heterogeneous agglomeration gains, and matching effects. Their conclusions for the United States are similar to those for Spain. Both static and dynamic gains from agglomeration are present, static gains being more important to explain differences between small and medium cities, and dynamic gains playing a more significant role to explain differences between medium-sized and large cities. Conversely, individual sorting and matching effects play a secondary role in the city wage premium.

Owing to computation limits, many studies consider only classes of city size and not all the cities separately. Moreover, in de la Roca and Puga (2012), the heterogeneous individual impact of dynamic agglomeration economies is supposed to be identical to the direct effect of individual skills, and static agglomeration effects are not allowed to be specific to skills, whereas in D’Costa and Overman (2014), both static and dynamic agglomeration effects are homogeneous across workers. Lastly, considering time-invariant city fixed effects makes the city experience component also capture the time evolution of static agglomeration gains. Other recent attempts that consider both static and dynamic effects in specifications closer to those of Glaeser and Maré (2001) include the work of Lehmer and Möller (2010), who find for Germany that only dynamic effects occur once firm size and individual fixed effects are taken into account, Carlsen et al. (2013), who find for Norway that static gains are homogeneous across education levels, while dynamic ones increase with education, and Wang (2013), who finds for the United States that both static and dynamic gains are present and that they are stronger for younger and more educated workers. To conclude, de la Roca and Puga (2012) and Baum-Snow and Pavan (2012) pioneered the simultaneous study of static and dynamic agglomeration effects on wages, while taking into account the observed and unobserved heterogeneity of workers. Further investigation along the lines suggested in Section 5.2 constitutes an appealing avenue of research.

As discussed in Section 5.4.1, it is worth studying TFP rather than wages since it is a direct measure of productivity that can sometimes be computed at the firm or establishment level, keeping in mind that interpretations change. On the other hand, no convincing method has been proposed to control for individual skills when estimating agglomeration effects on TFP even with individual data at hand, and we have seen that sorting according to skills can induce considerable biases. Henderson (2003) for the
United States and Cingano and Schivardi (2004) for Italy were among the first to study firm-level TFP. However, their assessment of possible endogeneity biases is only partial. Henderson (2003) uses GMM techniques to instrument both input use and local variables, with the caveats we mentioned in Section 5.4.3.3. Cingano and Schivardi (2004) take into account the endogeneity of input use only, through the implementation of the Olley–Pakes estimation procedure. Graham (2009) provides estimates for the United Kingdom based on firm-level TFP data but he instruments neither input use nor local effects. Di Giacinto et al. (2014) assess the respective impact of locating in an urban area and in an industrial district on firm-level TFP in Italy, while instrumenting input use but not the size of the local economy, which is also included as a control. As regards France, Combes et al. (2010) estimate firm TFP with the Olley–Pakes estimation procedure among others and use the estimates to construct a local measure of TFP, which is then regressed on density while using historical and geological variables as instruments. Martin et al. (2011) rather rely on GMM using lagged values of explanatory variables as instruments. To the best of our knowledge, a large number of European countries, including Germany and Spain, have not yet benefited from specific estimates of agglomeration effects on TFP.

Studies on TFP usually conclude that there are significant agglomeration gains in firm productivity, even if some authors who simultaneously control for the level of industrial employment (not its share) wrongly reach the conclusion of their absence (see the discussion in Section 5.3.2). Melo et al. (2009) show that elasticities of TFP with respect to density are on average estimated to be larger than those obtained for wages, typically around 50% larger, and so are they in Combes et al. (2010), where both types of estimates are computed on the same dataset and endogeneity is taken into account using the same instruments. Indeed, Combes et al. (2010) get an elasticity of TFP with respect to density of 0.035–0.040, whereas they obtain 0.027 for the elasticity of wages. According to our basic model, it is difficult to interpret the difference between the two types of estimates. In wage equations, all the effects are rescaled by the share of labor in the production function. Moreover, agglomeration economies percolating through the cost of inputs other than labor, such as land and intermediate inputs, affect wages but not TFP (see Section 5.4.1). A further possible reason for the difference in estimates obtained from wage and TFP regressions is that no one has managed to successfully control for individual skills when working on TFP. Taking properly into account workers’ unobserved heterogeneity in TFP estimations is an avenue for future research.

5.5.2 Heterogeneous effects

As explained in Section 5.4.5.3, the impact of local characteristics on productivity should be bell shaped as agglomeration gains are increasing and concave, while agglomeration costs are increasing but convex. Variations in the marginal effects of local characteristics
are a first type of heterogeneity. For instance, the gain from increasing city size could be positive and large for small cities, and turn negative for very large ones, predictions that need to be investigated, for instance, to assess whether or not the size of cities is optimal.

Most studies do not report an estimated degree of concavity for agglomeration effects. Exceptions include the study of Au and Henderson (2006b), who estimate for China a bell-shaped relationship between the productivity and size of cities and conclude that most cities lie on the left-hand-side of the peak—that is, they are too small to achieve the highest level of productivity. For the United Kingdom, Graham (2007) develops an original strategy based on road traffic congestion to estimate the diminishing returns of agglomeration effects and their link with transport congestion. Five of nine industries present concave effects of density. Furthermore, it is shown that when congestion is taken into account, the elasticity with respect to density increases in seven of the nine industries. This is in line with expectations since in the absence of controls, the elasticity with respect to density reflects the overall net impact of density, taking into account both positive and negative effects. In the United Kingdom, congestion is shown to represent up to 30% of the agglomeration effect.

Agglomeration effects can also be heterogeneous across industries as the strength of agglomeration economies depends on industry characteristics. Nevertheless, estimations by industry remain scarce. One reason may be that the design of the empirical model, and in particular the search for valid instruments, has to be done industry by industry. Another reason is the lack of availability of local data per industry. The works of Brüllhart and Mathys (2008) and Foster and Stehrer (2009) are notable exceptions, but these works are at the European regional level and do not control for individual effects. They find significant agglomeration effects in all but one of the industries they consider. The exception is agriculture, in which regional density has a negative impact, a result that is fairly intuitive. Given the share of land in agricultural production and the fact that land prices increase with density, less dense places clearly represent the best alternative for productivity in this industry. Morikawa (2011) estimates from firm-level data the elasticity of firm TFP with respect to density for detailed services industries in the United States without using instruments. He finds large elasticities ranging from 0.07 to 0.15. In their meta-analysis, Melo et al. (2009) conclude that on average agglomeration effects tend to be stronger in manufacturing industries than in service industries.

Some studies have tried to evaluate the extent to which agglomeration economies are stronger for some types of workers or firms. For instance, Bacolod et al. (2009b) and Abel et al. (2012) for the United States, Di Addario and Patacchini (2008) for Italy, and Groot and de Groot (2014) for the Netherlands confirm the intuition that returns to education are higher in cities. This is also found for the United States by Lindley and Machin (2014), who then assess to what extent the change in wage inequality across states over the 1980–2010 period arises from a shift in skill composition and a variation in education-specific returns to agglomeration economies. Firms in industries that are more
skill intensive should be concentrated where returns to education are higher, the larger
cities, and this is observed by Elvery (2010) for US metropolitan areas. The study by Lee
(2010) is one of the rare studies to exhibit an industry in which the urban wage premium
is found to decrease with skills, the health-care sector in the United States. He explains his
result by labor supply effects for high-skilled health-care employees as surgeons, dentists,
or podiatrists, who would be more attracted by urban life than nurses or massage
therapists, and this would put a downward pressure on their wages in larger cities.

Using a structural approach controlling for endogenous location choices, Gould
(2007) shows that both static and dynamic agglomeration gains are present for
white-collar workers but not for blue-collar workers. Matano and Naticchioni (2012)
reach a similar conclusion after performing quantile regressions on Italian data and con-
trolling for sorting on unobservable worker characteristics. They find that agglomeration
effects appear to strengthen along the wage distribution. This is in line with the conclu-
sions of Combes et al. (2012b), who use the full distribution of firm-level TFP in France
to show that the most efficient firms gain more from density than the least efficient ones.
For instance, firms in the last quartile of productivity gain three times more from density
than those in the first quartile. It is also found that the largest establishments gain more
from density. The benefits are 50% greater for establishments with more than 100
workers than those with 6–10 workers. Going in the opposite direction, Henderson
(2003) and Martin et al. (2011) conclude that specialization effects are larger for smaller
firms, but these two articles measure specialization with the level and not share of indus-
tral employment. Therefore, they partially confound density and the specialization
effects as explained in Section 5.3.2.

Other authors have investigated the sources of heterogeneous productivity gains from
agglomeration, but rarely take into account simultaneously the endogeneity issues related
to reverse causality and missing local variables. For instance, Rosenthal and Strange
(2003) using US data find that the number of hours worked decreases with density
for nonprofessionals but increases for professionals, and the effect is stronger for young
workers. Moreover, the number of hours worked by young professionals is particularly
sensitive to the proximity of other young professionals. Bacolod et al. (2009a) investigate
which skills have returns positively related to city size. They conclude that only cognitive
and social skills are better rewarded in large cities, while motor skills and physical strength
are rewarded less well. In line with these results, Andersson et al. (2015) find that it is only
for nonroutine jobs that there are gains from agglomeration in Sweden once the spatial
sorting of skills is taken into account.

There is also scarce evidence of heterogenous agglomeration gains across demographic
groups. Phimister (2005) estimates gender differences in city size premium from UK data,
controlling for individual fixed effects but without taking into account endogeneity issues.
He finds a larger urban premium for women, especially for those who are married or coha-
biting. Ananat et al. (2013) investigate differences across races in the United States while
controlling for unobserved worker heterogeneity through residential location choices as in Fu and Ross (2013) but without dealing with endogeneity issues at the local level. They find that agglomeration effects are heterogeneous across races, the black–white wage gap increasing by 2.5% when there are 1 million more inhabitants in the city.

5.5.3 Spatial extent of density effects

The rapid spatial decay of agglomeration effects is another robust finding in the literature. Agglomeration economies do not spill much over space. For the advertising agency industry, Arzaghi and Henderson (2008) provide evidence of an extremely fast spatial decay of agglomeration effects that are shown to occur primarily within 500 m. This decay is certainly too extreme to be representative of more standard industries but, still, effects are rarely found to be significant beyond 100 km, and the threshold is often lower.

The first way to assess the spatial extent of agglomeration effects consists in considering a single market potential variable that encompasses both the own location size and the sizes of other locations. As detailed in Section 5.3.1, one can consider the Harris market potential, which is simply the sum over all spatial units, including the own location, of their size (or density) divided by the distance between the location and the unit considered. More structural forms of market potential from economic geography models can also be used. Importantly, in all cases, one implicitly assumes a quite strong spatial decay of agglomeration effects. For instance, when trade costs are inversely related to distance, the impact on a location of the economic activity located 20 km away is four times lower than that of activity located 5 km away, it is 10 times lower at 100 km than at 10 km, and so on. The positive effect of the economic size of distant locations and the spatial decay of this effect are rarely rejected empirically. For instance, Head and Mayer (2006) in a study on European NUTS 2 regions obtain, when neither local skills nor endogeneity are taken into account, that both the Harris market potential and a structural market potential significantly increase regional wages, the two variables having a similar explanatory power. Holl (2012) assesses the effect of a Harris market potential based on distance through the real road network for which the historical population, geology, and historical transport networks are used as instruments. He finds a positive effect of this market potential on regional wages in Spain. Structural articles following Hanson (2005), such as the two early replications by Mion (2004) for Italy and Brakman et al. (2004) for Germany, confirm the positive impact of structural market potential on regional wages, even if sorting on skills is not always taken into account and endogeneity concerns are not always fully addressed. Brakman et al. (2006), Breinlich (2006), Brakman et al. (2009), and Bosker et al. (2010) find evidence of a positive effect of structural market potential on GDP per capita for NUTS 2 European regions. Fallah et al. (2011) show for US metropolitan areas
that the impact of the structural market potential is stronger at the top of the wage
distribution. Some other contributions for developing countries are discussed in
Section 5.5.7.

Assessing separately the role of the own density and market potential definitely
makes more sense if different local externalities operate at different distances. External
market potential (which excludes the own size or density) is most often found to have a
significant positive effect on local productivity when it is introduced in addition to den-
sity in the specification. For instance, Combes et al. (2008a, 2010) find that both vari-
ables have a significant positive effect in France, even when they are both instrumented
and individual unobserved heterogeneity is taken into account. For NUTS 2 European
regions, Foster and Stehrer (2009) introduce next to density a measure of market poten-
tial with a spatial decay of agglomeration economies arising from other regions of expo-
nential form—that is, with a decline that is even sharper than the inverse of distance.
When trying exponential functions with various coefficients, they find that only those
with the strongest spatial decay exhibit significant effects. Note that, in general, intro-
ducing the external market potential in regressions only slightly reduces the impact of
the own density.

The second strategy for assessing the spatial decay of agglomeration economies con-
sists in introducing in the specification variables for the economic size of distant loca-
tions. Ciccone (2002) finds for NUTS 3 European regions that production in
neighboring regions has a positive impact on local productivity. He does not report
the magnitude of the coefficient however, and he does not test for an impact of regions
located further away. Rice et al. (2006) find for UK regions that agglomeration econ-
omy attenuate sharply with distance. Distant markets do affect local wages and pro-
ductivity, but markets located 40–80 min away have one-quarter the effect of those
located less than 40 min away, and markets located 80–120 min away have no signif-
icant impact. Rosenthal and Strange (2008) obtain even larger spatial gradients when
estimating the effect of employment concentration in rings around location on wages
in US cities. The effect of the 0–5-mile ring is four to five times larger than the effect of
the 5–25-mile ring. Turning to the outer rings (25–50 miles and 50–100 miles), they
find that the effects are even smaller and very often not significantly different from zero.
The spatial pattern obtained for Italy by Di Addario and Patacchini (2008) is consistent
with this one since the impact of local population size is strongest between 0 and 4 km
and is not significant anymore beyond 12 km.

5.5.4 Market access effect evaluated using natural experiments

As our chapter shows, strategies used to tackle endogeneity issues are not always convinc-
ing, and in some cases, authors do not even attempt to tackle them. A few recent pub-
llications propose using natural experiments as a source of variation in the local economy
size to circumvent endogeneity problems. Greenstone et al. (2010) test the presence of agglomeration effects on firm TFP by exploiting the arrival of large plants in some given US counties. Such plants affect the intensity of agglomeration economies, although it is not possible to quantitatively assess the exact magnitude of the shocks. The key idea for finding a relevant control group for counties receiving a large plant is to rely on a real estate journal, Million Dollar Plants, that gives for any large plant created the county that the plant ultimately chose (the winner) and the counties that survived a long selection process but were ultimately not selected (the runners-up). Greenstone et al. (2010) show that on average runner-up counties have characteristics similar to those of winners. The effect of plant arrivals on incumbent plants is studied in a panel including both winner and runner-up counties but not others. Firm TFP is regressed on an interaction term between a dummy for being in the winner group and a dummy for the dates after the arrival of the large plant. The estimated coefficient of this interaction corresponds to the difference-in-differences estimator. It is found to be significantly positive and sizeable, especially for incumbent plants sharing similar labor and technology pools with the new plant. Whereas the empirical strategy is quite convincing for identifying the effect of arriving plants, the link between the arrival of plants and changes in the intensity of agglomeration spillovers remains unknown (see the argument in Section 5.4.3.4). Moreover, external validity is far from certain since only a small subsample of counties is studied.

Articles exploiting natural experiments to evaluate the effect of market potential typically use the opening and closing of frontiers that prevent firms or cities from interacting with neighbors. An early example is given by Hanson (1997), who studies the effect of the trade reform in Mexico in the 1980s that turned the country from a closed economy to an economy open to trade with foreign countries, and in particular with the United States. The opening of the frontiers has increased the market potential, especially for firms close to the Mexican–US border. It is shown that the opening of frontiers attracted firms close to this border, whereas the concentration of firms in the capital city Mexico, which is located at a distance from this border, decreased. A more recent interesting use of a natural experiment is provided by Redding and Sturm (2008), who study the effect of the division of Germany in 1949 on the growth of cities on the western side of the West German–East German border. The border cut their access to cities on the eastern side and thus decreased their market potential. The effect on cities located further away from the border should have been smaller as they had better access to other cities in western Europe. Consequently, Redding and Sturm (2008) compare the population growth of western cities close to the border with that of western cities far from the border, the two groups of cities having the same population trends before

16 Note that the outcome here is city growth and not productivity as in other contributions surveyed in this section. This is because we chose to review all significant articles using natural experiments at the same place. Other results on city growth are reviewed in Section 5.6.
the division of the country. This is done in the same spirit as Greenstone et al. (2010), by restricting the sample to western cities and regressing city growth on an interaction term between a dummy for being close to the West German–East German border and a dummy for dates after 1949. It is found that division of Germany led to a substantial relative decline of population growth for cities close to the border. The effect is larger for smaller cities, which is expected since they have a smaller own market and rely more on other city markets. An interesting additional exercise would be to assess to what extent the division of Germany decreased the value of a market potential index and to deduce from this measure of the shock and the difference-in-differences estimator a value for the elasticity of population growth with respect to market potential. This coefficient could be compared with the one obtained using a more standard least squares instrumentation approach.

5.5.5 Specialization and diversity

We now review articles evaluating the effect of localization economies on local productivity. The main variable used for that purpose is specialization, which is computed as the share of the industry in the local economy. Its effect on local productivity is assessed while controlling for the size or density of total activity. In many studies, when density and specialization are simultaneously introduced, both are found to have a significant positive effect on productivity. For instance, Cingano and Schivardi (2004) show that this is the case in Italy when industries are pooled together. They also find that the spatial decay is very strong, since specialization in neighboring regions has no impact on local productivity. For France, Combes et al. (2008a) find that the effect of specialization, estimated on wages separately for each industry, is significantly positive for 94 industries out of 99. Its magnitude is larger in business services and in two high-tech industries, medical instruments and artificial fibers. This is intuitive since such industries could face stronger technological spillover effects. These results confirm those of Henderson (2003) for the United States, where a larger effect of specialization is found in high-tech industries. Martin et al. (2011) obtain a significant positive effect of specialization on firm productivity in France that becomes negative above a certain level of specialization, which is consistent with the presence of concave localization effects. From European data, Brühlhart and Mathys (2008) find a negative impact of own-industry density on output per worker in the industries they study, with the notable exception of financial services. Using a spatial variance analysis, Combes et al. (2008a) show that whereas total

A follow-up study (Ahlfeldt et al., 2012) shows that the division and reunification of Berlin had a significant effect on the gradient of land prices and employment in West Berlin close to the former main concentration of economic activity in East Berlin but a negligible effect along other more economically remote sections of the Berlin Wall.
employment density explains a large share of spatial disparities in productivity, the explanatory power of specialization remains small.

Following both the intuition of Jacobs (1969) and the central role of preference for diversity in many economic geography models, another appealing variable to explain productivity is the overall industrial diversity of the location. However, its estimated effect has been shown to be not robust. It is sometimes significantly positive, sometimes significantly negative, and often not significant at all, as, for example, for France in both Combes et al. (2008a, 2010), for Italy in Cingano and Schivardi (2004), and for the United States in Henderson (2003). Even if there are interesting intuitions behind diversity variables, no effect seems to be at play. This may be due to the way diversity is measured, since it is often through a Herfindahl or Krugman specialization index computed from the industry shares in the local economy using a rather aggregate industry classification. Moreover, some industries may benefit from a group of other industries but usually not from all industries as assumed in the Herfindahl index. To tackle this issue, Moretti (2004b) uses a measure of proximity between industries and finds for the United States that spillovers between economically close industries are larger than spillovers between economically distant industries, and this better matches what Jacobs had in mind.

5.5.6 Human capital externalities

We have already emphasized that the local share of professionals or highly educated workers has many effects on productivity that can be difficult to disentangle. First, when using data aggregated at the city level or the region level, one cannot identify separately the direct composition effect of skilled workers on average productivity and their human capital externality effect. When using individual data, one can assess the role of the local share of skilled workers on individual productivity, while simultaneously taking into account the direct composition effect by introducing individual variables or individual fixed effects. Nevertheless, Section 5.3.3 shows that the local share of skilled workers captures not only the externality effect but also a substitution effect, which is positive for unskilled workers and negative for skilled workers.

There has been a debate since the beginning of this millennium on the existence and magnitude of local human capital externalities. While Moretti (2004a,b) find significant positive effects of human capital measures, Ciccone and Peri (2006) rather obtain an estimate that is not significant. It is difficult to make a conclusive case for either side. Moretti (2004a) implements the now standard approach of regressing the individual wage on the share of college-educated workers, but this share captures both the externality and substitution effects. This is also the case in Moretti (2004b) when studying TFP rather than wages. On the other hand, Ciccone and Peri (2006) use a shift-share approach supposed to control for substitution effects, but the sources of identification remain unclear as
explained in Section 5.3.3. Importantly, no article simultaneously controls for the presence of possible gains from density, whereas density is usually positively correlated with local human capital.

Other articles mostly use the same approach as Moretti (2004a) and obtain similar results. Rosenthal and Strange (2008) find the same positive effect of the local share of college-educated workers in the United States. Considering this share at various distances from each worker location, they also find that the effects of human capital externalities attenuate sharply with distance. The effect of the share of college-educated workers in the 0–5-mile ring around the location is 3.5 times larger than the effect of this share in the 5–25-mile ring. These results are consistent with those of Fu (2007), who finds for the Boston Metropolitan Area using data on census blocks that human capital externalities decrease quickly beyond 3 miles.

For Europe, Rice et al. (2006) assess the role of the local share of workers with degree-level qualifications in the United Kingdom and find that it has a positive effect on wages and productivity. However, since the specification is estimated not at the individual level but rather at the local level, it is not possible to quantify separately the composition and externality effects. This is possible for France, and Combes et al. (2008a) find a positive effect of the local share of professionals within the industry on individual wages, even after controlling for individual fixed effects and age, as well as location-time fixed effects that capture in particular the effect of density. Similarly, Rodríguez-Pose and Tselios (2012) find a positive impact of the regional levels of education on individual earnings for European regions while using individual data and controlling for individual characteristics and region-time fixed effects.

Interestingly, when both productivity and wage data are available, one can evaluate how much of the productivity gains due to agglomeration are transformed into wage gains for workers. While this has not been done for Europe, Moretti (2004b) finds for the United States that estimated productivity differences between cities with high human capital and low human capital are similar to observed differences in wages of manufacturing workers, indicating an almost complete transfer of human capital effects to workers. Since unobserved worker heterogeneity is not controlled for in that study, the similarity between the productivity and wage differences can also result from a composition effect affecting both wages and TFP.

5.5.7 Developing economies

We now present empirical results on the presence of agglomeration economies in some developing countries. The related literature is recent, and research needs to be pursued to gain knowledge on additional countries. The effect of market size on wages has been studied for China, India, and Colombia. Panel data are usually not available, and it is thus, generally not possible to take into account unobserved individual heterogeneity. Differences between individuals are rather taken into account through individual explanatory
variables such as qualification, gender, age, and sometimes occupation or the type of firm where the individual is employed. Overall, market size is found to have a larger effect than in developed countries. Combes et al. (2013), for instance, study the effect of density on individual wages in 87 Chinese prefecture cities, using as instruments for density the peripherality, the historical status of the city, and the distance to historical cities. The elasticity of wages with respect to density is found to be 0.10–0.12, around three times larger than in developed countries. Chauvin et al. (2014) evaluate the effect of density on individual annual earnings in India at the district level and also find a large elasticity of around 0.09–0.12. Duranton (2014) investigates the impact of population on individual wages in Colombia while controlling for area at the local labor market level (which amounts to investigating the effect of density). Instrumentation is conducted using historical populations or soil characteristics (erodibility and fertility). The estimated elasticity is 0.05, and thus lower than in China and India, but still large compared with estimates for developed countries.

Other measures of productivity have been used in studies at the aggregate level. Henderson et al. (2001) evaluate the effect of city population on value added per worker in Korea for 5 industry groups and 50 cities using panel data over the 1983–1993 period. They do not find evidence of a size effect for any industry, but their results are based on time evolutions without instrumentation for the endogeneity of the city population. Similarly, Lee et al. (2010) find that population density does not have any significant effect on establishment-level output per worker in Korea when estimating a specification where local fixed effects and control variables are considered. Au and Henderson (2006a) and Au and Henderson (2006b) study at the city level the effect of total employment and its square on output per worker in China in the 1990s, using as instruments urban plans not related to output and urban amenity variables. They control for the local shares of manufacturing and services, and the shape of the total employment effect is allowed to vary with these shares. They find a concave effect of total employment on output per worker. The vast majority of Chinese cities appear to have a size of less than 50% of the peak, where agglomeration economies are the most important. This can be explained by the hukou system that restricts workers’ social rights mostly to their birthplace and thus limits their mobility, especially in the 1990s, when it was strictly enforced.

There are also a couple of publications on firm productivity. Lall et al. (2004) study the effect of urban density on firm productivity in India for 11 industries considered separately, estimating jointly a production function and a cost function. The effect is found to be significantly positive in one industry only. Saito and Gopinath (2009) quantify the impact of regional population on firm TFP in the food industry in Chile, estimating a production function using the Levinsohn–Petrin approach. The elasticity is found to be significantly positive, at around 0.07. In both articles, the authors do not deal with the endogeneity of local determinants of agglomeration economies.

The role of market potential is considered along with the size of the local economy by some of the previous articles. Lall et al. (2004) study the impact of the Harris market
potential in India, an originality of their work being the use of accurate transport times rather than distances in the construction of their market potential variable. This variable includes the own location, and its effect is found to be negative but nonsignificant for several industries. Other articles conduct similar exercises but remove the own area from the computation of the market potential measure to disentangle the size effects from the local economy and external markets. Interestingly, Duranton (2014) obtains a significantly negative sign for the effect of external market potential on wages in Colombia. An explanation may be that when workers are perfectly mobile as in Krugman (1991b), the spatial equilibrium without full agglomeration implies lower nominal wages in larger regions to compensate for the better market access that decreases the prices of consumption goods. Combes et al. (2013) find no significant effect of market potential on wages in China once it is instrumented simultaneously with other local determinants, whereas Au and Henderson (2006a) find a positive effect on output per worker but the variable is not instrumented.

Some articles have adopted quasi-structural approaches inspired by Redding and Venables (2004) and Hanson (2005) to focus on the effects on wages of structural market access and supplier access that are derived from economic geography models. This has the limitation that the own area is involved in the construction of the access variables and the effect of the own local economy size cannot be identified separately from the effects of external market and supplier access. Amiti and Cameron (2007) study the effect of both access variables on wages at the firm level in Indonesia, but without being fully structural in their construction and without using instruments to take into account endogeneity issues. Both market and supplier access are found to have a positive effect. Only 10% of the market access effect goes above 108 km, and only 10% of the supplier access effect goes above 262 km.

Fally et al. (2010) evaluate the impact of market and supplier access on individual wages in Brazil using a two-stage approach. First, a wage equation including state-industry fixed effects and individual characteristics is estimated in the spirit of Combes et al. (2008a) but at the industry level and without individual fixed effects since only cross-section data are available. In a second step, estimated state-industry fixed effects are regressed on structural measures of market and supplier access. These measures are obtained following strictly the strategy proposed by Redding and Venables (2004) where market and supplier access are recovered from the estimates of the trade flow specification derived from a economic geography model. An originality is that trade flows are measured at the industry level, which allows the construct of the access variables for each industry separately, whereas other articles only use aggregate flows and therefore construct only aggregate access variables. Both market and supplier access variables are found to have a significant positive effect on wages when estimations are conducted using OLS.

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18 The second-step estimation could have been for each industry separately, as proposed in Section 5.2.1, but pooling all industries together was preferred, possibly because the number of locations (27 states) is small.
The supplier access variable is then removed from the specification and only the market access variable is instrumented (both variables rarely have simultaneously a significant effect owing to their high correlation). Market access is found to keep its significant positive impact on wages.

Finally, Hering and Poncet (2010) evaluate the effect of market access on individual wages in 56 Chinese cities. They also follow the strategy proposed by Redding and Venables (2004) to build the market access variable but they do not consider the role of supplier access at all. Labor skills are captured by individual observed characteristics and a single-step estimation strategy is used. Hering and Poncet (2010) instrument market access by centrality indices and find a significant positive effect which is larger for skilled workers.

Note that in all these contributions, structural access variables are the only local determinants of agglomeration economies considered in the specifications. Therefore, their impacts cannot be identified separately from the effects of other local determinants not derived from economic geography models if these other determinants are correlated with access variables, which can occur in particular when distance plays a similar role in the attenuation of their effects.

Finally, some articles have studied local determinants of agglomeration economies other than market size. Henderson et al. (2001) assess the effect of industrial specialization (measured with industry local employment) on productivity growth in Korea. They find some evidence of localization economies for all the industry groups they consider, the magnitude of the effects being similar to those for the United States. Lopez and Suedekum (2009) are interested in localization economies and agglomeration spillovers on TFP for establishments in Chile. They consider both downstream and upstream spillovers between firms related by input–output relationships. They find a positive effect of the number of intraindustry establishments consistent with the presence of localization effects and a positive effect of the number of establishments in upstream industries consistent with unidirectional agglomeration spillovers. Saito and Gopinath (2009) evaluate the impact of diversity, measured by a Herfindahl index, on firm TFP in the food industry in Chile, but find no significant effect. Endogeneity of local determinants and spatial sorting of workers are considered in none of these articles.

5.6. EFFECTS OF AGGLOMERATION ECONOMIES ON OUTCOMES OTHER THAN PRODUCTIVITY

Although the most straightforward interpretations are made for the effects of local variables on local productivity, a rather large literature has attempted to identify the role of agglomeration economies on local outputs other than productivity. These outputs include employment or employment growth, and firm location decisions. We now turn to this literature and relate it to the same theoretical framework as the one we developed.
for productivity. This allows us to emphasize difficulties that are encountered when interpreting the results. Nevertheless, we survey the results that have been obtained over the last decade.

5.6.1 Industrial employment

We first focus on the local determinants of local industrial employment. We provide a theoretical background to specifications estimated in the literature, comment on the interpretations that can be made for the estimated coefficients, and finally present the results obtained in related articles.

5.6.1.1 From productivity externalities to employment growth

The two early studies that initiated the empirical evaluation of agglomeration economies in the 1990s, those of Glaeser et al. (1992) and Henderson et al. (1995), do not directly focus on the determinants of local productivity but focus rather on those of local employment growth at the industry level. A possible reason is that data on wages or TFP at fine geographical levels such as cities or local labor markets were less available than today, and this is even more the case for individual data. At the same time, employment is, by itself, a local outcome of interest, especially for policymakers, when, for instance, regional unemployment disparities are large as in Europe.

We develop a theoretical framework similar to the one used for productivity in order to ground employment equations and to allow for relevant interpretations of the effects found in this literature. As will become clear below, it is necessary to rely on a production function at the industry level with nonconstant returns to scale and we consider

\[ Y_{c,s,t} = \frac{A_{c,s,t}}{a_1 - a_2} (s_{c,s,t} L_{c,s,t})^{a_1} K_{c,s,t}^{a_2}, \]  

(5.57)

where \( a_1 + a_2 < 1 \). The first-order conditions equalizing the return of inputs to their marginal productivity are

\[ w_{c,s,t} = \frac{\alpha_1 p_{c,s,t} A_{c,s,t}^{a_1} (s_{c,s,t} L_{c,s,t})^{a_2 - 1} K_{c,s,t}^{a_2}}{a_1 - a_2} L_{c,s,t}^{a_1} K_{c,s,t}^{a_2}, \]  

(5.58)

\[ r_{c,t} = \frac{\alpha_2 p_{c,s,t} A_{c,s,t}^{a_1} (s_{c,s,t} L_{c,s,t})^{a_2 - 1} K_{c,s,t}^{a_2}}{a_1 - a_2} L_{c,s,t}^{a_1} K_{c,s,t}^{a_2}. \]  

(5.59)

Substituting into (5.59) the expression of capital given by (5.58) leads to

\[ L_{c,s,t} = \left( \frac{p_{c,s,t} A_{c,s,t}^{a_1} (s_{c,s,t} L_{c,s,t})^{a_2}}{w_{c,s,t} r_{c,s,t}} \right)^{1/(1 - a_1 - a_2)}. \]  

(5.60)

We first leave aside the role of wages, which will be discussed below. Making the same assumptions as in Section 5.2 on how local characteristics determine \( p_{c,s,t}, A_{c,s,t}, \) and \( r_{c,s,t}, \)
we can use Equation (5.60) to motivate an empirical specification where the logarithm of local industry employment (instead of wage) is expressed as a function of local variables such as local density, land area, and specialization:

\[
\ln L_{c,s,t} = \beta \ln \text{den}_{c,t} + \mu \ln \text{area}_{c,t} + \theta \ln \text{spec}_{c,s,t} + \nu_{c,s,t} .
\] (5.61)

First notice that, as in the case of productivity, the exact channel of agglomeration economies cannot be identified since local characteristics determining agglomeration effects may have an impact on employment not only through technological progress, but also through input prices and goods prices. Importantly, the role of specialization cannot be identified since the dependent variable, industrial employment, is a log-linear combination of specialization and density, and terms have to be rearranged to avoid redundancy. This identification issue is the reason why the production function was specified at the industry level. By contrast, the role of other local variables can still be studied since (5.61) implies

\[
\ln L_{c,s,t} = \frac{\beta - \theta}{1 - \theta} \ln \text{den}_{c,t} + \frac{\mu - \theta}{1 - \theta} \ln \text{area}_{c,t} + \nu_{c,s,t} .
\] (5.62)

The impact of the remaining local determinants is now net of the impact of specialization, and cannot be identified separately from it. It was initially suggested in the literature that the static agglomeration effect related to specialization could be identified using nonlinearities by also including in (5.61) the level of specialization in addition to its logarithm as an extra local variable. However, this makes interpretations difficult, especially when the two effects are estimated with different signs as, for instance, in Henderson et al. (1995). Parametric identification relying only on specific functional forms should be avoided.

Glaeser et al. (1992) propose rewriting (5.60) in first difference and then considering that the growth rate of local variables instead of their level is a function of the levels of local determinants. They interpret local variables as determinants of technological progress, but these variables also capture the role of agglomeration economies operating through goods and input prices as shown by (5.60). Specialization can now be included among local characteristics, and its effect is identified separately. The corresponding specification is given by

\[
\ln L_{c,s,t} - \ln L_{c,s,t-1} = \tilde{\beta} \ln \text{den}_{c,t-1} + \tilde{\mu} \ln \text{area}_{c,t-1} + \tilde{\theta} \ln \text{spec}_{c,s,t-1} + \tilde{\nu}_{c,s,t} .
\] (5.63)

The coefficients of local variables capture dynamic agglomeration effects such as improved learning but not the impact of static ones as in (5.62).

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19 Firm-level data would make it possible to identify the effect of industry employment by regressing firm employment on industry employment, in a way analogous to how individual wages allowed us to identify the role of individual skills separately from human capital externalities. This has not been done before to the best of our knowledge.
When there is time autocorrelation of residuals, it is possible to derive from (5.62) a dynamic specification of local-industry employment similar to (5.63) even if there are no static and dynamic agglomeration effects. Suppose for instance that $\nu_{c,s,t}$ follows an AR(1) process such that

$$
\nu_{c,s,t} = (1 - \rho) \nu_{c,s,t-1} + \epsilon_{c,s,t},
$$

(5.64)

where $0 < \rho < 1$ and the residuals $\epsilon_{c,s,t}$ are identically and independently distributed. When there is no agglomeration effect such that Equation (5.62) reduces to $\nu_{c,s,t} = \ln L_{c,s,t}$ and if we take into account the fact that $L_{c,s,t} = \text{den}_{c,t} \cdot \text{area}_{c,t} \cdot \text{spe}_{c,s,t}$, equation (5.64) implies

$$
\ln L_{c,s,t} - \ln L_{c,s,t-1} = -\rho \ln L_{c,s,t-1} + \epsilon_{c,s,t} \\
= -\rho \ln \text{den}_{c,t-1} - \rho \ln \text{area}_{c,t-1} - \rho \ln \text{spe}_{c,s,t-1} + \epsilon_{c,s,t},
$$

(5.65)

which involves the same explanatory variables as (5.63) but with coefficients constrained to be the same and negative. This suggests that when a specification such as (5.63) is estimated, it is possible to obtain negative coefficients for local variables even in the presence of dynamic agglomeration economies, and negative signs have indeed been obtained in the literature.

Taking all the intuitions in (5.61), (5.63), and (5.65) together, one may consider a specification with static and dynamic agglomeration effects (as we did for productivity in Section 5.2.2), as well as time autocorrelation of residuals, which leads to

$$
\ln L_{c,s,t} - \ln L_{c,s,t-1} = -\rho \ln L_{c,s,t-1} + \beta (\ln \text{den}_{c,t} - \ln \text{den}_{c,t-1}) \\
+ \mu (\ln \text{area}_{c,t} - \ln \text{area}_{c,t-1}) + \theta (\ln \text{spe}_{c,s,t} - \ln \text{spe}_{c,s,t-1}) \\
+ \tilde{\beta} \ln \text{den}_{c,t-1} + \tilde{\mu} \ln \text{area}_{c,t-1} + \tilde{\theta} \ln \text{spe}_{c,s,t-1} + \epsilon_{c,s,t}.
$$

(5.66)

This specification involves time variations of static effects, dynamic effects, and inertia in industrial employment due to the time autocorrelation of residuals. Rearranging terms to eliminate current and past specialization (as their coefficients are not identified), we finally get

$$
\ln L_{c,s,t} - \ln L_{c,s,t-1} = \frac{\tilde{\theta}}{1 - \tilde{\theta}} \ln L_{c,s,t-1} + \frac{\beta - \tilde{\theta}}{1 - \tilde{\theta}} \ln \text{den}_{c,t} + \frac{\mu - \tilde{\theta}}{1 - \tilde{\theta}} \ln \text{area}_{c,t} \\
+ \frac{\tilde{\beta} - \beta + \tilde{\theta} - \tilde{\theta}}{1 - \tilde{\theta}} \ln \text{den}_{c,t-1} + \frac{\tilde{\mu} - \mu + \tilde{\theta} - \tilde{\theta}}{1 - \tilde{\theta}} \ln \text{area}_{c,t-1} + \epsilon_{c,s,t}.
$$

(5.67)

---

20 This specification is not completely consistent with all the specifications above. It is possible to derive a specification which is consistent but it is much more intricate.
which is a specification close to the one estimated by Henderson (1997) and Combes et al. (2004). Alternatively, one can replace past industrial employment $L_{c,t-1}$ by $\text{den}_{c,t-1} \cdot \text{area}_{c,t-1} \cdot \text{spe}_{c,s,t-1}$ to rather consider a specification with past specialization although the same parameters are identified.

Unfortunately, the five coefficients in Equation (5.67) are combinations of the seven parameters of interest. It is thus difficult to interpret the estimated coefficients even if one is able to deal with the endogeneity of right-hand-side variables. For instance, a negative impact of past industrial employment is compatible not only with the presence of inertia in the series together with a positive static effect of specialization, but also with a negative static effect of specialization. Similarly, a positive impact of past local determinants is not incompatible with a negative impact of some static or dynamic agglomeration effects. As there are more parameters of interest than estimated coefficients, the different effects cannot be disentangled. The model could be augmented with other local characteristics such as market potential or diversity, and more lags of industrial employment, using statistical tests to determine how many lags should finally be kept. However, the same identification issues would remain as the impact of these variables would mix again static and dynamic effects.

Another point that we have not discussed so far about Equation (5.60) is that the local wage (or local wage growth if the dependent variable is employment growth) should be used as a control variable in the empirical specification if one wishes to restrict the interpretation of the effects of local characteristics to their role in $p_{c,s,t}$, $A_{c,s,t}$, and $r_{c,s,t}$ only (consistent with the analysis on productivity) and avoid considering their role in $w_{c,s,t}$. Since one estimates a labor demand equation, the local wage is expected to have a negative effect on local employment. For given wages, agglomeration effects increase labor demand, and therefore we expect a positive effect of density, area, and market potential among other factors on local employment as in the case of productivity.

However, controlling for wages means that only a partial equilibrium effect of agglomeration economies is captured. It corresponds to the direct impact of agglomeration economies on labor demand but it does not capture the feedback effects on this demand resulting from the wage change induced by agglomeration. Moreover, from the econometric point of view, controlling for wages raises serious additional endogeneity issues, on top of those described above when the dependent variable measures productivity.

One can choose not to control for the local wage but then the impact of local characteristics on local employment operates not only through $p_{c,s,t}$, $A_{c,s,t}$, and $r_{c,s,t}$ but also through $w_{c,s,t}$, and the effect through the wage is negative. Typically, agglomeration economies raise nominal wages, which in turn yield a decrease in labor demand. The overall impact of agglomeration economies on employment is now ambiguous, and in particular it can be negative. On the one hand, agglomeration economies that increase $p_{c,s,t}$ and $A_{c,s,t}$ and decrease $r_{c,s,t}$ tend to positively affect employment; on the other hand,
they also increase $w_{c,s,t}$, which tends to negatively affect employment. When the effect of density on local employment is found to be negative, one does not know if density has a negative effect on productivity, and therefore a negative effect on employment because productivity is positively related to employment, or if density has a positive effect on productivity, which in turn has a positive effect on wages, themselves affecting employment negatively. For instance, Cingano and Schivardi (2004) get opposite signs for some of the common determinants of productivity and employment, on the basis of the same Italian dataset. This suggests that a positive effect of agglomeration economies on local productivity can actually turn into a negative effect on local employment, an issue that was initially raised by Combes (2000).

Finally, Combes et al. (2004) also propose breaking down local employment into two terms, employment per firm and the local number of firms:

$$
\ln L_{c,s,t} = \ln \left( \frac{L_{c,s,t}}{n_{c,s,t}} \right) = \ln \frac{L_{c,s,t}}{n_{c,s,t}} + \ln n_{c,s,t},
$$

(5.68)

where $n_{c,s,t}$ is the local number of firms within the industry. One can evaluate separately the impact of local characteristics on average employment in existing firms and on the number of firms. Indeed, urbanization and localization variables can have different effects on the intensive and extensive margins of employment. In first differences, the analysis indicates whether agglomeration economies have the same or opposite effects on internal firm growth and on external growth, or whether the effects are stronger for one or the other employment growth components. Finally, note that some authors evaluate the effect of local human capital on employment growth in the spirit of what has been done for productivity, as, for instance, by Simon (2004) for the United States, and by Suedekum (2008, 2010) for Germany. The interpretation is again blurred by the existence of substitution effects between high-skilled and low-skilled workers as discussed in Section 5.3.3.

### 5.6.1.2 Total employment, specialization, diversity, and human capital

The explanatory variables introduced into employment growth regressions are usually very similar to those considered in productivity regressions, except that local density is replaced by local total employment. Estimated specifications generally involve dynamic agglomeration effects following (5.63) but not static effects. Results for the effect of total employment on industrial employment growth clearly illustrate the diversity of results obtained in the literature on local employment growth. Beyond the fact that samples for different countries and periods are used, the previous section illustrates how the use of different specifications changes the interpretation of estimated effects. For instance, Combes (2000) finds for France that the local market size has a positive effect on industrial employment growth for manufacturing industries but a negative effect for service industries. Viladecans–Marsal (2004) finds for Spain that the effect on industrial employment is
not significant for three of six industries, while it has a bell-shaped effect in the three other industries. Blien et al. (2006), who extend the analysis of Blien and Suedekum (2005), obtain for Germany that local market size plays a positive role on industrial employment growth for both manufacturing and service activities. There are two recent studies on Italy, one that pools together manufacturing and service industries (Mameli et al., 2008) and one that focuses on business services (Micucci and Di Giacinto, 2009). Both conclude that total employment has a positive impact on industrial employment growth.

As we mentioned above, the question of the spatial decay of agglomeration effects is crucial. For the United States, Desmet and Fafchamps (2005) consider the impact on local employment growth of total employment and industrial employment share at various distances from the location. They show that for nonservice industries, such as manufacturing and construction, the effects are negative for distances below 20 km, but are slightly positive for distances between 20 and 70 km. This is consistent with employment moving away from city centers with high aggregate employment to nearby locations. Service industries exhibit a different pattern for the effect of total employment: the coefficients are positive at distances below 5 km, and are slightly negative at distances between 5 and 20 km. This is consistent with employment growing faster in city centers and more slowly in nearby areas. Unfortunately, this question has rarely been addressed for European economies. Viladecans-Marsal (2004) studies the effect on industrial employment of the local characteristics of neighboring cities in Spain. She finds the effects of total local employment and employment in neighboring locations to be significant in two of the six industries she considers. In the same vein, and still with Spanish data, Solé-Ollé and Viladecans-Marsal (2004) show that growth of the central municipality within metropolitan areas has a positive effect on growth in the suburbs. Micucci and Di Giacinto (2009) also find for Italy a significant impact of distant locations on local employment growth.

The impact of diversity on productivity has been found to be not robust, and this is also true for its effect on industrial employment growth. Whereas Glaeser et al. (1992) find a positive impact of diversity (measured by the share of the five largest industries within the city) on industrial employment growth, Henderson et al. (1995), who use a Herfindahl index over all local industries, obtain a significant positive effect in a couple of high-tech industries only. For France, Combes (2000) finds that the same diversity index has a positive impact on employment growth in service industries but a negative one in most manufacturing industries, although it is positive for a few of them. For Spain, Viladecans-Marsal (2004) finds a positive static effect on employment for three industries but a negative effect for some others and a nonsignificant effect for two of them. For Germany, Blien et al. (2006) find that diversity has a positive effect on employment growth in both manufacturing and service industries, the effect being strong in manufacturing industry. Diversity is also found to have a significant positive impact in Italy according to Mameli et al. (2008).
The impact of specialization is difficult to assess because its effect on agglomeration economies cannot be disentangled from the mean reversion process of industrial employment as shown earlier. The impact of specialization is found to be negative in both manufacturing and service industries in France by Combes (2000), in Germany by Blien et al. (2006), and in Italy by Mameli et al. (2008). This result may arise from strong mean reversion that more than compensates for positive agglomeration effects. Van Soest et al. (2006) obtain a positive effect of specialization in the Netherlands, but the impact is very local and dies out quickly with distance.

Glaeser et al. (1992) popularized the use of the local average size of firms in industry as a determinant of localization economies as discussed in Section 5.3.2. Both Combes (2000) for France and Blien et al. (2006) for Germany find that the presence of larger firms reduces employment growth in both manufacturing and service industries. To refine the role of local firm size, Combes (2000) introduces a local Herfindahl index of firm size heterogeneity. He finds that the local concentration of employment within large firms is also detrimental to local growth. Therefore, in France, the local market structure that fosters employment growth the most appears to be small firms of even size. A further example of the difficulty of interpreting the findings of this literature is given by Mameli et al. (2008), who show from Italian data that the effect of most local determinants on local employment is not very robust, in the sense that their sign changes depending on the industrial classification which is used.

Finally, local human capital is found to positively affect total employment growth, both in the United States by Simon (2004) and in Germany by Suedekum (2008). However, the latter study emphasizes that mostly unskilled employment growth is favored, which is consistent with the presence of strong substitution effects between the two groups of workers and weak agglomeration effects.

5.6.1.3 Dynamic specifications

A crucial question is the time needed for a determinant of agglomeration economies to have a sizeable effect. The availability of panel datasets has generated a series of articles that estimate jointly the dynamics of both the dependent local variable and local determinants of agglomeration economies in specifications with multiple lags involving both static and dynamic agglomeration effects. In other words, instead of estimating the specifications described in Section 5.6.1, researchers estimate full autoregressive models, as initially proposed by Henderson (1997) for US cities. Once this kind of model has been estimated, short-run effects of local determinants can be distinguished from their long-run effects.

For instance, Blien et al. (2006) show that in Germany the impact of diversity dies out quickly over time, in both the manufacturing sector and the service sector. This means that diversity has no long-run effects. Similarly, the effect of local firm size is significant in
the short run but not in the long run in the two sectors. As mentioned above, Combes et al. (2004) propose decomposing industrial employment into average employment per firm and the number of firms in the local industry. They then estimate from French data a vector autoregressive model involving these two dependent variables (this approach has been replicated with German data by Fuchs, 2011). It is found that the local determinants of the growth of existing firms are not necessarily the same as those that promote the creation of new firms. Overall, there is a greater inertia in the adjustment process in the United States than in France and Germany. Lagged values stop being significant after 1 year of lag for France and Germany. This is starkly at odds with the 6- or 7-year significant lags found in Henderson (1997) for the United States.

Unfortunately, as emphasized in Section 5.6.1.1, interpretations of estimated coefficients in terms of static and dynamic agglomeration effects remain very difficult because both types of effect can enter each estimated coefficient. Moreover, even if the structure of vector autoregressive models makes them rather suited to deal with endogeneity concerns by using dynamic panel estimation techniques, the application of such techniques is debatable in the context of agglomeration effects as argued in Section 5.4.3.3. Ultimately, the literature using dynamic specifications remains descriptive and is not really able to provide causal interpretations of the effects in terms of agglomeration economies.

5.6.2 Firms’ location choices

Rather than assessing the impact of local determinants of agglomeration economies on productivity or industrial employment, some authors have tried to evaluate the impact of these determinants on the location choices of firms. Firms should locate where their expected profit is the highest. As profit increases with productivity, the local determinants of productivity should also affect firm location choices. This is the intuition motivating the approaches presented in this subsection. They lead to applications usually relating to location choices of foreign direct investments (FDIs) or determinants of firm creation.

5.6.2.1 Strategies and methodological concerns

To assess the role of local determinants of firm location choices, Carlton (1983) proposes using the discrete choice modeling strategy developed by McFadden (1974). The idea is that, for any given firm, the value of each location depends on a deterministic local profit and an idiosyncratic component. The local profit is supposed to be the same for all firms, but the idiosyncratic component varies across firms (and components are identically and independently distributed across locations for a given firm). This prevents firms from all choosing the same location, which would not correspond to reality. Assuming that idiosyncratic components follow extreme value laws, the firm location choice follows a logistic model, or logit model, which is quite easy to estimate.

Economic geography models predict how firms distribute themselves across space according to local profits, which are nonzero in the short run under imperfect
competition. The location choice thus depends on the same quantities as those that enter the productivity equation (5.50) (the prices of goods and intermediate inputs, the technological level of the firm, and workers’ efficiency) as well as the nominal wage. As a result, any of the urbanization and localization variables which enter the empirical specification of productivity can be included in a specification explaining firm location choices. However, interpretations are even more difficult than in the case of industrial employment, as there are direct and indirect effects which sometimes go in opposite directions. Indeed, profits depend not only on productivity but also on input use and output quantity, which are themselves influenced by agglomeration effects but are not introduced in the regression. One can also choose whether or not to control for the local level of wages, but interpretations then differ as in the case of industrial employment. Therefore, proposing correct and precise interpretations is difficult because many effects are at play, and they interfere in nonlinear ways to shape local profits.

Furthermore, almost all the local variables explaining location choices can be considered to be endogenous, precisely owing to the location choices of both firms and workers. This induces reverse causality affecting most local determinants of agglomeration economies. Unfortunately, this kind of issue is tackled even less often in empirical studies on firm location choices than in the literature on the local determinants of productivity and employment. At best, authors lag explanatory variables by one period of time, which is certainly not enough to correct for any endogeneity bias that may occur. To cope with the problem of omitted local variables, some authors include regional dummies at a geographical scale larger than the one considered for location choices, while others exploit time series and introduce local fixed effects. The same important caveats appear as for productivity studies, and they are detailed in Section 5.4.3.

For all these reasons, the literature on firm location choices has to be considered as mostly descriptive. A safer route to assess the role of agglomeration effects on firm location choices would probably be to consider much more structural approaches, which however present the drawback of considering a more limited number of agglomeration channels.

Besides these limits, it is possible to enrich the approach when studying the location choices of firms among places in several countries using a nested logit model involving several stages. For instance, firms first choose the country to which they will locate and then, conditional on this choice, choose the region or city within the country. Two additive random components are now considered, one specific to the region and one specific to the country, and they are assumed to be independent. This structure produces a total random component correlated between regions within a given country, and the correlation can be estimated simultaneously with the other parameters in the model. In fact, the effects of local determinants of location choices at the different spatial scales are evaluated separately, once the geographical decomposition of the whole territory has been chosen (e.g., countries or continents, divided themselves into regions or cities). The nested logit approach has the advantage of limiting the number of possible locations
considered for a firm’s choice at a given stage. This can be a desirable feature considering current computer capacities, especially if some fixed effects (for industries or other geographical scales) are introduced in the model. These estimation strategies have been considered in empirical studies that take either a reduced form approach, such as Carlton (1983), or a more structural approach where firm location choices are part of an economic geography model, such as Head and Mayer (2004).

Research based on discrete location choice models has primarily been applied to FDI because the determinants underlying their location decisions are more discernible than those of domestic firms, which are less footloose. In particular, location choices are made by multinational firms in a relatively short period of time, without bearing the weight of historical contingencies like national firms. This makes them more appropriate candidates to test for the presence of agglomeration effects. An alternative approach adopted in a number of articles consists in considering the number of firm entries in a region as the dependent variable, and studying its determinants with a simple Tobit approach, or a count model such as the Poisson model or the negative binomial model, or even with a linear model. The Tobit model takes into account the left censorship of the dependent variable but considers that this variable is continuous. The main advantage of count models is that there is no computational limit on the number of alternatives such as in the logit model. However, there are strong distributional assumptions on residuals. The standard linear model does not impose any assumption on the distribution of residuals and is very flexible for the number of covariates that can be considered, but it ignores the discrete nature of the data and left censoring.

5.6.2.2 Discrete location choice models

Among early studies on the effect of local economy characteristics on location choices of FDI, Head et al. (1999) focus on the determinants of firm location choices between the 50 states of the continental United States, while Guimaraes et al. (2000) conduct a similar exercise for the 275 regions in Portugal, which are much smaller. Because of the urban and regional perspective of our survey, we do not discuss studies on location choices between countries. It may be noted, however, that their findings do not significantly differ from those for location choices within a country even if the nature of the underlying agglomeration economies is likely to differ.

As predicted by theory, the first factor that is almost systematically found to have a positive effect on location choices of FDI is the size of the local economy. For instance, market size is measured with local total income in Head et al. (1999), and with two variables, manufacturing and services employment, in Guimaraes et al. (2000). Among other determinants of firm location choices is market access. Guimaraes et al. (2000) consider the distance to the main cities in Portugal as a proxy. At the European level, Head and Mayer (2004) compare the performance of Harris and structural market
potential variables in explaining the location choices of Japanese affiliates across European regions at the NUTS 2 level. They find that both have a significant positive impact on these choices, even when controlling for a substantial number of other variables. Basile et al. (2008) analyze the location choices of multinational firms of various nationalities in 50 regions in eight EU countries. External market potential is found to have a significant positive effect as well as the own region total value added, which is considered simultaneously. However, both effects appear to be mainly driven by location choices of European multinationals, and they are not significant for non-European ones.

The positive impact of market potential seems to be fairly universal, and it is confirmed when data are disaggregated along various dimensions. For instance, Crozet et al. (2004) find a positive effect on FDI in France whatever the country of origin of firms. When studying FDI in Germany, Spies (2010) always finds a positive effect of market potential when conducting estimations for each industry separately. Pusterla and Resmini (2007), who focus on FDI in the NUTS 2 regions in four eastern European countries, find that both local manufacturing employment and market potential variables positively affect FDI, although most of the impact is on low-tech industries and not on high-tech ones.

As in the literature on productivity determinants, the functional form chosen for the role of distance in the market potential—the inverse of distance in most cases—assumes a fast spatial decay of agglomeration effects. The role of proximity has been further investigated. Basile (2004), for instance, finds a negative effect on FDI of agglomeration in adjacent provinces in Italy, while at the same time agglomeration in the own province has a positive effect. Interestingly, foreign acquisitions can be distinguished from greenfield investments. The effect of the local number of establishments is found to be significantly positive only for foreign acquisitions. However, local demand measured by electricity consumption, which is also introduced into the specification, has a positive influence on the two types of firms. Greenfield investments are more appealing for evaluating the role of agglomeration effects because firms have more freedom in their location choices.

This literature almost systematically considers the role of a variable absent from local productivity or growth estimations: past foreign presence in the region. This variable can have effects going in opposite directions. On the one hand, it may attract future FDI because it reflects unobservable characteristics of the region that are also beneficial to new FDI, or because it reflects an existing business network that may be useful to new FDI. On the other hand, past foreign presence may have a negative impact on new FDI because of competition effects. From a theoretical point of view, it is also difficult to assess how such a variable interferes with other local determinants of agglomeration economies, in particular the size of the local economy. As always, absent relevant instruments and natural experiments, identifying causal effects is very difficult.
Current FDI is shown to be positively correlated with previous FDI. For instance, past FDI is found to attract Japanese affiliates in European regions (Head and Mayer, 2004), and to induce both acquisitions and greenfield investments in Italy (Basile, 2004). Past investment also has an influence in both low-tech and high-tech industries in Germany (Spies, 2010), eastern European countries (Pusterla and Resmini, 2007), and Ireland (Barrios et al., 2006). Basile et al. (2008) find for European regions a positive effect of foreign presence on both European and non-European FDI. Crozet et al. (2004) study FDI in France by the country of origin and find a positive effect of past presence for specific countries only, the largest effects being observed for Japan, the United Kingdom, Belgium, and the United States. Finally, Devereux et al. (2007) find a positive effect of past foreign investment in the United Kingdom on both new investment by domestic firms and FDI, the effect being larger for FDI. The role of social and business networks has also been indirectly investigated through variables such as the distance to the home country or headquarters, which is found to have a negative impact on FDI in France by Crozet et al. (2004) and on European FDI in European regions by Basile et al. (2008). Generally, sharing a common language also has the expected positive effect on FDI, and this can be interpreted as indirect evidence of the presence of communication externalities.

As for productivity, authors also study the effect of local industry characteristics on location choices. FDI is fairly systematically found to be positively correlated with specialization, usually measured by the local count of domestic firms in the industry at the European level (Head and Mayer, 2004), or within countries such as in Portugal (Guimaraes et al., 2000), France (Crozet et al., 2004), or the United Kingdom (Devereux et al., 2007). Devereux et al. (2007) also find a positive impact of local industrial diversity. For Ireland, Barrios et al. (2006) find that diversity has had a significantly positive impact on FDI since the 1980s, but not before, and only for high-tech firms for which specialization has no impact. Conversely, whereas diversity does not matter for low-tech firms, specialization has a positive impact on low-tech FDI. Hilber and Voicu (2010) find for Romania that both domestic and foreign industry-specific agglomeration measures positively affect FDI, but only the effect of domestic agglomeration is robust to the introduction of regional fixed effects. The same is found for the effect of domestic industry-specific agglomeration in neighboring regions. The positive effect of diversity that is estimated without regional fixed effects is found to be not robust to their introduction.

Guimaraes et al. (2000) distinguish between the impact of manufacturing and service concentration, and find a larger impact from service concentration. This result was confirmed in later studies, in particular for eastern European regions. According to Cieślik (2005), service concentration has a significant positive large effect on FDI in Poland at the NUTS 3 level (49 regions), and the same is found for Romania at the NUTS 3 level (21 regions) by Hilber and Voicu (2010), even when region fixed effects are included in the specification. As an example, an increase of 10.0% in the density of service employment in a Romanian region makes the average Romanian region 11.9% more likely to attract a foreign investor.
As we can see, there are a variety of results that emphasize effects going more or less in the same direction but that remain difficult to compare (because authors usually estimate different specifications) and interpret (because of both the large number of possible effects and the possible presence of reverse causality).

These issues are even more important when studying the role of local labor markets in FDI as has been done in the literature. In particular, the impact of local labor costs has been investigated, but a significant concern is that authors are rarely able to control simultaneously for the local quality of labor. The labor cost per efficient unit of labor would be predicted by theory to influence location choices, but only the nominal cost is, in general, available. When labor efficiency is not taken into account, a positive impact of wages on the choice of a location may reflect the presence of high-skilled workers. Moreover, wages are simultaneously determined with firm location choices, and this endogeneity issue is usually not addressed. The endogeneity issue may be even more important when the local unemployment rates are introduced into the specification and microfoundations of the specification are even more unclear. A high local unemployment rate may reflect a large labor supply, and thus low wages or, on the contrary, wages that are too high and cause unemployment. Ultimately, owing to the lack of theoretical background for empirical specifications, we think that little can be learned from the impact of these variables. This is why we do not detail here their estimated effects, and we believe that a better use of theory will be required to really investigate the role of local labor markets.

5.6.2.3 Firm creation and entrepreneurship
Some recent literature argues that the location choices of new entrepreneurs and their determinants are worth studying because they should be more informative on the role and magnitude of agglomeration effects than the location choices of new plants by existing firms, as these choices are influenced by the locations of existing establishments of these firms. Unfortunately, as pointed out by Glaeser et al. (2010b), the literature on this topic is relatively small. Some contributions relate to the literature on innovations, and are surveyed in Carlino and Kerr (2015). We describe here some contributions that describe the determinants of firm creations in a more general way.

Among articles on the United States, Rosenthal and Strange (2003) show that firm creation is more important when the own-industry employment located within the first mile is larger, but the effect then vanishes rapidly with distance. Indeed, the impact within the first mile is 10–1000 times larger than the impact 2–5 miles away. They do not find any robust impact of urbanization on firm creation. Glaeser and Kerr (2009) propose disentangling among plant creations those that do not result from existing firms, as this is a better measure of entrepreneurial activity. The local level of activity appears to favor entrepreneurship, as it goes along with the presence of many small local suppliers. Glaeser et al. (2010a) find not that there are higher returns where entrepreneurs settle but that entrepreneurs rather choose places where there are larger local entrepreneurial
pools. Using the same dataset, and in the spirit of articles on determinants of local industrial employment, Delgado et al. (2010) augment the specification with dynamic effects and argue that mean reversion effects coexist with agglomeration gains.

Among contributions on other countries, Figueiredo et al. (2002) investigate the location choices of entrepreneurs in Portugal. Interestingly, they are able to distinguish between native and non-native entrepreneurs, and agglomeration effects are found only for non-natives. At a fine geographical scale, Arauzo-Carod and Viladecans-Marsal (2009) show for Spain that firm creation increases with own-industry previous entries. The effect is larger, the higher the technological level of the industry. Finally, Harada (2005) and Sato et al. (2012) find for Japan that a larger market size increases the willingness to become an entrepreneur, and that the effect is U shaped for the share of individuals that become entrepreneurs eventually. Put differently, people are more often entrepreneurs in both large and small locations. By contrast, Addario and Vuri (2010) find that population density reduces the probability of being an entrepreneur in Italy even if entrepreneurs’ earnings are larger in denser areas.21

Overall, there is a great variety of results, which may be related to the estimation of different specifications and the way endogeneity issues are handled, especially as these issues are not always addressed. Still, once the burgeoning literature on location choices of entrepreneurs is better related to theory, and takes better into account spatial sorting and reverse causality, it should deliver interesting conclusions on the local determinants of entrepreneurship.

5.7. IDENTIFICATION OF AGGLOMERATION MECHANISMS

The literature assessing the effects of local determinants of agglomeration economies on local outcomes estimates the overall net impacts of local variables, but it does not enter the black box of the underlying mechanisms at stake. Some attempts to identify some of these mechanisms have been made recently in three directions. A series of articles focuses on job search and matching effects, and evaluates whether agglomeration effects on productivity are related to the way local labor markets operate. Other authors have taken an indirect route by testing whether industrial spatial concentration or firms co-location relates to industry characteristics associated with the Marshallian three broad families of agglomeration mechanisms: labor pooling, knowledge spillovers, and input–output linkages. Lastly, a couple of case studies have been proposed to quantify specific agglomeration effects.

21 There is also recent literature on developing countries (see Ghani et al., 2013, 2014).
5.7.1 Labor mobility, specialization, matching, and training

Some of the gains from agglomeration arise from an increase in job mobility and better matching between workers and firms. Some studies assess whether agglomeration increases the frequency of workers’ moves between firms, industries, or occupations, as well as the chances for the unemployed of finding a job. Freedman (2008) studies the effect of specialization on workers’ job mobility and earnings dynamics for the software publishing industry in one anonymous state using a US longitudinal matched employer–employee dataset. Higher specialization in a 25 km radius increases the chances of moving between two software jobs. A wage regression also shows that specialization within a 25 km radius lowers the initial wage but is also associated with a steeper wage profile leading to a wage premium.

Using the National Longitudinal Survey of Youth, Wheeler (2008) evaluates the effect of local population, density, and diversity on mobility between industries depending on the number of previous job moves. When looking at a sample of first job changes, he finds that industry changes occur more often in large and diverse local markets than in small and nondiversified ones. Once several jobs have been held, the positive relationship becomes negative. As workers in large markets also tend to experience fewer job changes overall, the evidence is consistent with agglomeration facilitating labor market matching. In a similar spirit, Bleakley and Lin (2012) study the effect of the metropolitan area employment density on occupation and industry changes using US data. They instrument current local density with historical local density and current density at the state level. The rate of transitions of occupation and industry is found to be lower in denser markets, but the result is reversed for younger workers, which is consistent with the interpretation of Wheeler (2008). The local employment share in the own industry or the own occupation also has a negative effect on industry and occupation changes.

The effects of agglomeration variables on the job search process is investigated by Di Addario (2011) for Italy. She estimates the effects of local population and specialization on the probabilities for nonemployed individuals of searching for a job and becoming employed. Agglomeration variables are instrumented with historical population, seismic hazard, and soil characteristics. Overall, the results show that a larger local population and location in an industrial district or superdistrict increase the probability of being employed. Conversely, the impact of any variable on search behavior is found to be zero.

Some authors have investigated whether matches between workers and firms are more productive in larger/denser areas. Some approaches used to evaluate the effect of matching on productivity in a static framework are discussed in Section 5.2.3. In an application, Wheeler (2006) finds that wage growth is more important in large cities than in small ones and that this difference is mostly related to differences in wage growth when changing jobs. This is consistent with better matching in larger cities. However, this study does not take into account the endogeneity of job and location mobility.
This can be done using a more structural approach as explained in Section 5.2.4. Baum-Snow and Pavan (2012) estimate a structural model and find that match quality contributes little to the observed city size premium, in comparison with other static and dynamic agglomeration effects. Differences in the conclusions may be due to differences in the structure of the static and dynamic models, and more specifically how the endogeneity of individual choices is handled.

Alternative static approaches have been proposed to assess the role of match quality. Andersson et al. (2007) use matched worker–firm panel data on California and Florida to estimate a wage equation involving worker and firm fixed effects. They then compute for each county the correlation across firms between the firm fixed effect and the average worker fixed effect within the firm. The correlation is regressed at the county level on the average firm fixed effect, average worker fixed effect, and density. The estimated coefficient of density is found to be positive and significant, indicating improved matching in denser areas. Figueiredo et al. (2014) evaluate the effect of density on matches between workers and firms using Portuguese employer–employee panel data. Their empirical strategy has two stages. First, they estimate a wage equation involving worker, firm, and match effects. Second, estimated match effects are regressed on explanatory variables including, in particular, density and specialization, as well as worker and firm fixed effects. The estimated effect of density in the second stage is not significant. The effect of specialization is significantly positive at the 10% level only. What remains unclear is to what extent the sole match effect captures all complementarity effects between workers and firms. Wage is expressed in logarithmic form in the first-stage specification, which means that the exponentiated product of worker and firm fixed effects also captures complementarities.

Finally, Andini et al. (2013) assess for Italy whether there is an effect of density (and classification into an industrial district) on worker and firm individual measures of labor pooling. Density is measured at the local labor market level, and is instrumented using historical values. The individual outcomes are the change of employer or type of work, or both, workplace learning, past experience, training by the firm, skill transferability, difficulty of replacing the worker or finding another job, measures of specialization, and the appropriateness of experience and education. The firm outcomes are the share of terminations that are voluntary, the share of vacancies filled from workers previously employed in the same industry, and the number of days needed to train key workers, a measure of appropriateness of a new worker in terms of education and experience. Overall, the results support theories of labor pooling, but the evidence is weak, possibly owing to the small size of the datasets. In particular, there is some evidence of a positive effect of agglomeration on turnover, on-the-job training, and improvement of job matches.

Another possible mechanism that might lead to higher productivity in cities is task specialization. The underlying idea is that there are benefits to the division of labor, and this division is limited by the extent of the market. The division of labor is then expected to be greater in larger markets. There are a few bits of research on the
relationship between the division of labor and city size. Duranton and Jayet (2011) study this relationship using information on more than 5 million workers in 454 occupations and 114 sectors extracted from the 1990 French census. It is shown that even after the uneven distribution of industries across cities has been taken into account, larger cities exhibit a larger share of workers in scarcer occupations. For example, the difference between Paris and the smallest French cities is around 70%. For Germany, Kok (2014) shows that the specialization of jobs and the required level of cognitive skills increase with city size. To our knowledge, the links between city size, the division of labor, and productivity have not yet been investigated.

Lastly, some authors have investigated whether knowledge spillovers arise from the mobility of workers between firms within the same local labor market. Serafinelli (2014) shows that in the region of Veneto, Italy, hiring a worker with experience at highly productive firms significantly increases the productivity of other firms. According to his results, worker flows explain around 15% of the productivity gains experienced by other firms when a new highly productive firm is added to a local labor market. Combes and Duranton (2006) propose a model in which firms choosing their location anticipate that they can improve their productivity by poaching workers from other firms. However, their workers can be poached too unless they are paid higher wages, which makes firms’ production costs higher. Some authors have proposed testing this story indirectly by studying how training within firms varies with city size, the alternative to training being to poach workers who have already been trained from other firms. Brunello and Gambarotto (2007) for Italy, Brunello and Paola (2008) for the United Kingdom, and Muehlemann and Wolter (2011) for Switzerland show that indeed there is less on-the-job training in larger markets, and this is particularly true in the United Kingdom.

Overall, the literature on mobility, job search, and training comprises interesting attempts to determine the agglomeration mechanisms that relate to the labor market. It remains mostly descriptive though and would gain from considering approaches more grounded in theory.

### 5.7.2 Industrial spatial concentration and coagglomeration

Another strand of the literature has tried to identify the separate role of the three main types of mechanisms underlying agglomeration economies according to Marshall (1890): knowledge spillovers, labor pooling, and input–output linkages. For that purpose, a couple of articles augment the specifications of employment or firm creation presented in Section 5.6 with variables that should capture these three types of mechanisms. A larger number of articles, which we present first, compute spatial indices of concentration or coagglomeration for every industry, and then regress them on industry characteristics related to the three families of mechanisms. As analyses usually do not rely on a precise theoretical framework, this literature is for the moment mostly descriptive.
Kim (1995) was among the first to compute a spatial concentration index for some industries, in his case the Gini spatial concentration index (see Combes et al., 2008b), and regress it on industry characteristics and more particularly on average firm size. His purpose was to test the intuition that industries with stronger increasing returns to scale, which should be characterized by larger firms in equilibrium, are spatially more concentrated. The spatial concentration index is computed for a division of the United States into 9 large regions, for 20 industries, and for 5 points in time over the 1880–1987 period. The share of raw materials in production is introduced in the specification supposedly to control for the impact of comparative advantages on spatial concentration, and industry fixed effects are used to capture the role of industry effects that are constant over time.

There are major limitations to this kind of empirical strategy. Even simple economic geography models show that increasing returns to scale interact with trade costs and the degree of product differentiation to fix the degree of spatial concentration in equilibrium (see Combes et al., 2008b). However, only one industry characteristic among these three is introduced in the specification. It is thus necessary to make the strong assumption that either the two other characteristics are not correlated with the first one or they are sufficiently invariant over time to be captured by industry fixed effects. If trade costs and product differentiation indices were available, considering them in the specification would certainly not be straightforward since theoretical models usually predict highly nonlinear relationships between outcomes and underlying parameters. Introducing these characteristics as additional separate linear explanatory variables could be too extreme a simplification. Similarly, comparative advantage theory stresses the role of the interaction between factor intensity in the production function and regional factor endowments. Controlling for factor intensity but not for the distribution of endowments over space leads to ignoring the mechanism that generates regional specialization. Lastly, some mechanisms affecting spatial concentration, such as knowledge spillovers and labor pooling, are not taken into account either.

Further studies have tried to assess the role of additional agglomeration mechanisms by augmenting the estimated specification. The attempt by Rosenthal and Strange (2001) is an interesting one in this direction. The spatial concentration measure is the Ellison and Glaeser (1997) index computed for four-digit manufacturing industries in the United States. Variables for the three types of mechanisms are considered. Input sharing is measured by the shares of manufacturing and nonmanufacturing inputs in shipments. Knowledge spillovers are captured by innovations per dollar of shipment. Alternatively, some other authors also use R&D expenses. The measures of labor pooling are the value of shipments less the value of purchased inputs divided by the number of workers, the share of management workers, and the share of workers with at least a bachelor degree. These measures remain far from the intuition that industries with specific

22 They also use more detailed data, albeit on a shorter period of time.
needs for some labor skills gain more than others from concentrating. A number of other control variables are introduced, many of which relate to primary input use with the purpose of capturing again comparative advantage effects. As only cross-section data are available, industry fixed effects can be introduced only at the three-digit level and not at the four-digit level. The Ellison and Glaeser index takes into account in its construction an index of productive concentration that closely relates to the industry average plant size. Therefore, it is not clear whether or not one should control for firm size, and Rosenthal and Strange (2001) choose to leave it out of the specification.

The results obtained by Rosenthal and Strange (2001) are typical of this kind of study. Whereas labor pooling has a positive effect, knowledge spillovers have a positive impact on spatial concentration only when they are measured at a small scale (the zip code). Reliance on manufactured inputs affects agglomeration at the state level but not at a smaller scale. By contrast, reliance on service inputs has a negative effect on agglomeration at the state level. Overman and Puga (2010) propose an alternative indirect measure of labor market pooling. It is based on the assumption that a labor pool of workers with adequate skills allows firms to absorb productivity shocks more efficiently. Using UK establishment-level panel data, they construct an establishment-level measure of idiosyncratic employment shocks and average it across time and establishments within the industry. They find that industries that experience more volatility are more spatially concentrated.

Long ago, Chinitz (1961) suggested that examining the degree of coagglomeration of industries depending on their characteristics is another way to test for the presence of agglomeration economies. This approach is implemented in a systematic way by Ellison et al. (2010), who study the extent to which US manufacturing industries locate close to one another. The idea is to compute an index of coagglomeration between two industries and to regress it on measures of proximity between the two industries in terms of labor pooling, knowledge spillovers, and input–output linkages. Labor pooling is measured with the correlation of occupation shares between the two industries. Alternatively, some authors use a measure of distance between the distributions of these shares in the two industries. The share of input from the other industry and the share of output to the other industry are used as proxies for input and output linkages. Technological proximity is measured by two types of variables. The first type uses the shares of R&D flowing to and from the other industry. The second type uses patent citations of one industry made by the other industry. Such variables are, in general, not symmetrical. For instance, the first industry can cite the second industry more than the second industry cites the first industry. Therefore, it is the maximum value of the variable for the two industries that is used in the regressions.

Importantly, in order to control for comparative advantage effects, Ellison et al. (2010) introduce among the explanatory variables a coagglomeration index of spatial concentration due to natural advantages, which is an extension of the natural advantages spatial concentration index proposed by Ellison and Glaeser (1999). Results are also
provided for alternative coagglomeration indices. Indeed, a standard index such as the one of Ellison and Glaeser considers a classification of spatial units across which the economic activity is broken down and measures the concentration in these units. A limitation is that the relative location of units and the distances that separate them are not taken into account. As a result, the index is invariant up to any permutation of the units. For instance, it takes the same values if one relocates all units with large amounts of activity close to the center of the economy or if one locates them at the periphery. Alternative measures of spatial concentration and coagglomeration have been developed by Duranton and Overman (2005) to deal with this issue. They are based on the distribution of distances between establishments and can be computed for any spatial scope. One can assess whether there is concentration for a distance between establishments of 5 miles, 10 miles, and so on. Ellison et al. (2010) also estimate their specifications using the Duranton and Overman index computed for a distance of 250 miles. Finally, since explanatory variables are computed from the same quantities as the dependent variable, there might be endogeneity issues, and Ellison et al. (2010) propose instrumenting explanatory variables with similar variables constructed from UK data instead of US data.

The results give some support to the three types of agglomeration mechanisms. The largest effect is obtained for input–output linkages, followed by labor pooling. Kolko (2010) conducts a similar exercise for both manufacturing and service industries, using as additional measures of the links between industries variables related to the volume of interindustry trade. He studies both agglomeration and coagglomeration at various spatial scales: zip code, county, metropolitan area, and state. The limitations are that he does not use distance-based concentration indices such as the Duranton and Overman index, he does not control for spatial concentration due to natural advantages, and he does not deal with endogeneity issues using instrumentation. Ultimately, trade between industries appears to be the main driver of industry coagglomeration for both manufacturing and services. More precisely, service industries that trade with each other are more likely to colocate in the same zip-code area, although not in the same county or state; by contrast, manufacturing industries that trade with each other are more likely to colocate in the same county or state but not in the same zip-code area. Input sharing also positively affects coagglomeration for both manufacturing and services at any spatial level, and this is true for occupational similarity to some extent as a positive effect is found but only for services and at the zip-code level. As regards spatial concentration, labor pooling is the only variable having a significant impact. Its effect is positive but occurs in the manufacturing sector only.

Kerr and Kominers (2015) further study the determinants of spatial concentration in the spirit of Ellison et al. (2010). They compute the Duranton and Overman spatial concentration index for different industries and different distances. Values are pooled together and then regressed on dummies for distances interacting with an industry measure of knowledge spillovers, and then alternatively an industry measure of labor pooling.
The proxies used for these determinants are slightly different from those in other studies. As regards knowledge spillovers, Kerr and Kominers (2015) consider the citation premium for 0–10 miles relative to 30–150 miles. Labor pooling is captured by a Herfindahl index of occupational concentration computed over 700 categories. Most estimated coefficients obtained for interactions with dummies for distances decrease with distance, and they are significantly different from zero for short distances only. This suggests that establishments in industries with shorter knowledge spillovers or more labor pooling are more concentrated. Similar results are obtained whether one uses US data or UK data to compute measures of knowledge spillovers and labor pooling. Nevertheless, estimations for these two channels of agglomeration economies are conducted separately without confronting them in a single regression. Finally, estimated coefficients for interactions between dummies for distances and dependency on natural advantages tend to increase with distance and are significant for large enough distances only. This is consistent with the intuition that industries more dependent on natural advantages are more dispersed.

A difficulty faced by this literature is that the dependent variable is a complex function of certain quantities, such as local industrial employment, which relate to the quantities describing firms and establishments within the industry that are used in the construction of explanatory variables. Therefore, it is not easy to argue about expected effects of explanatory variables in equilibrium, and this makes interpretations difficult. In light of this difficulty, Dumais et al. (1997) in a section not included in Dumais et al. (2002) propose re-examining the literature on industrial employment in order to assess the role of some specific agglomeration channels. They consider a specification where local industrial employment is used as the dependent variable instead of an index of spatial concentration in the industry. Proxies for Marshallian externalities are constructed at the local level using the following strategy. Measures of proximity between industries as regards knowledge spillovers, labor pooling, and input and output linkages are computed at the national level. For a given type of agglomeration channel, the local variable for an industry is then computed as the sum over all other industries in their proximity weighted by the share of these industries in the location. These local variables are also sometimes interacted with some of the local determinants of industrial employment presented in Section 5.6.1. All these terms serve as explanatory variables in the specification of local industrial employment.

Recently, a similar strategy has been implemented by Jofre-Montseny et al. (2011) to determine the effects of the different types of agglomeration economies on the location of new firms in Spain at the municipality level and city level. In the same vein, Jofre-Montseny et al. (2014) estimate from Spanish data, for each industry separately, a firm location model with two main local explanatory variables, local employment within the industry and in other industries. The industry-specific estimates for these

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23 Articles using the same strategy but for the study of agglomeration economies on TFP include those of Rigby and Essletzbichler (2002), Baldwin et al. (2010), Drucker and Feser (2012), and Ehrl (2013).
two variables are then regressed on industry characteristics with proxies for knowledge spillovers, labor pooling, input sharing, and energy and primary input use. We emphasized above the difficulty in interpreting estimates of employment growth specifications, while Jofre-Montseny et al. (2014) propose further extending these specifications by introducing interactions between local determinants and factors influencing the different agglomeration forces at the industry level. Such extended empirical frameworks are necessarily even more ambiguous and difficult to interpret than the basic employment growth specifications that we discussed in Section 5.6.1.

Overall, this strand of literature is an interesting effort to identify the mechanisms underlying agglomeration economies. Ultimately though, it is very difficult to give a clear interpretation of the results, and the conclusions are mostly descriptive. This is due to the weak links between estimated specifications and theoretical models. Another concern is whether the right measure of concentration or coagglomeration has been chosen. The exact properties of concentration indices, even measures à la Duranton and Overman (2005), still need to be established. Moreover, one needs to assume that industry characteristics used as explanatory variables really capture the mechanisms they are meant to, and have additive linear effects, whereas this is not certain. For instance, according to theory, two industries sharing inputs have more incentive to colocate when trade costs for these inputs are large. In that perspective, variables capturing input–output linkages should be caused to interact with a measure of trade costs, but this is not done in the literature. Finally, there are probably some endogeneity issues since the dependent variable and the explanatory variables are usually computed from the same quantities. However, the presence and channels of endogeneity are difficult to assess, and it is hard to conclude that some instruments are valid, as estimated specifications have usually not been derived from any precise theoretical framework. On the other hand, since the overall impact of agglomeration on productivity can be evaluated with reasonable confidence nowadays as we emphasized in previous sections, we think that investigating the relative magnitude of agglomeration channels is an important and promising avenue for future research. The descriptive evidence presented in this subsection could be used to build theoretical models from which specifications could be derived, allowing the identification of agglomeration channels and strategies to tackle endogeneity concerns. Structural approaches applied to case studies, which are presented in the next subsection, constitute some first steps in that direction.

5.7.3 Case studies

Some specific mechanisms of agglomeration economies can be assessed through case studies of firms or industries for which the nature of possible density effects are known and can be specified.

An interesting structural attempt to evaluate the importance of agglomeration economies in distribution costs is proposed by Holmes (2011). The study focuses on the
diffusion of Wal-Mart across the US territory and considers the location and timing of the
opening of new stores. These new stores may sell general merchandise and, if they are
supercenters, they may also sell food. When operating a store, Wal-Mart gets merchan-
dise sales revenues but incurs costs that include not only wages, rent, and equipment costs,
but also fixed costs. These fixed costs depend on the local population density as well as the
distance to the nearest distribution center for general merchandise and, possibly, the dis-
tance to the nearest food distribution center. Higher store density usually goes along with
shorter distance from distribution centers. When opening a new store, Wal-Mart faces a
trade-off between savings from a shorter distance to distribution centers and cannibali-
zation of existing stores. The estimation strategy to assess the effects of population density
and proximity to distribution centers is the following. The choice of consumers across
shops is modeled and demand parameters are estimated by fitting the predicted merchan-
dise and food revenues with those observed in the data. An intertemporal specification of
the Wal-Mart profit function taking into account the location of shops is then considered.
In particular, this function depends on revenues net of costs, which include wages, rent,
and equipment costs as well as fixed costs. For a given location of shops, net revenues can be
derived from the specification of demand, where parameters have been replaced by their
first-stage estimators. To estimate parameters related to fixed costs, Holmes (2011) then
considers the actual Wal-Mart choices for store openings as well as deviations in which
the opening dates of pairs of stores are reordered. Profit derived for an actual choice of store
openings must be at least equal to that of deviations. This gives a set of inequalities that can
be brought to the data in order to estimate bounds for the effects of population density and
distance to distribution centers. It is estimated that when a Wal-Mart store is closer by 1
mile to a distribution center, the company enjoys a yearly benefit that lies in a tight interval
around $3500. This constitutes a measure of the benefits of store density.

The benefits from economies of density in agriculture related to the use of neighbor-
ing land parcels are evaluated by Holmes and Lee (2012). When using a particular piece of
equipment, a farmer can save on setup costs by using it across many fields located close to
each other. Moreover, if a farmer has knowledge of a specific crop, it is worth planting
that crop in adjacent fields, although this may be at the expense of reducing the crop
diversity that can be useful against risks. The analysis is conducted on planting decisions
in the Red River Valley region of North Dakota, for which there are a variety of crops
and years of data on crop choice collected by satellites. More precisely, the focus is on
quarter sections which are 160-acre square parcels. These sections can be divided into
quarters of 40 acres, each designed as a field. The empirical strategy relies on a structural
model where farmers maximize their intertemporal profit on the four quarters of their
parcels, choosing for each quarter the extent to which they cultivate a given crop (rather
than alternative ones). Production depends on soil quality and the quantity of investment
in a particular kind of equipment useful to cultivate the specific crop but which has a cost.
It is possible to show that because of economies of density arising from the use of the
specific piece of equipment on all quarters, the optimal cultivation level for a crop on a quarter depends not only on the soil quality of this quarter but also on that of the other quarters. The specification can be estimated and parameters can be used to assess the importance of economies of density. Results show that there is a strong link between quarters of the same parcel. If economies of density were removed, the long-run planting level of a particular crop would fall by around 40%. Two-thirds of the actual level of crop specialization can be attributed to natural advantages and one-third can be attributed to economies of density.

5.8. CONCLUSION

Most of the literature identifies the overall impact of local determinants of agglomeration economies, but not the role of specific mechanisms that generate agglomeration effects. This is already a crucial element when assessing the role of cities. Major progress has been made in dealing with spatial sorting of workers and firms as well as endogeneity issues due to missing variables and reverse causality, especially when assessing the effect of density on productivity.

We developed a consistent framework that encompasses both the early attempts to estimate agglomeration effects using aggregate regional data and more sophisticated strategies using individual data, recently including some structural approaches. This allowed us to discuss most empirical issues and the solutions that have been proposed in the literature. We also presented the attempts to study the determinants of other local outcomes—namely, employment and firm location choices—but more investigations are still needed. For instance, further theoretical and empirical clarifications would be useful when studying the determinants of local employment in order to better disentangle the short-term dynamics from long-term effects, and the respective role of labor demand and supply. The determinants of firm location choices have benefited so far from a very limited treatment of selection and endogeneity issues. Surprisingly, the impact of agglomeration economies on unemployment has received little attention and deserves more work at least from a European perspective as regional disparities in unemployment rates there remain large. Finally, identifying the channels of agglomeration economies is also clearly important, but the related literature remains limited except for some contributions on innovation that are surveyed in Carlino and Kerr (2015). Meaningful strategies relying on sound theoretical ground to provide an empirical assessment of channels of agglomeration economies are still needed, and current evidence while being interesting is rather descriptive.

Some researchers have started to investigate routes complementary to those mentioned in this chapter. First, the existence of a spatial equilibrium implies that agglomeration costs are a necessary counterpart of agglomeration gains. This prediction is
supported by Gibbons et al. (2011), who show that in Great Britain there is an almost one-for-one relationship between local housing costs and nominal earnings, which are higher in larger cities, once the effects of housing quality and workers skills are taken into account. Second, some authors have gone a step further by looking at the implications in terms of welfare of the simultaneous presence of agglomeration costs and gains. However, some effects have not yet been considered in the analyses, whereas they have some importance from a policy perspective. For instance, considering how city size affects environmental concerns or road congestion costs is important for designing urban policies that improve welfare.

There have been only a few early independent attempts to evaluate agglomeration costs, and they are for developing countries only (Thomas, 1980; Richardson, 1987; Henderson, 2002). Recently, housing and land prices have started to be investigated more systematically, although articles usually rely for their analyses on datasets that are not comprehensive. There are a few rare exceptions, such as Davis and Heathcote (2007) and Davis and Palumbo (2008) on the whole United States, or Combes et al. (2012a) on the determinants of land prices in French urban areas. This last article estimates the elasticity of land prices with respect to city population, from which the elasticity of urban costs is recovered. Its magnitude is found to be similar to that of the elasticity of agglomeration gains on productivity. Albouy and Ehrlich (2013) replicate the approach to investigate the determinants of land prices in US metropolitan areas. Finally, some authors have tried to exploit natural or controlled experiments, such as Rossi-Hansberg et al. (2010), who use residential urban revitalization programs implemented in Richmond, Virginia, to evaluate the effect of housing externalities on land value.

Housing is not the only good whose price varies across locations, but little is known for other types of goods. Using barcode data on purchase transactions, Handbury and Weinstein (2015) and Handbury (2013) assess how prices of grocery products vary with city size. Handbury and Weinstein (2015) find that raw price indices slightly increase with city size, and this would constitute an additional source of agglomeration costs for households. However, this result is obtained before correcting prices for quality differences across varieties and before taking into account effects related to preferences for diversity that are present when considering CES utility functions. Once these are taken into account, price indices decrease with city size. This is the typical agglomeration gain that can be found in economic geography models with mobile workers à la Krugman (1991b). The price index decrease is due mostly to a much larger number of available varieties in larger cities, but is also due to a higher quality of varieties sold there. Handbury (2013) allows preferences to differ between rich and poor households, and obtains the further result that the price index decreases with city size only for rich households but increases for poor ones. Clearly, investigating further these types of agglomeration effects is high on the agenda.
Lastly, since there is evidence that gains and costs from agglomeration as well as location choices differ across types of workers, there is a need to consistently reintroduce space in welfare analyses when one wishes to assess individual or household inequalities. Moretti (2013) shows that real wage disparities between skilled and unskilled workers have increased less over the last 30 years than what nominal wage disparities would suggest, once the increase in the propensity of skilled workers compared with unskilled workers to live in larger cities has been taken into account. Indeed, the increase in the difference in housing costs between skilled and unskilled workers represents up to 30% of the increase in the difference in nominal wages. Albouy et al. (2013) show that Canadian cities with the highest real wage differ for English speakers and French speakers.

However, this type of real wage computation does not consider differences in amenity endowments across cities and possible differences in the valuation of amenities across worker groups. As workers are mobile, differences in real wages across locations should reflect to some extent differences in amenity value (see Roback, 1982). Albouy et al. (2013) show that indeed the real wage they compute for Canadian cities is slightly correlated with arts and climate city ratings. For the United States, Albouy (2008) and Albouy (2009) find that the most valuable cities have coastal proximity, sunshine, and mild seasons. These findings are in line with those of Desmet and Rossi-Hansberg (2013), who use a slightly more general model calibrated on US data to assess the welfare impact of eliminating differences in amenities or frictions (within-city commuting time, local taxes, government expenditure) between cities. Diamond (2013) takes into account workers’ heterogeneity and shows that the increased skill sorting in the United States is partly due to the endogenous increase in amenities within high-skill cities.

Some recent theoretical contributions such as those of Behrens et al. (2014), Eeckhout et al. (2014), and Behrens and Robert-Nicoud (2014) suggest that sorting and disparities are worth studying simultaneously within and between cities. Glaeser et al. (2009) and Combes et al. (2012c) show that indeed larger cities present larger dispersions of wages and skills, respectively, in the United States and France. Baum-Snow and Pavan (2013) further document the emergence of both within–city and between–city inequalities in wages and skills in the United States. A full empirical welfare assessment of both within–city and between–city disparities considering agglomeration costs and benefits, heterogeneous workers that are imperfectly mobile, and amenity data in addition to productivity measures as well as land and housing prices is a challenge for future research.

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